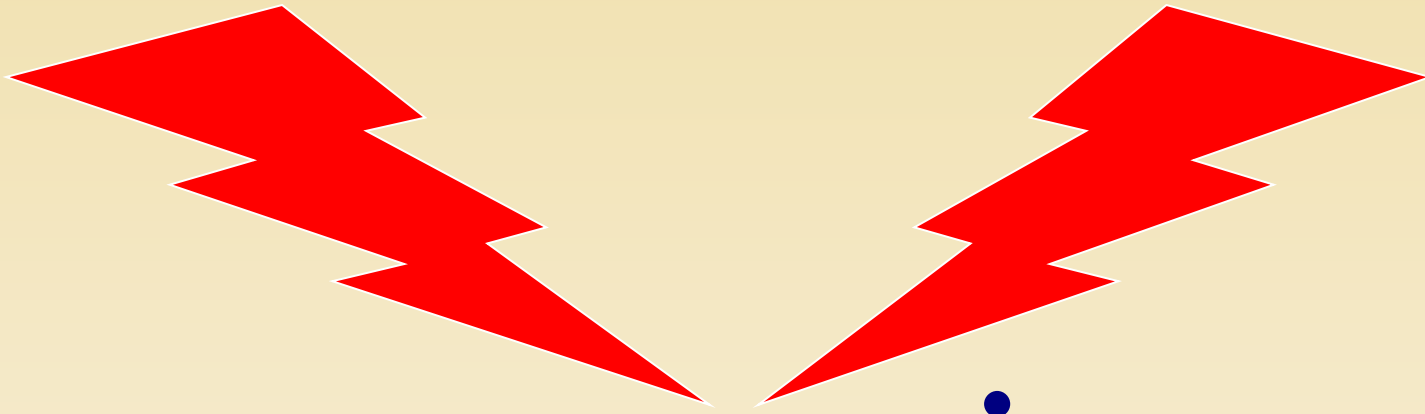


# weak bosons



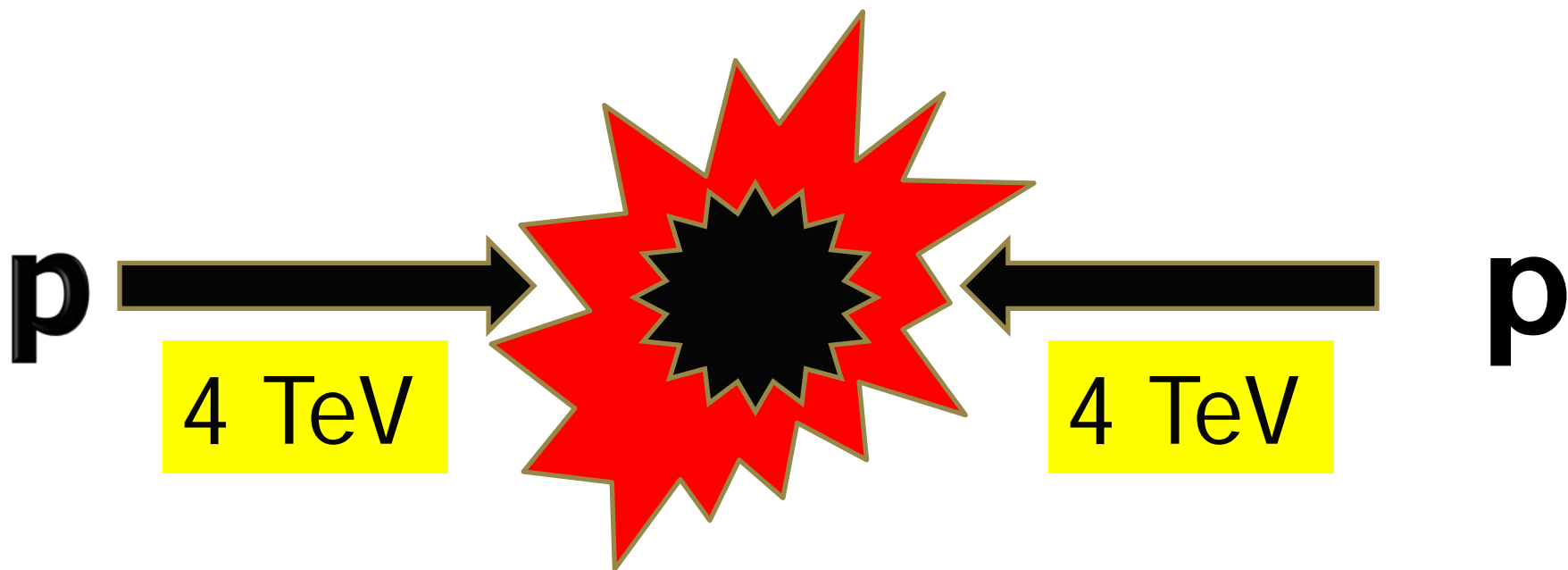
## composite

H. Fritzsch

LMU Munich

An aerial photograph of a vast valley with a yellow circular outline overlaid on it. The outline has eight small yellow circles at regular intervals along its perimeter. In the center of the image, there is a white rectangular box with a gradient background containing the text 'LHC' in a bold, blue, sans-serif font. The background shows a wide expanse of green and brown fields, with distant mountains under a clear blue sky.

**LHC**



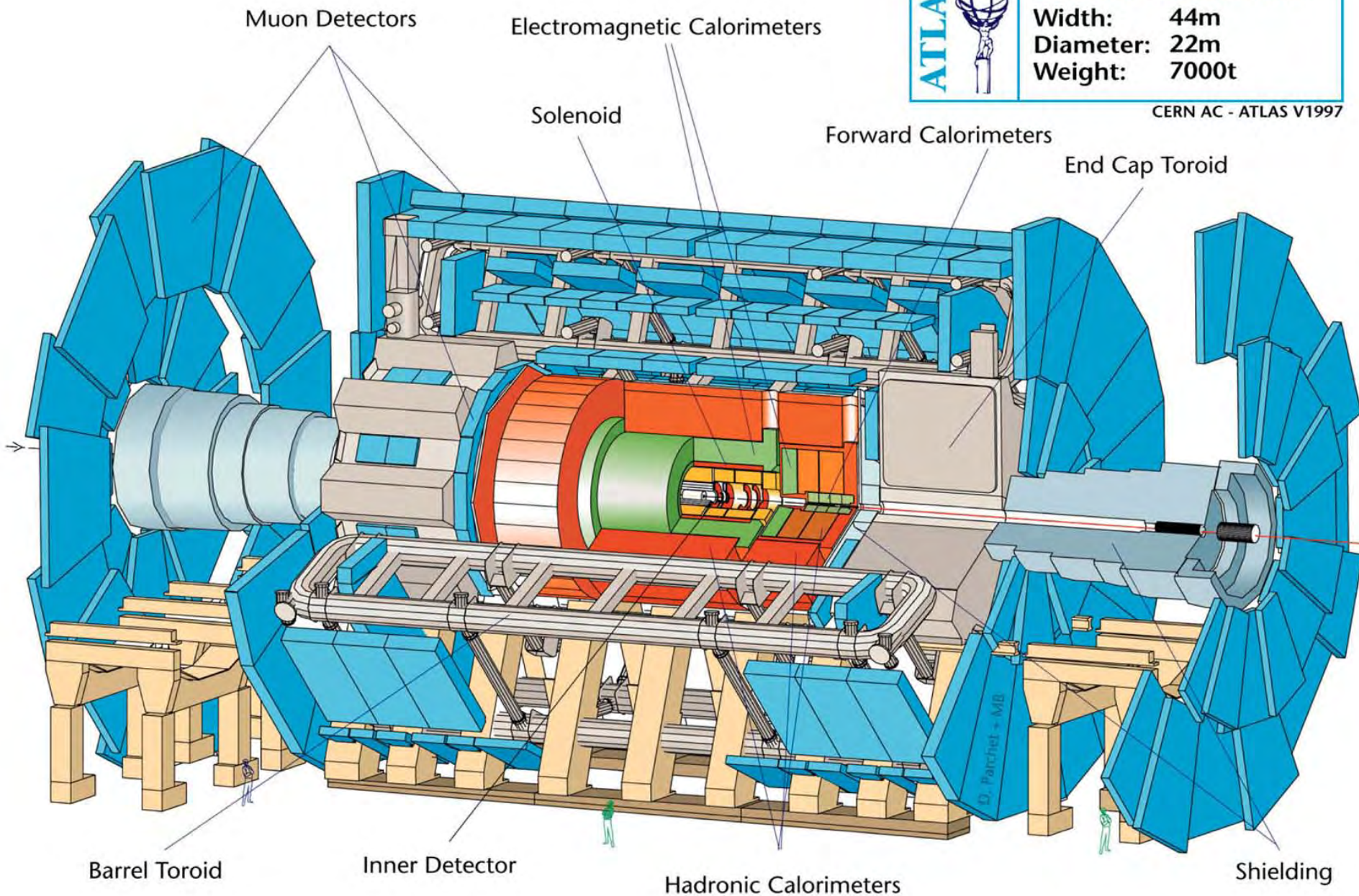
# ATLAS at Large Hadron Collider / CERN

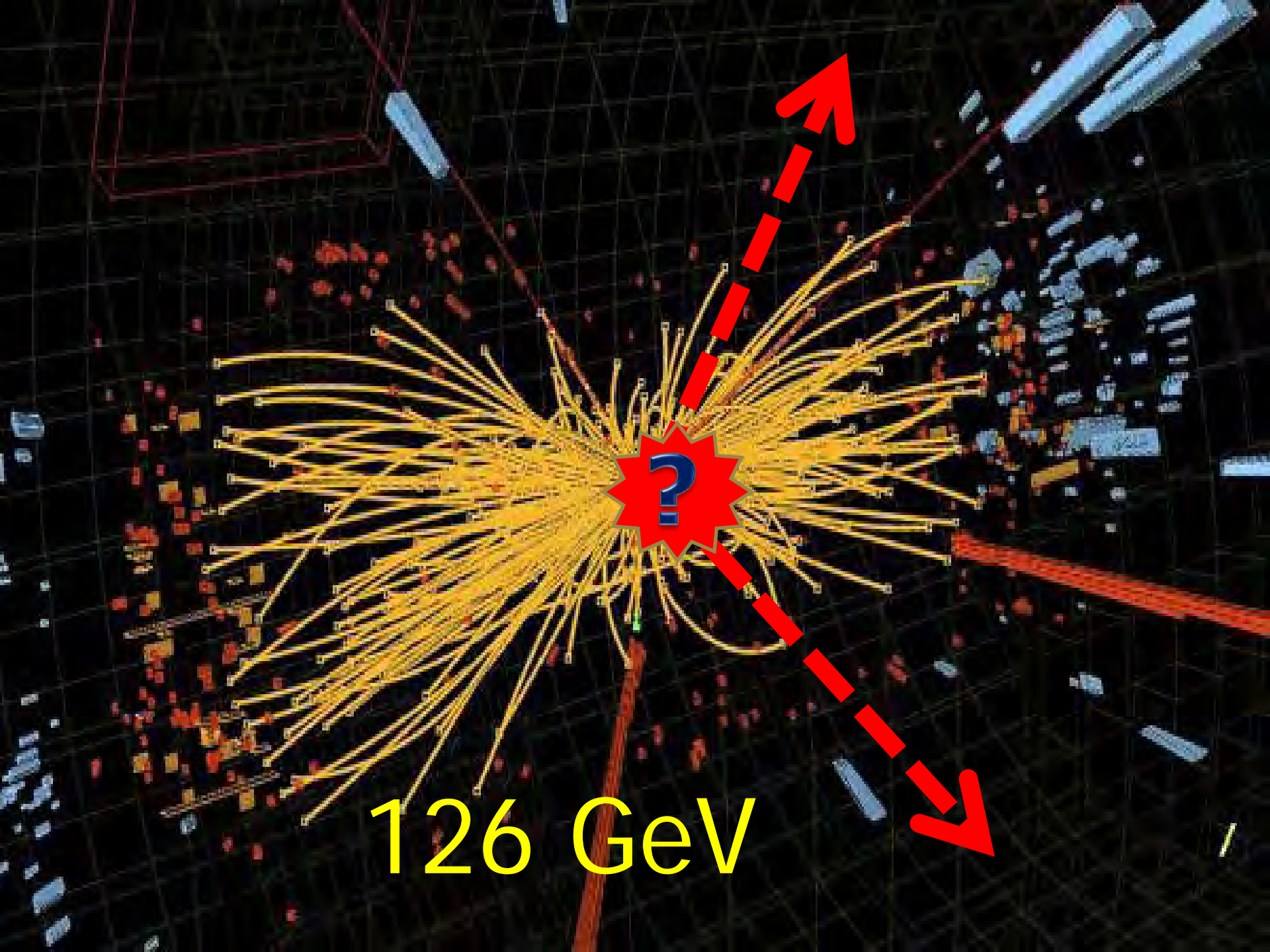


## Detector characteristics

**Width:** 44m  
**Diameter:** 22m  
**Weight:** 7000t

CERN AC - ATLAS V1997





126 GeV

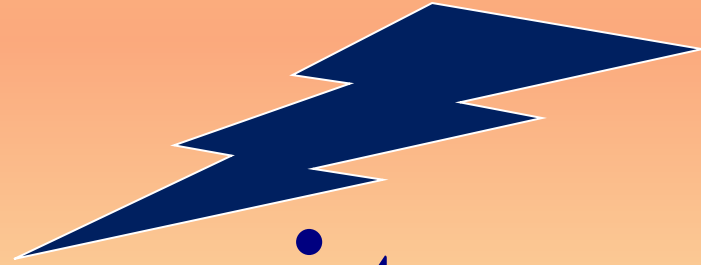
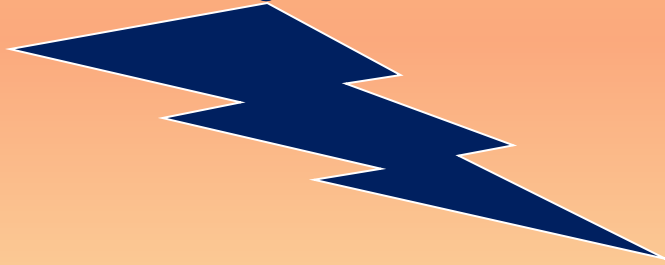
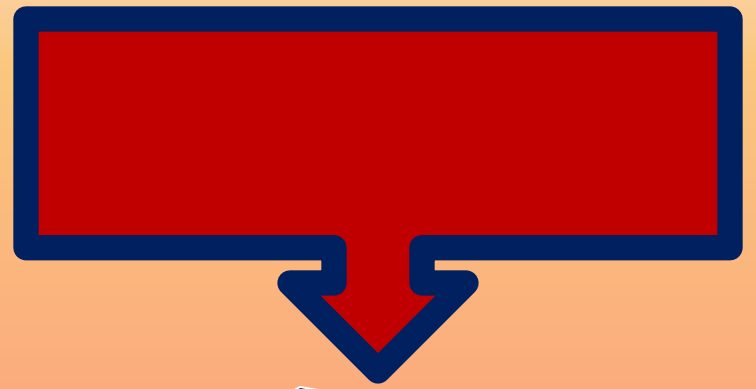
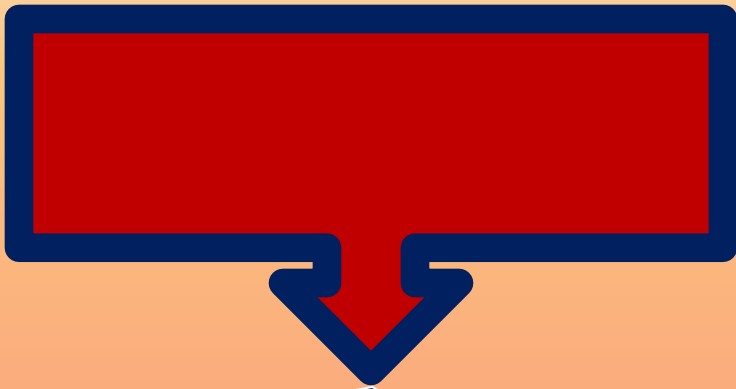
?

excited

weak boson

spin 0

# weak bosons



# composite

# Standard Model

quarks + leptons

weak bosons



pointlike



# SLAC – DESY

## LEP - Tevatron

radius of electron:

$$\leq 10^{-17} \text{ cm}$$

radius of u/d-quark:

# STANDARD MODEL

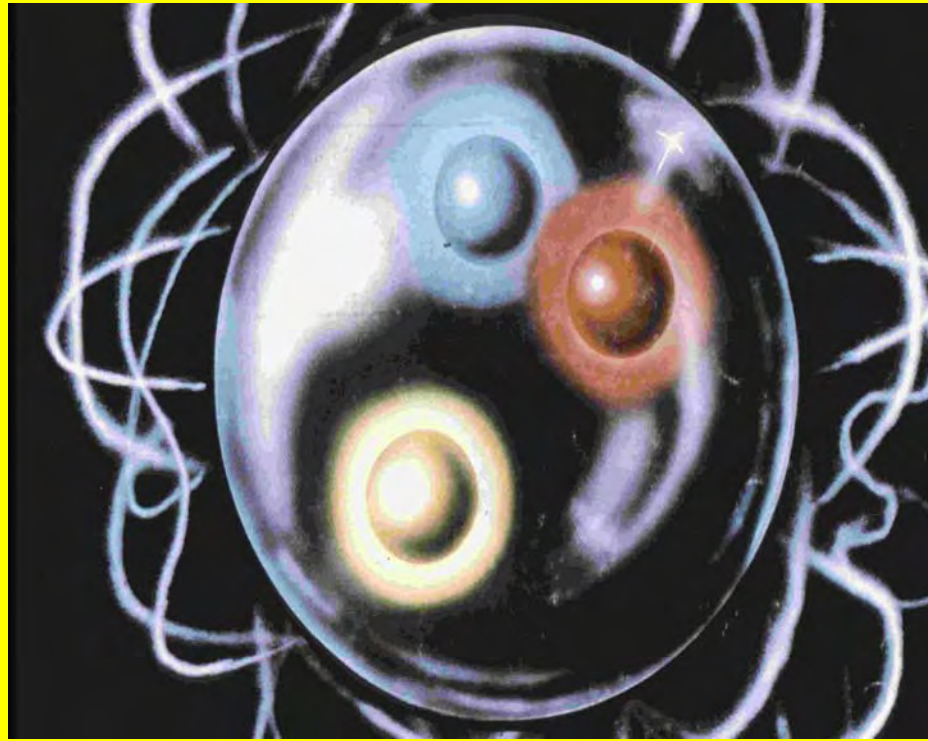
**! Mass of Proton !**

**? Mass of Weak Boson ?**

**proton  
mass**



**field energy of  
gluons and quarks**



$$E(\text{gluons}) + E(\text{quarks}) = M_p c^2$$

**70 %**

**30%**

**Mass**

**of**

**Weak Boson**

**???**

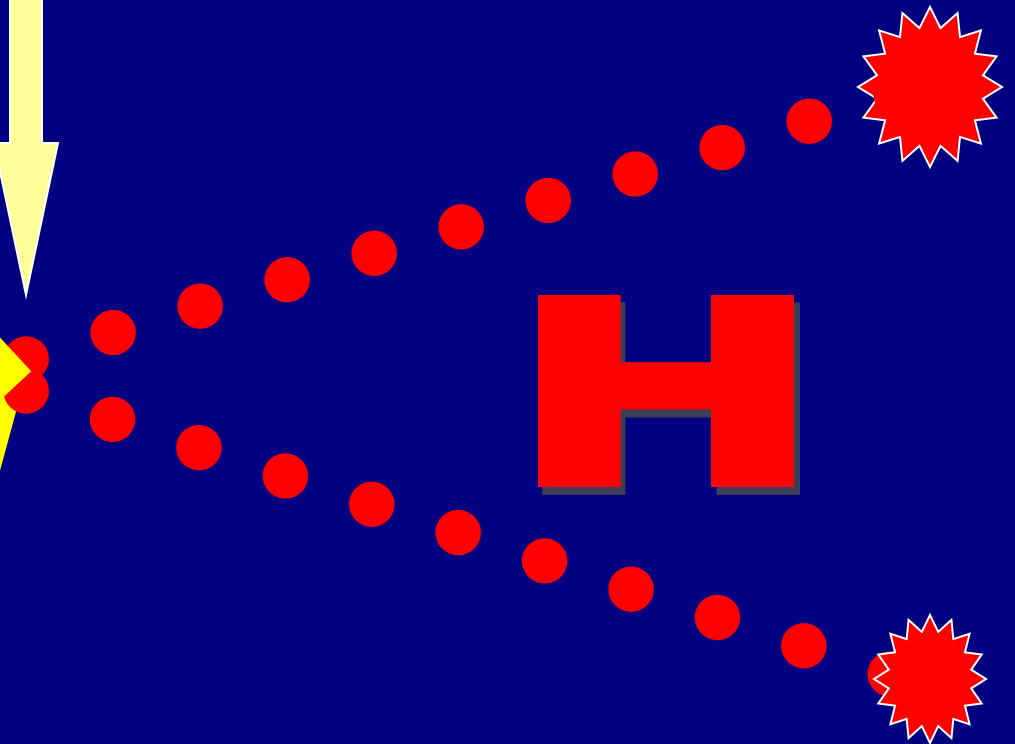
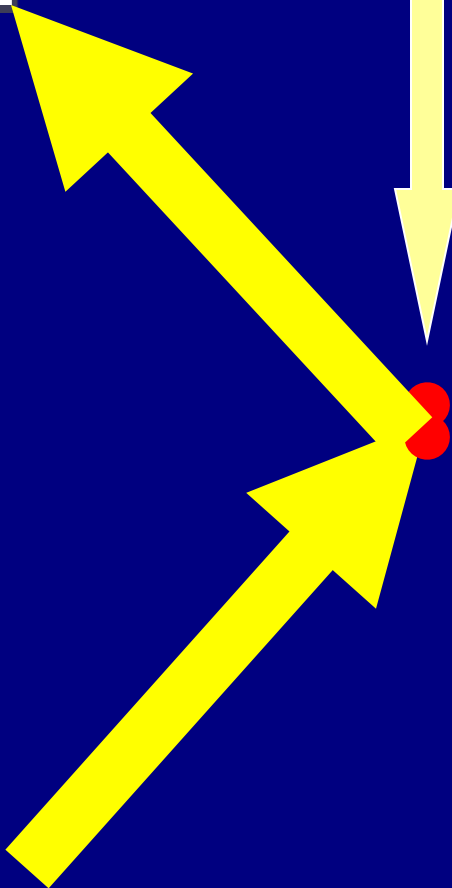
# **spontaneous symmetry breaking**



***“Higgs” - mechanism***

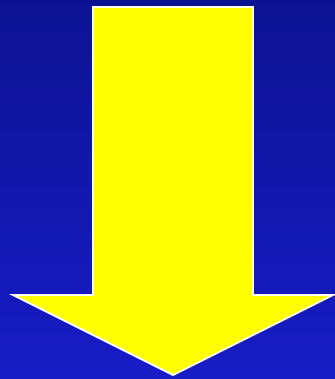


# weak boson mass



***alternative:***

**mass generation**



**confinement**



# Example

## $\rho$ - mesons

„Higgs“  
mechanism

~ 1960: J. J. Sakurai

**rho mesons**



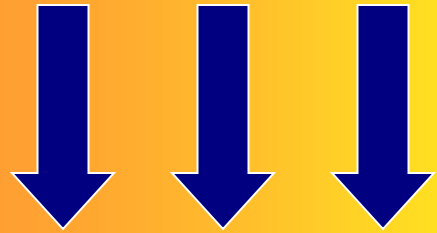
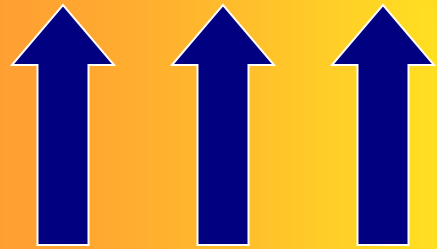
**elementary  
gauge bosons**

~ 1964

mass generation  
for rho mesons

„Higgs“  
mechanism

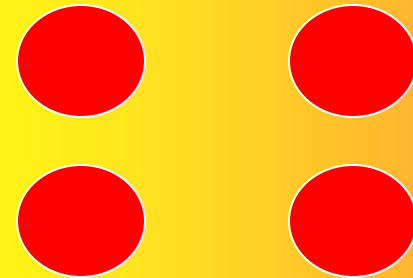
# **SU(2)**



**massless**

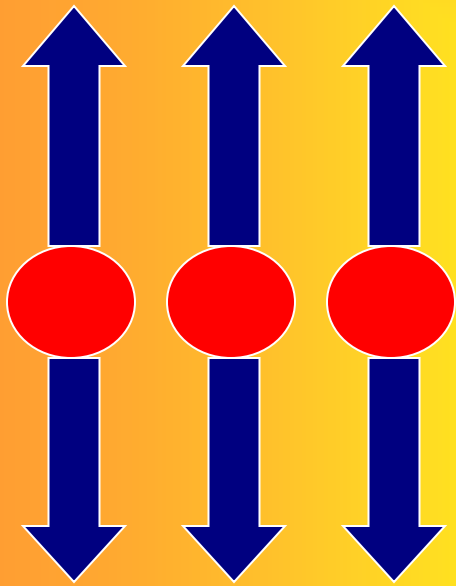
**rho - mesons**

2 x 2 scalars



**mass M**

# “Higgs” - mechanism



„Higgs” - scalar

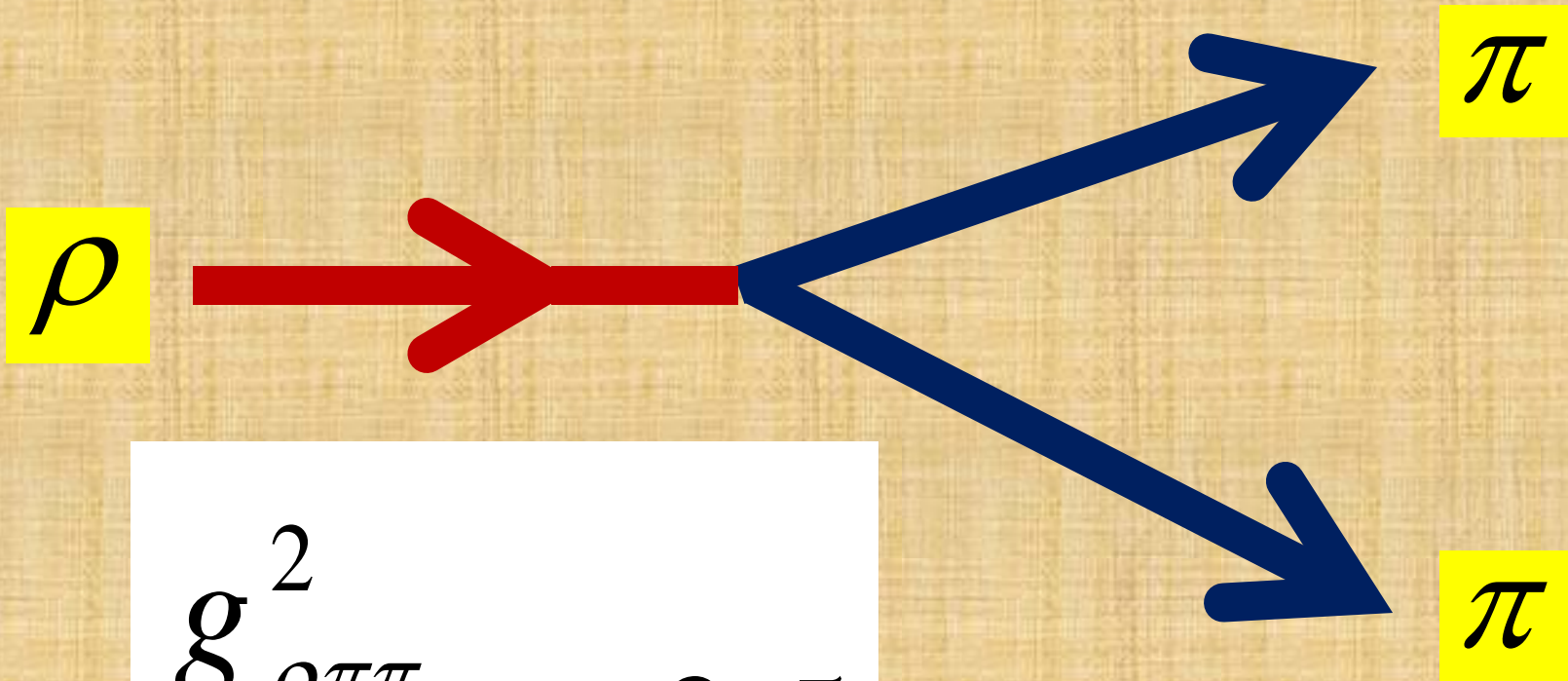


**mass M**

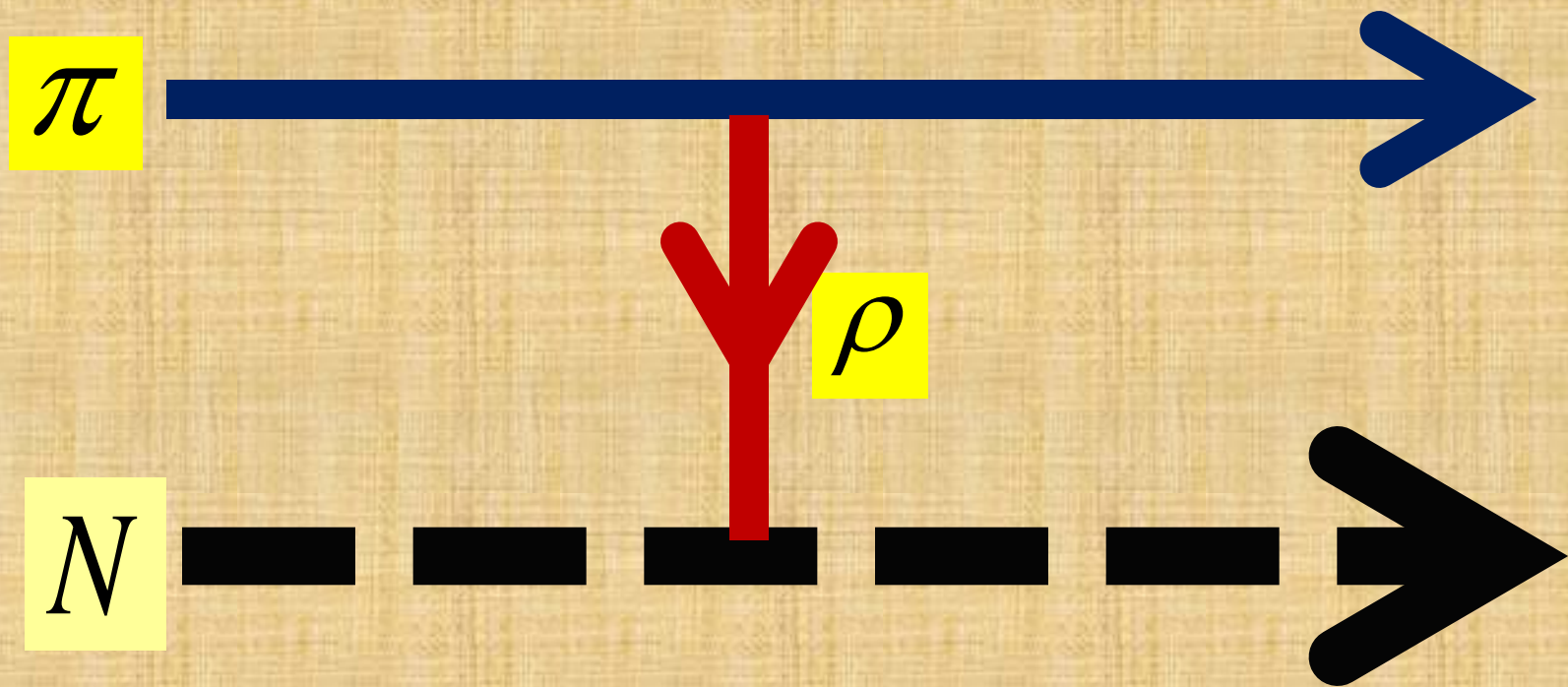
**massive**

**rho - mesons**

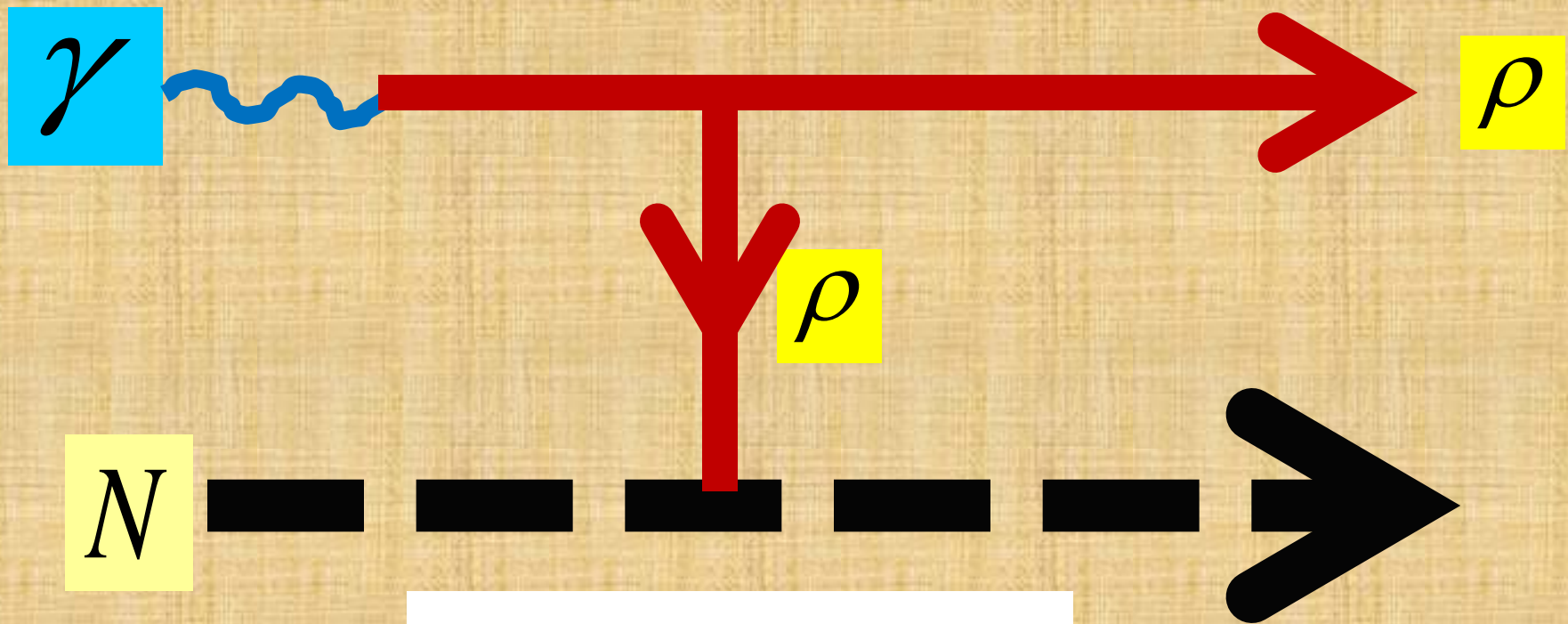
# UNIVERSALITY



$$\frac{g_{\rho\pi\pi}^2}{4\pi} \approx 2.5$$



$$\frac{g_{\rho NN}^2}{4\pi} \approx 2.5$$



$$\frac{g_{\rho\rho\rho}^2}{4\pi} \approx 2.5$$

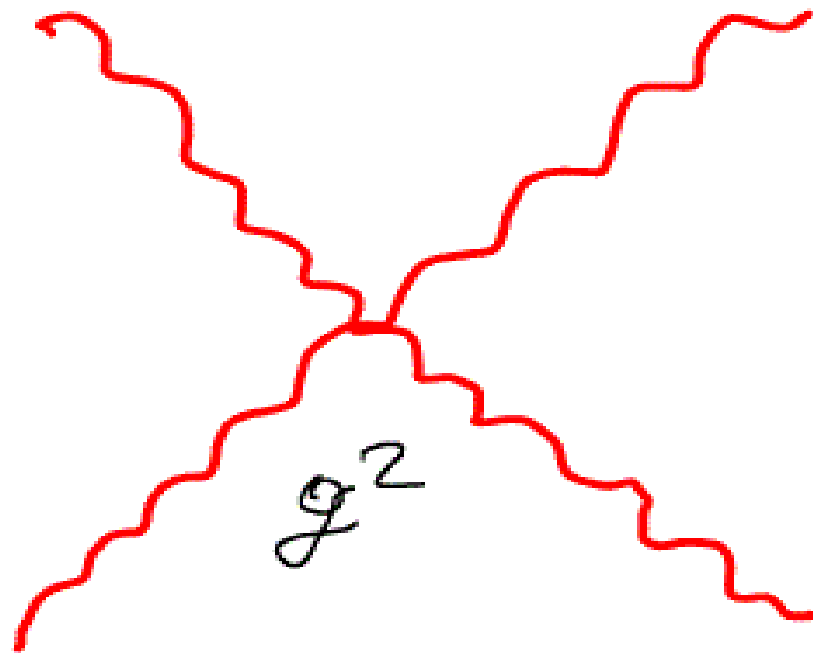
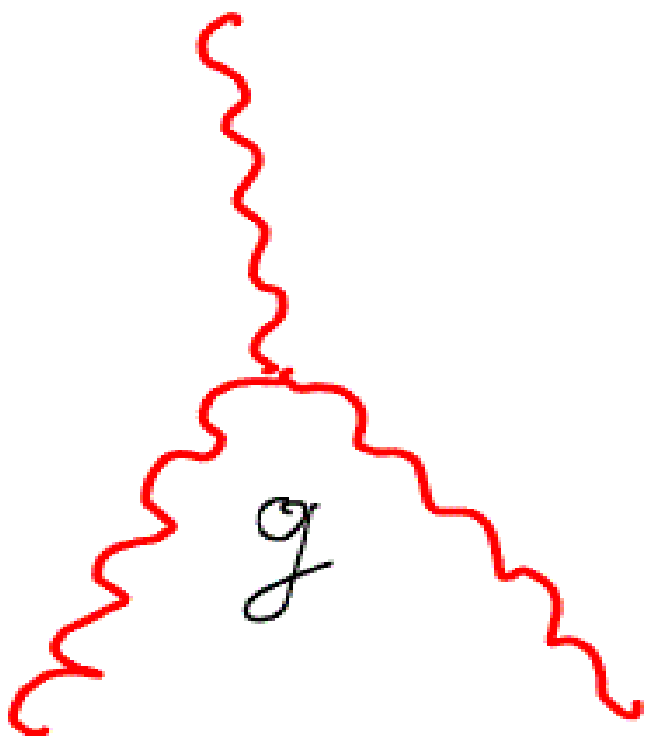
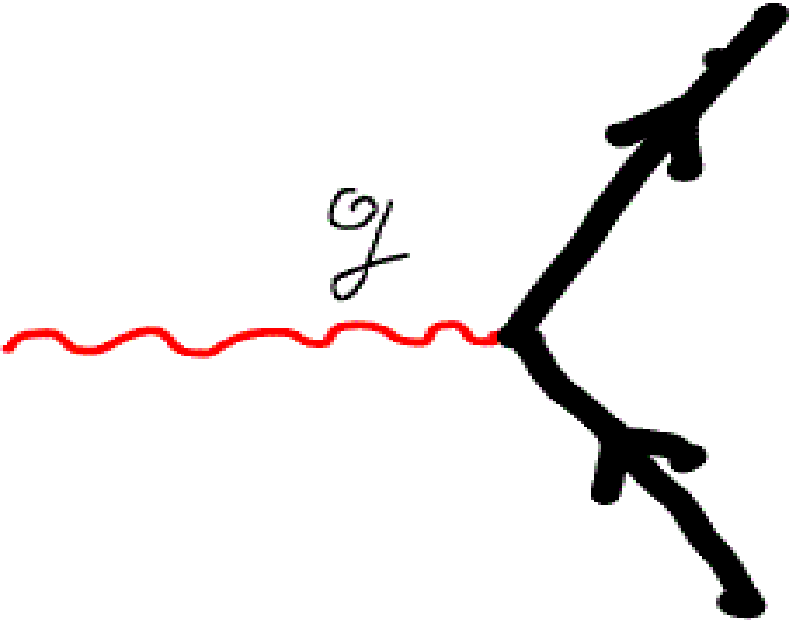


**universality  
of  
coupling constants**



**non-Abelian  
gauge invariance**

# gauge theory



**rho mesons**

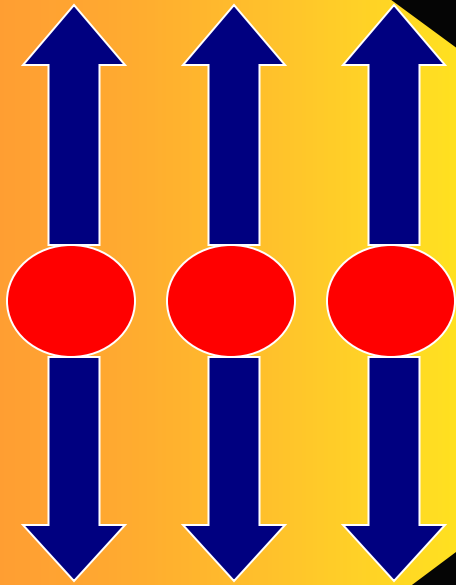


**elementary**

**gauge bosons**

# ~~“Higgs” - mechanism~~

“Higgs” - scalar

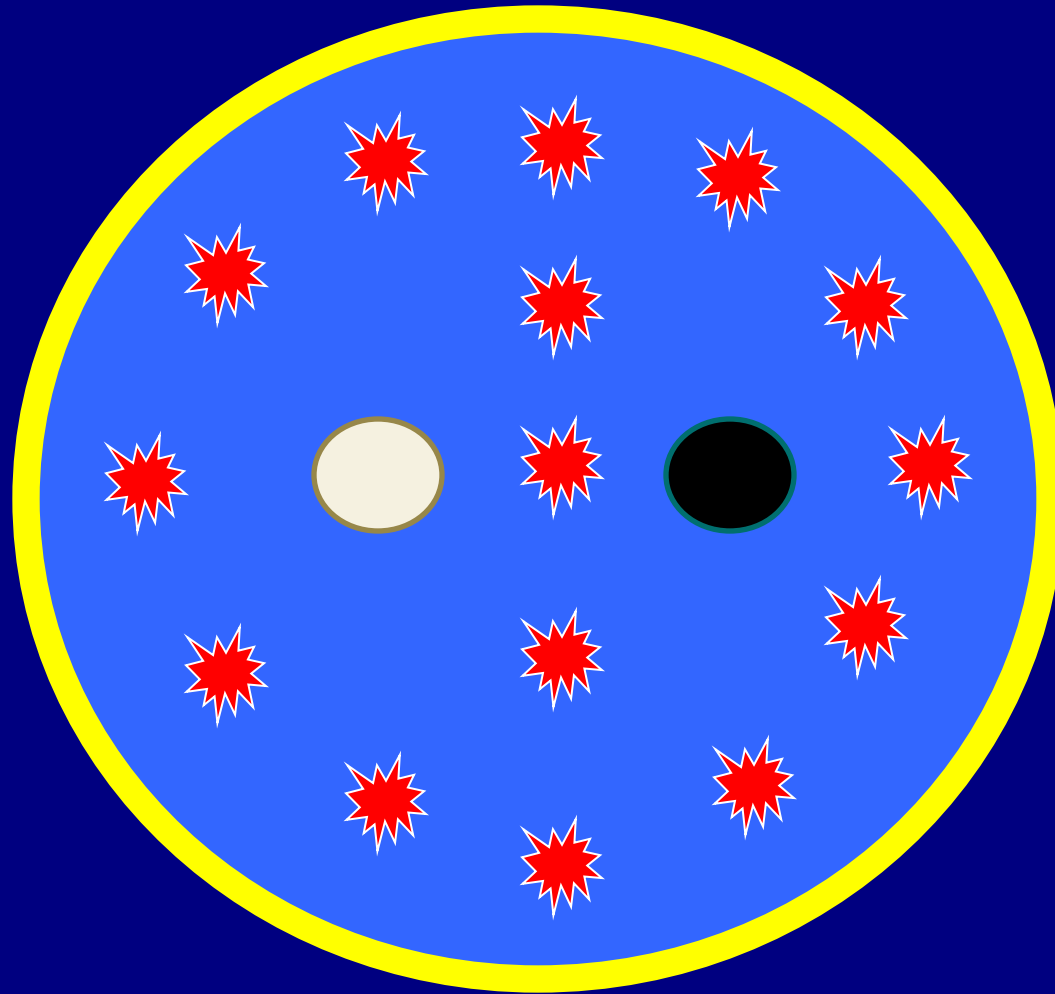


**mass M**

**massive**

**rho - mesons**

# $\rho$ - meson in QCD :



quark - antiquark - gluons 

$$\rho = (\bar{q}q)$$

$$M_\rho \approx 760 \text{ MeV}$$

$$= \text{const.} \cdot \Lambda_c$$

# QCD

1 GeV

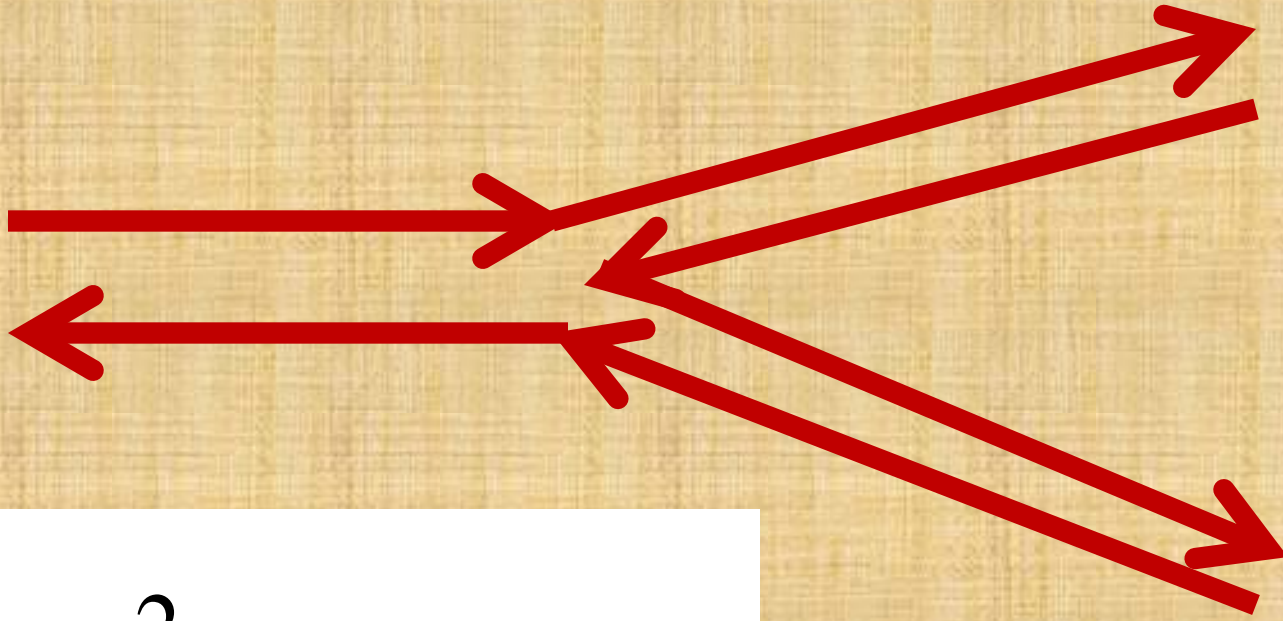


no „Higgs“ - scalar

**3 massive  
rho - mesons**

# UNIVERSALITY

$\rho$

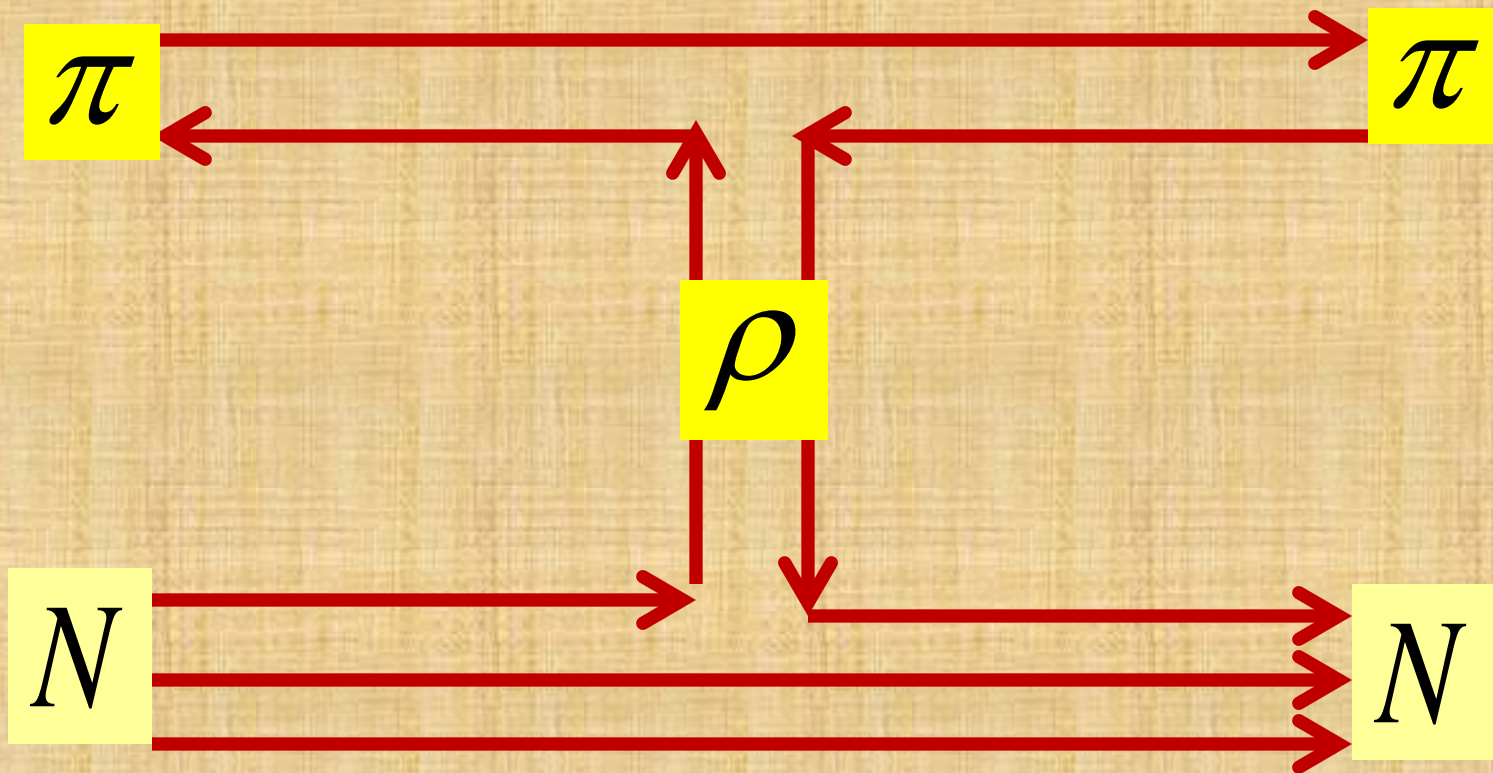


$\pi$

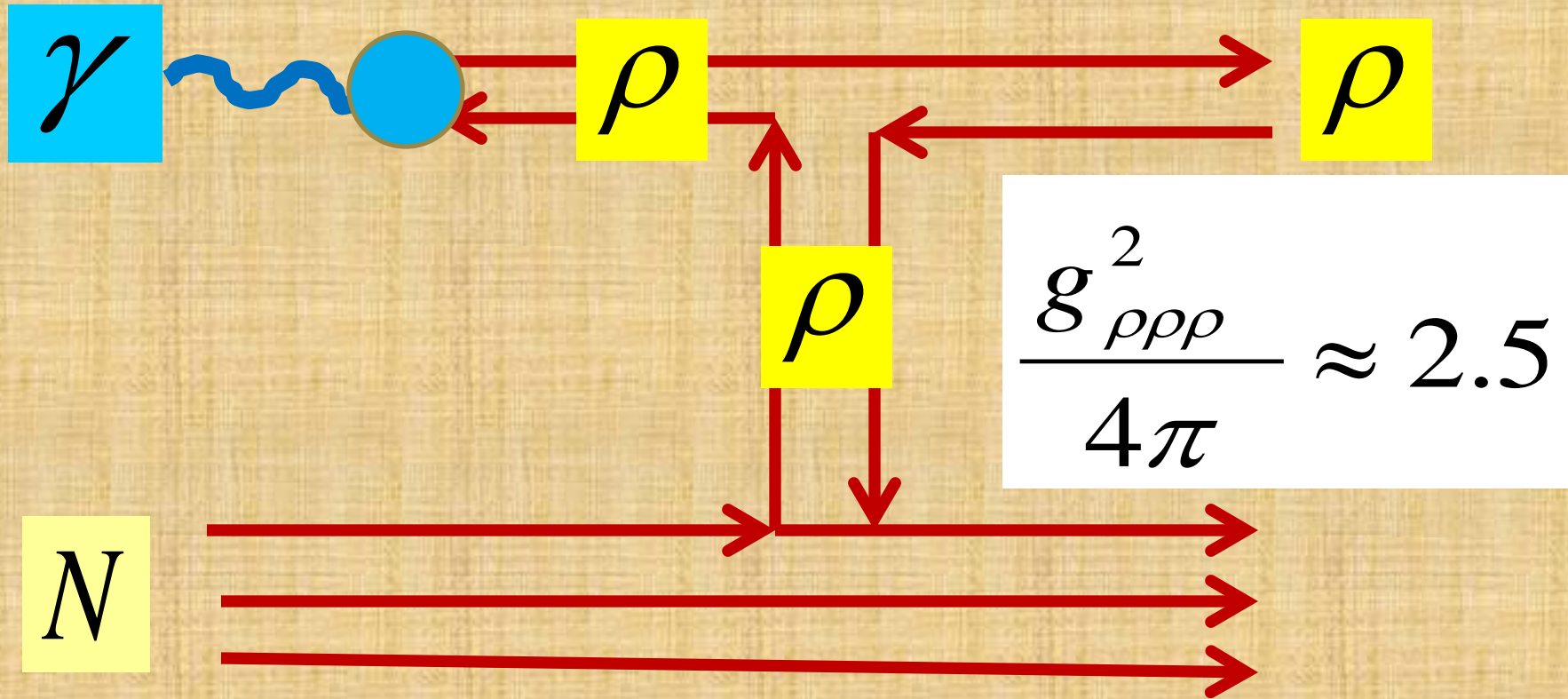
$\pi$

$$\frac{g_{\rho\pi\pi}^2}{4\pi} \approx 2.5$$



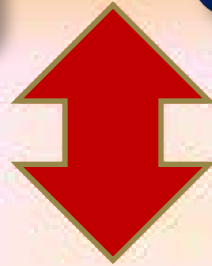


$$\frac{g_{\rho NN}^2}{4\pi} \approx 2.5$$



**universality**

**coupling constants**



**quarks**

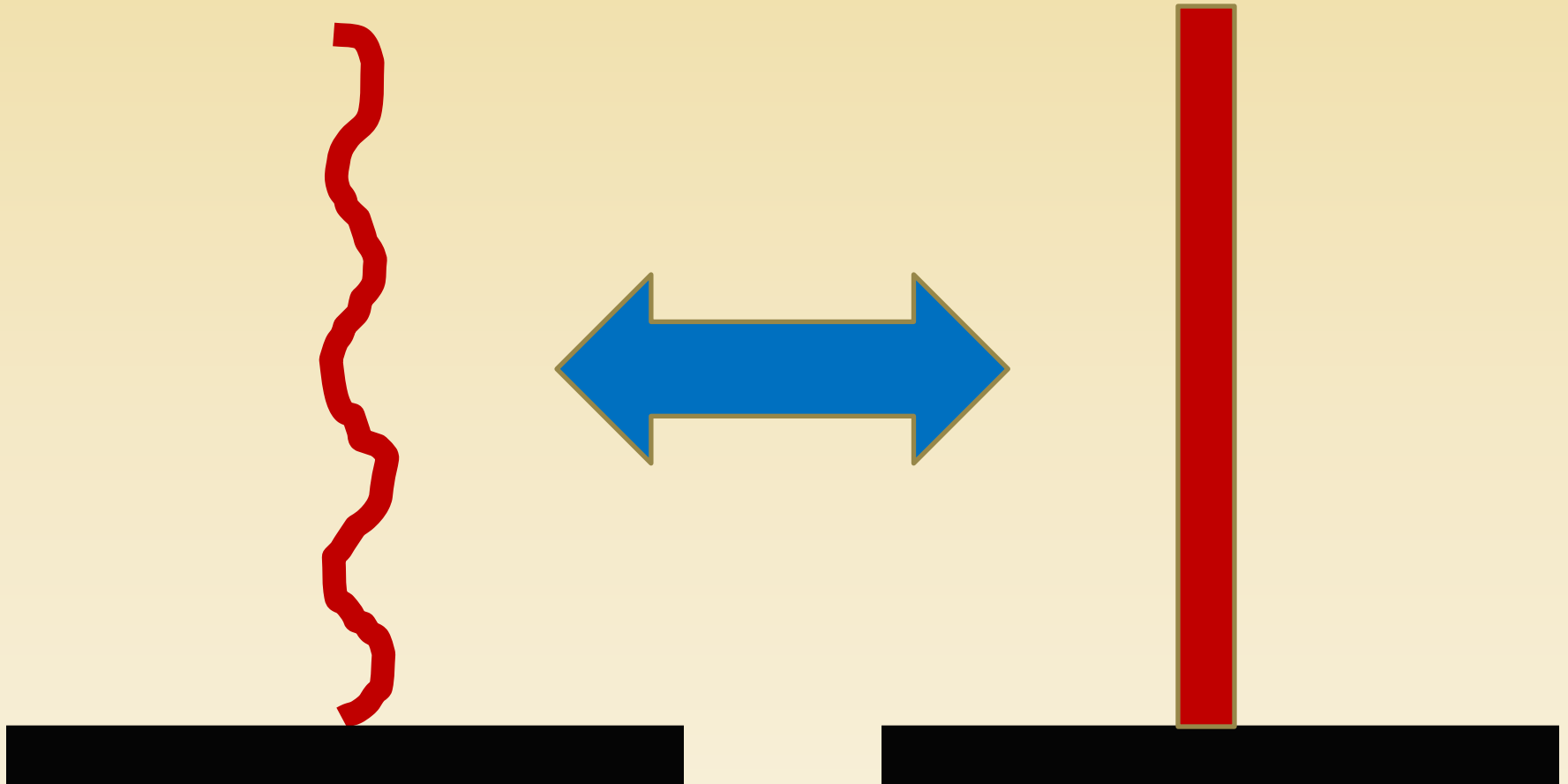
**duality diagrams**

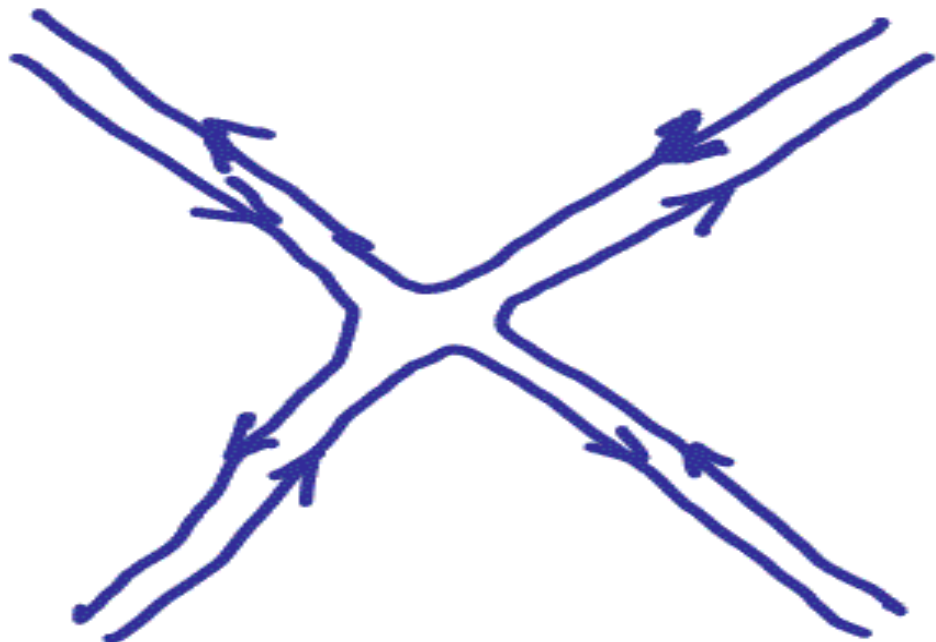
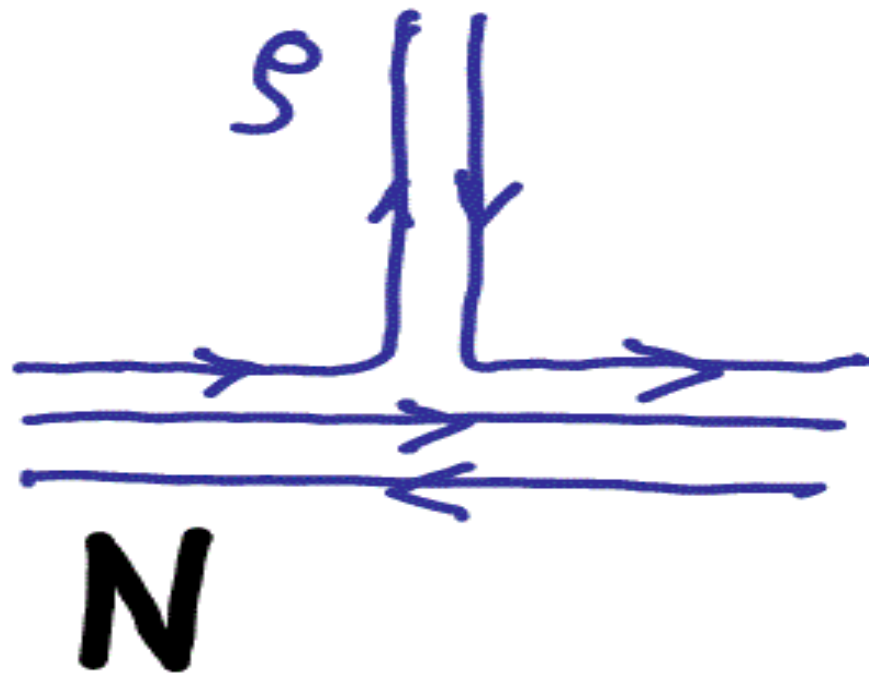
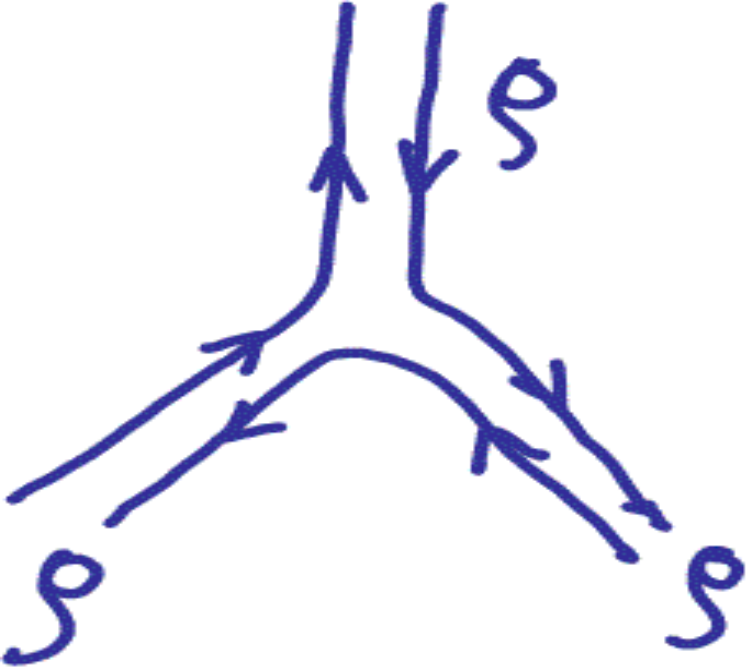
**current algebra**

**vector meson dominance**

current

rho - meson





**weak bosons**



**composite**



# old references:

Bjorken (1977)

Fritzsch and Mandelbaum (1981)

Abbott and Farhi (1981)

Barbieri and Mohapatra (1981)

Fritzsch, Kogerler and Schildknecht (1982)

Lüst (1985)

Calmet and Fritzsch (2000)

**new:**

*H. Fritzsch*

2010 - arXiv: 1010.1428

2011 - arXiv: 1105.3354

2012 - arXiv: 1203.5600



**masses of composite  
weak bosons ?**

**analogy**

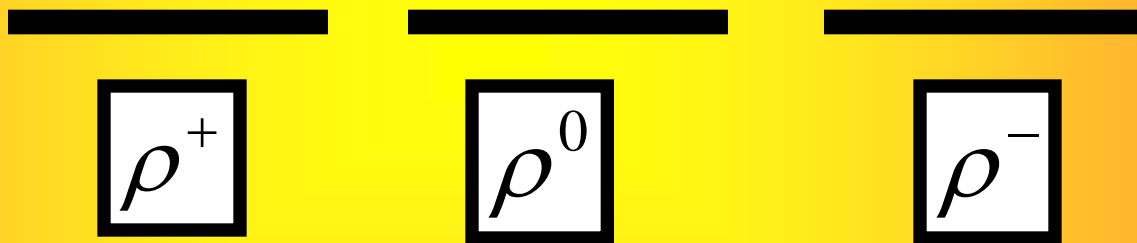
$$\rho^+ \Leftrightarrow W^+$$

$$\rho^0 \Leftrightarrow W^0$$

$$\rho^- \Leftrightarrow W^-$$

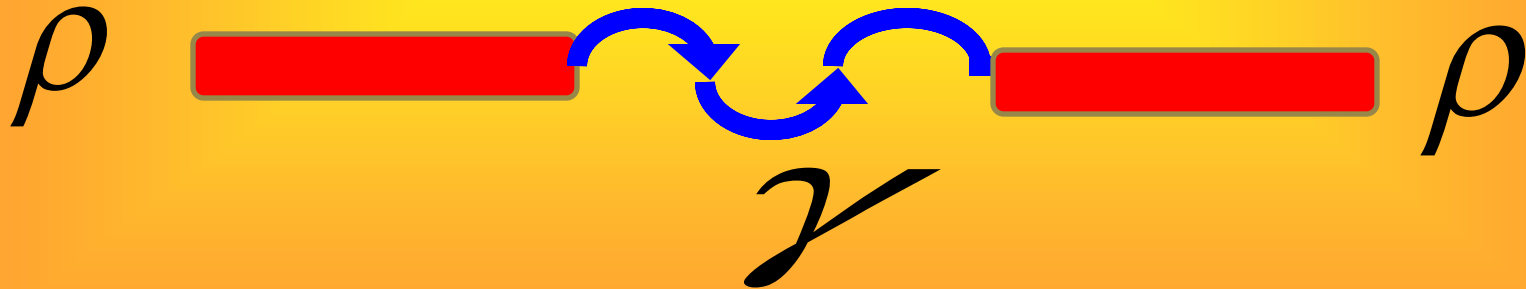
M

# QCD

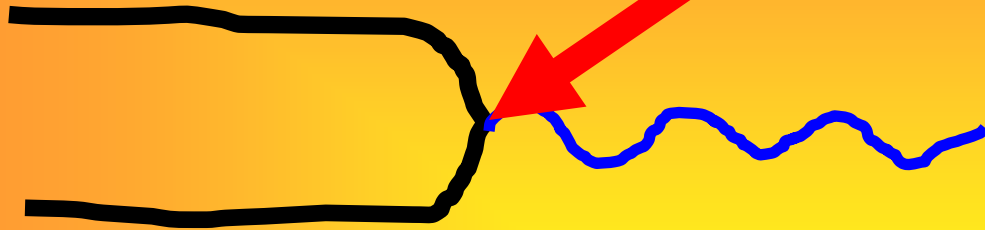


# QCD + QED

Dynamical mixing of rho meson and photon:



**mixing parameter  $m$**



$$m = e \frac{F_\rho}{M_\rho}$$

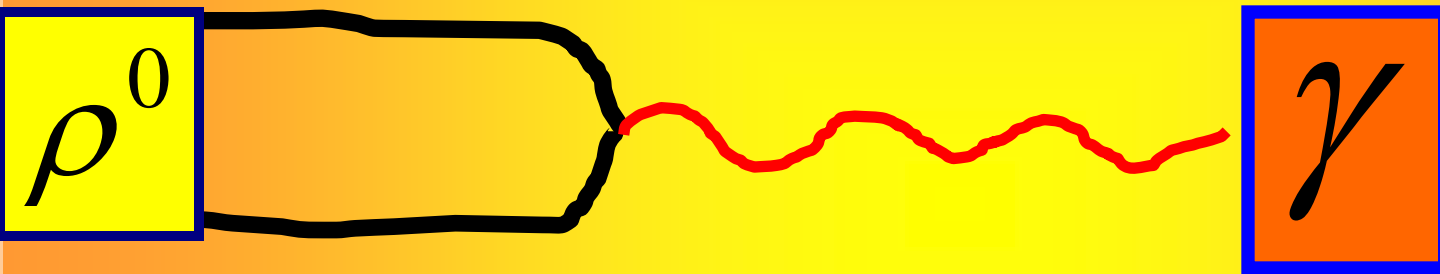
$$\langle 0 | \frac{1}{2} (\bar{u} \gamma_\mu u - \bar{d} \gamma_\mu d) | \rho_0 \rangle = \varepsilon_\mu M_\rho F_\rho$$

$F_\rho$  : decay constant

$$F_{\rho} \approx 220 \text{ MeV}$$

$$F_{\rho} \approx \Lambda_c$$

# mixing with photon



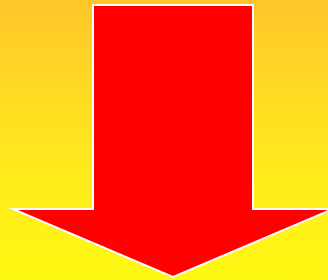
**m: mixing parameter**

$$M_{\rho^0}^2 = \frac{M_{\rho^+}^2}{1 - m^2}$$

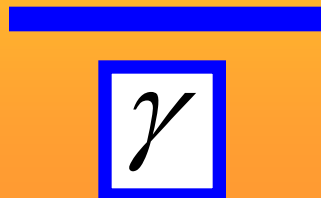
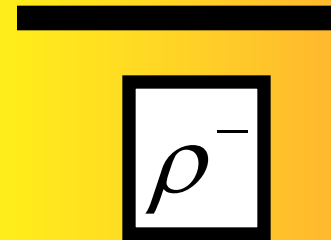
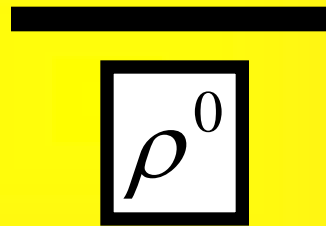
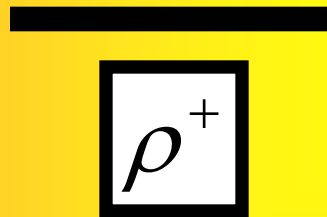
**$\sim 3.1$  MeV**

**$m = 0.09$**

# QCD + QED



mass shift:  
3.1 MeV



$Z$

$W^+$

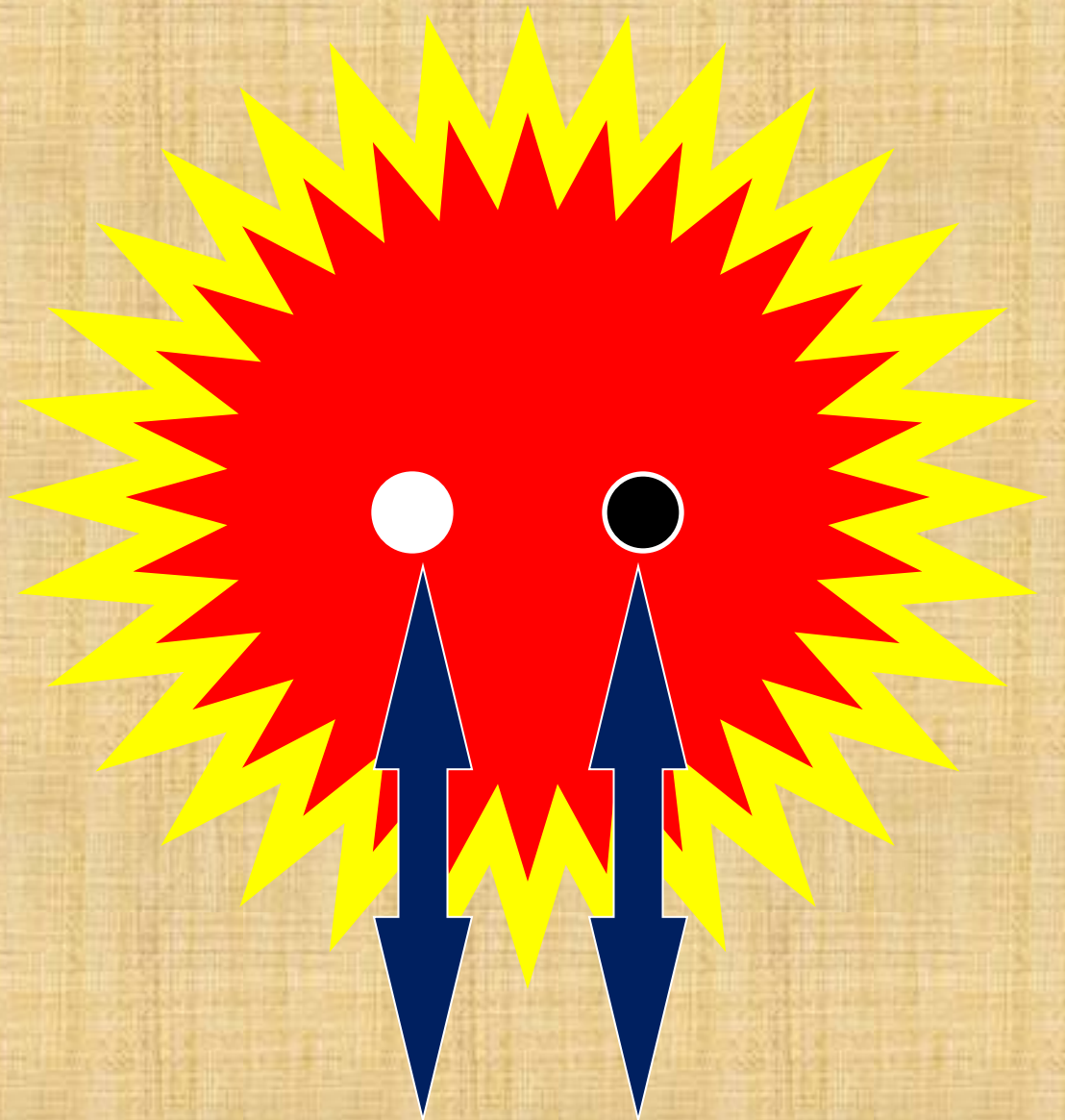
$W^-$

$\sim 10.4 \text{ GeV}$

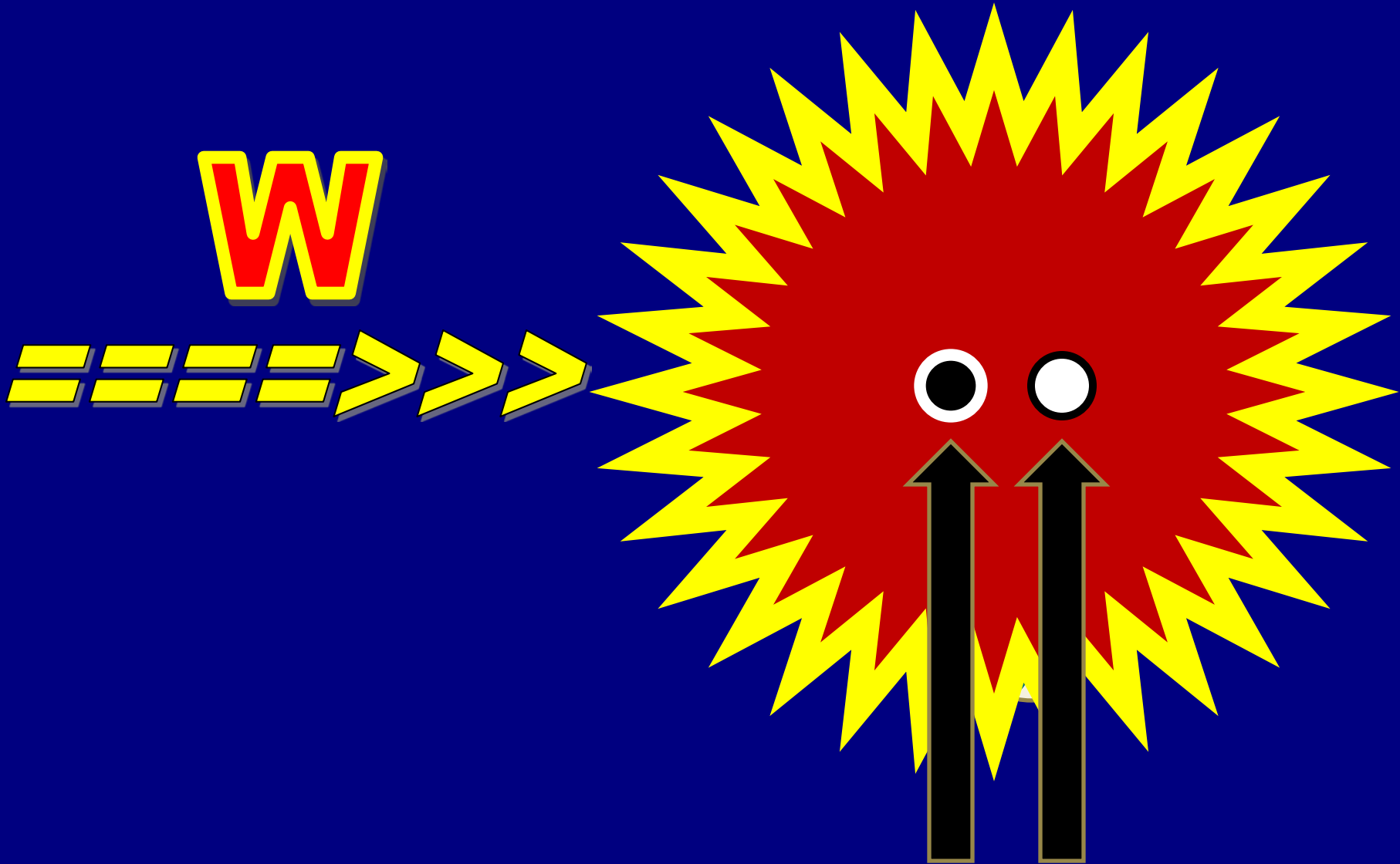
?

$\gamma$

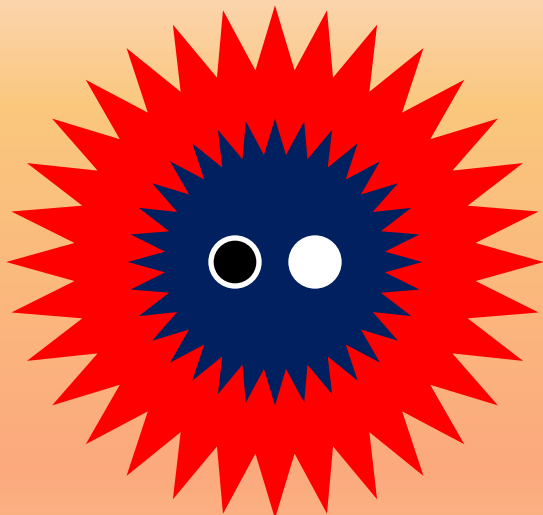




quarks

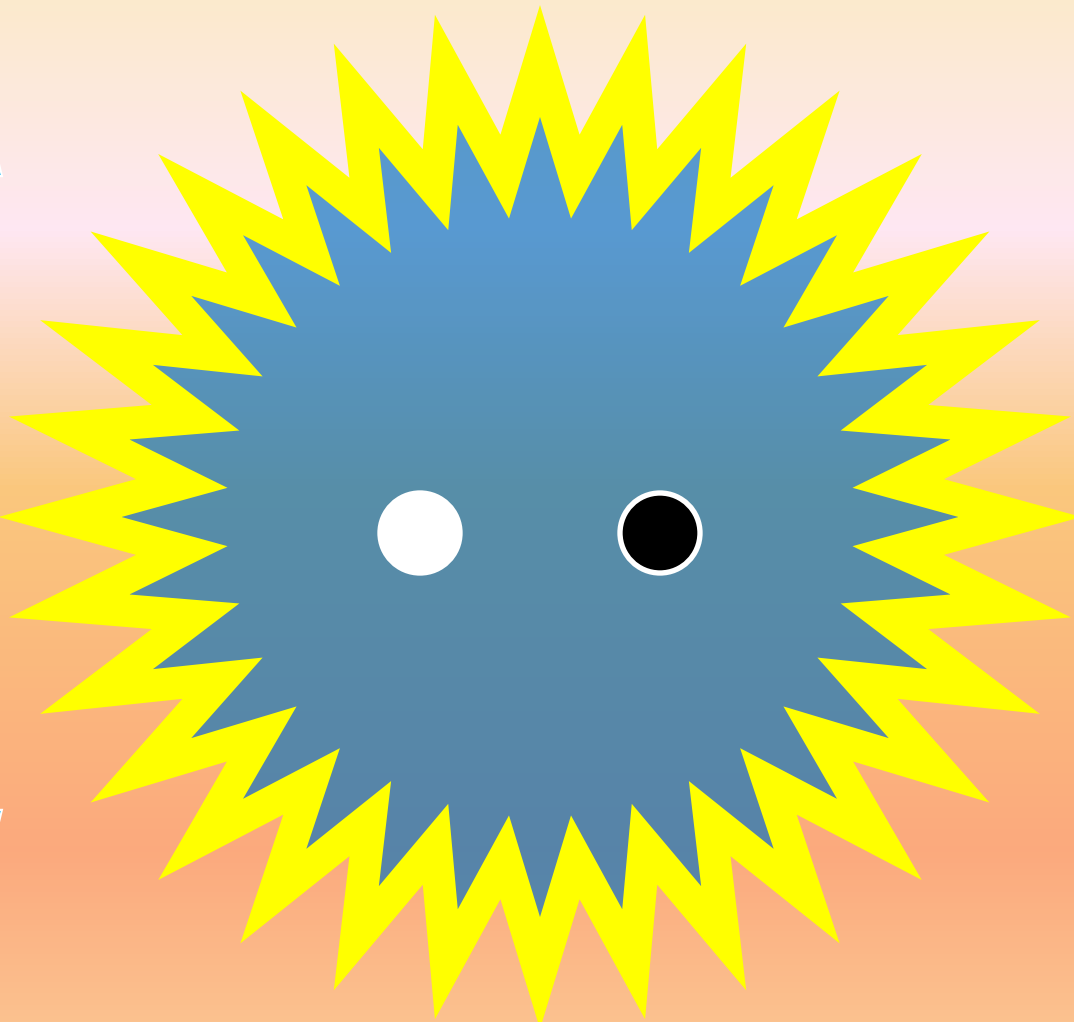


**constituents**



$W$

$\geq 1000$



$\rho$

# Constituents of W-bosons

$$\begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$

lefthanded fermions

$$\begin{pmatrix} \alpha \\ \beta \end{pmatrix}$$



*haplons*

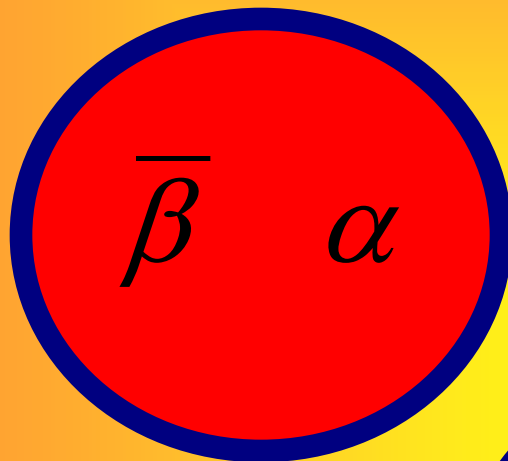
**haplos**  $\Leftrightarrow$  **simple**

# *electric charges*

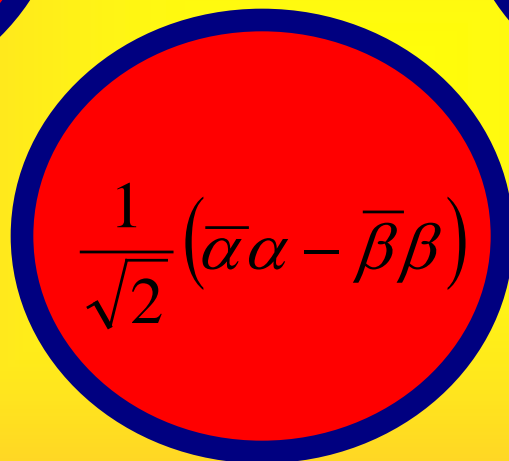
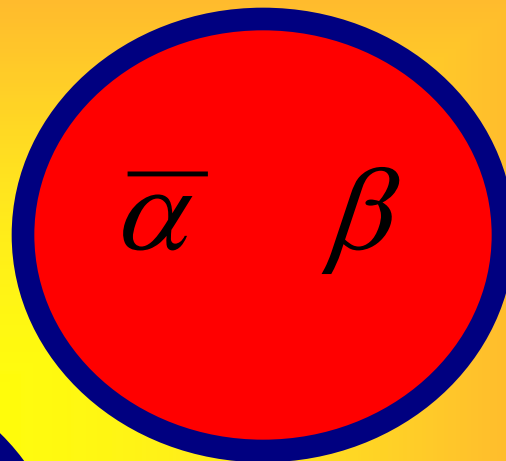
$$\alpha \Rightarrow +1/2$$

$$\beta \Rightarrow -1/2$$

$W^+$



$W^-$



$W^3$

haplons confined  
by gauge force

**QHD**

chiral gauge theory



glue → gluten

gauge bosons

**glutons**

Gauge group  
of QHD

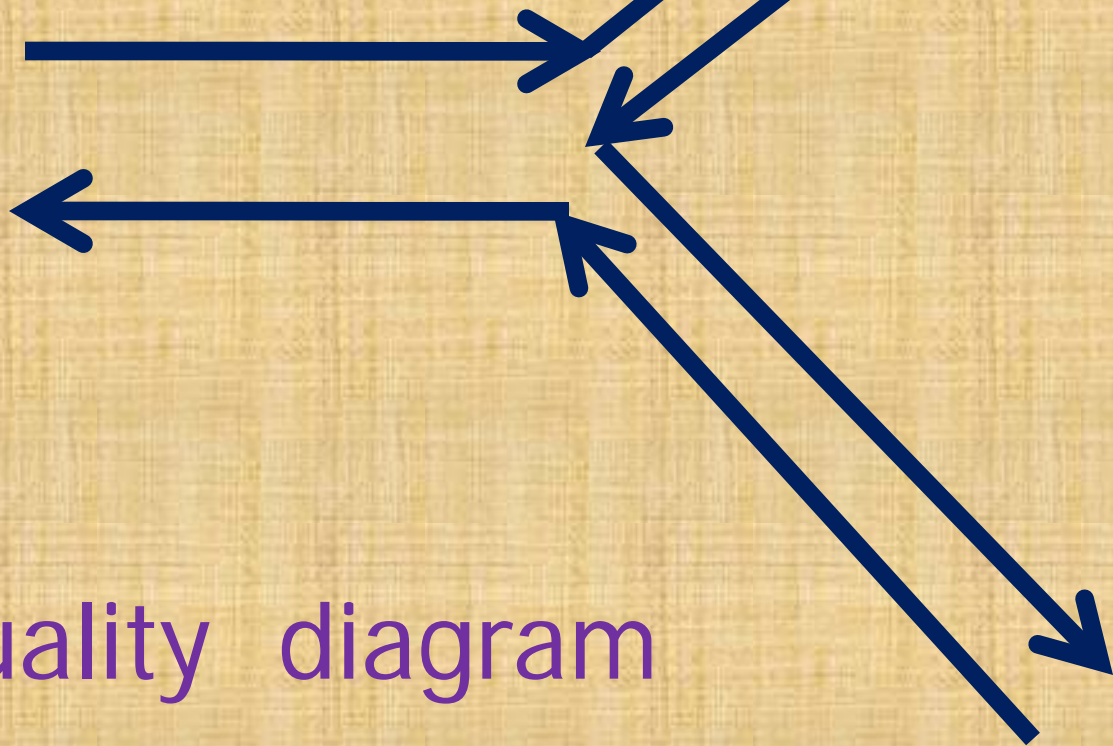
**SU(n)**

Gauge group  
of QHD:

? **SU(3)** ?

**QCD**

$\rho$

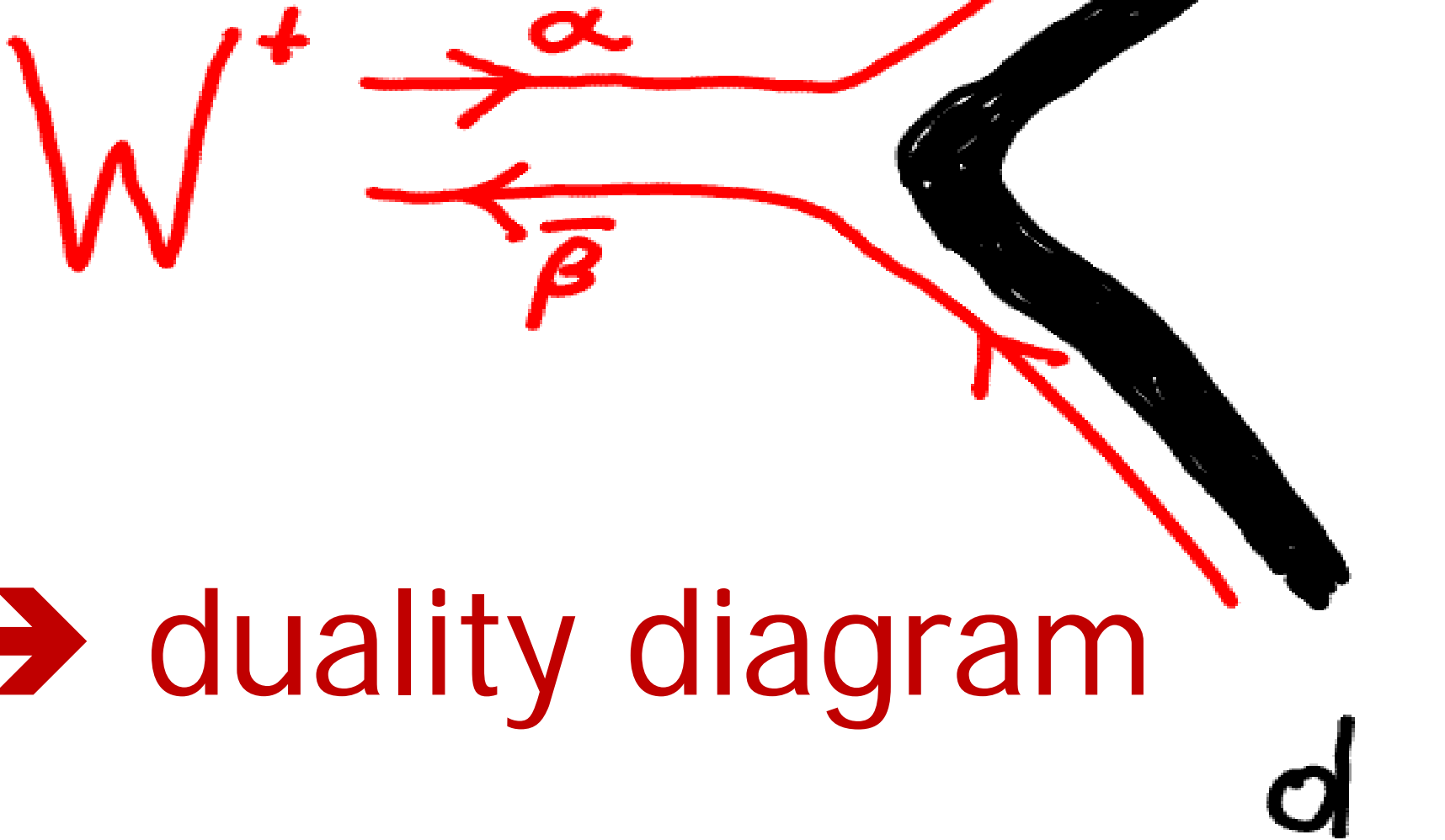


$\pi$

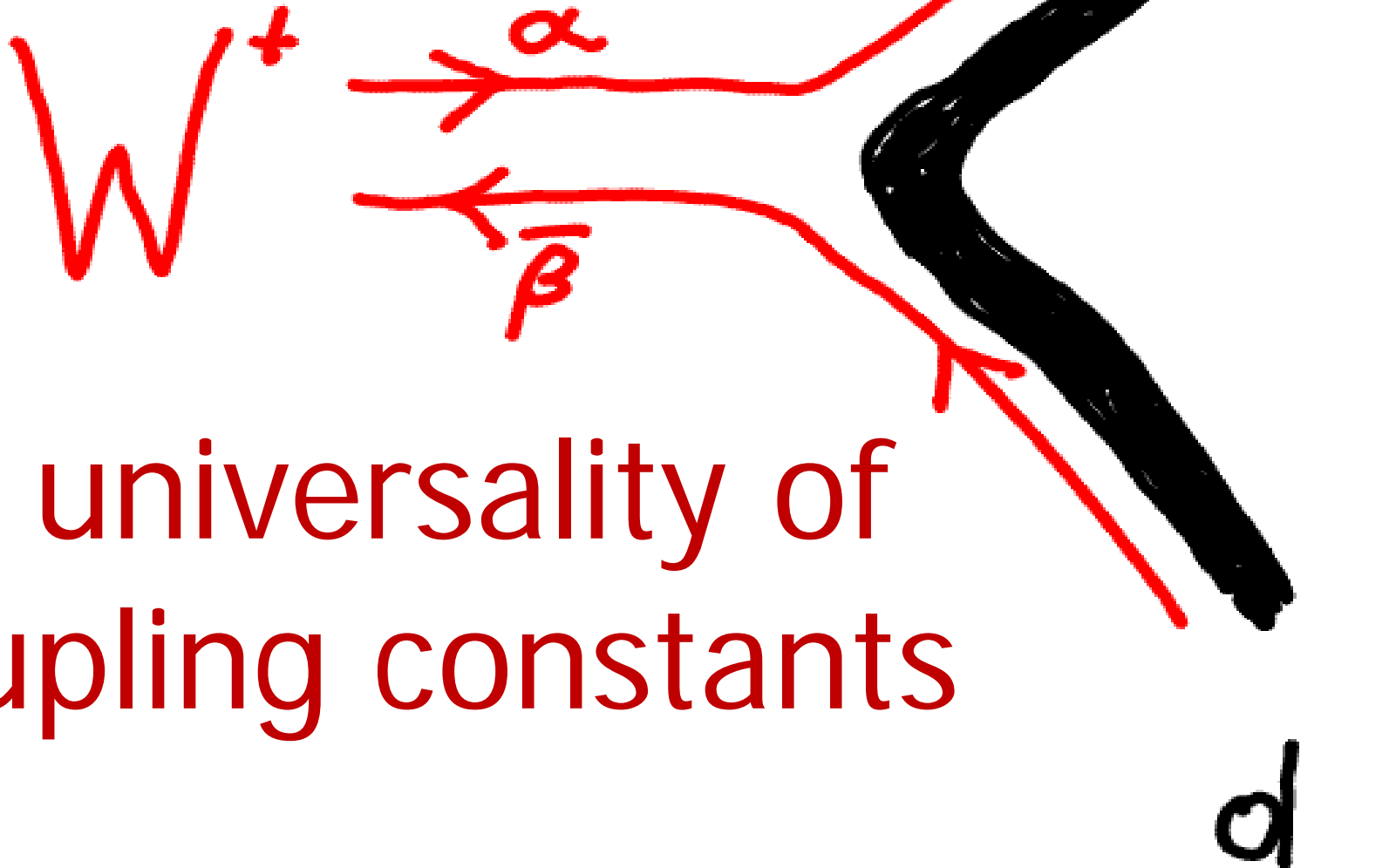
duality diagram

$\pi$

# QHD



# QHD



→ universality of  
coupling constants

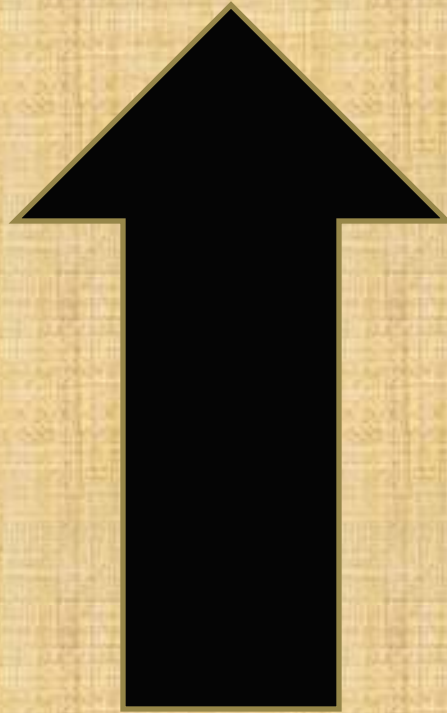
**maximal parity  
violation**

$$SU(2)_L \otimes U(1)$$



$$SU(2)_L \otimes SU(2)_R \otimes U(1)$$

$$SU(2)_L \otimes SU(2)_R \otimes U(1)$$

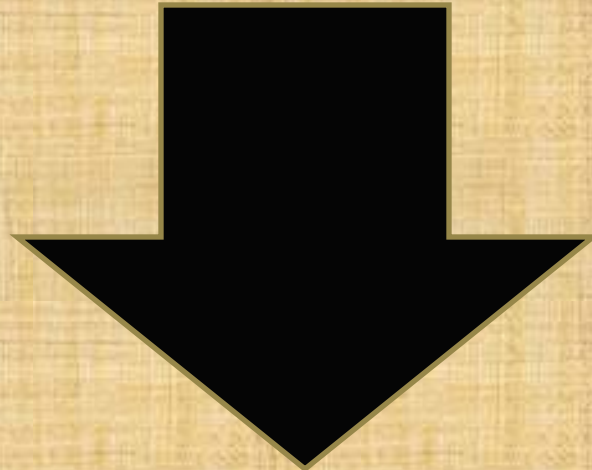


*mass of  $W_R$  :  $> 1 \text{ TeV}$*



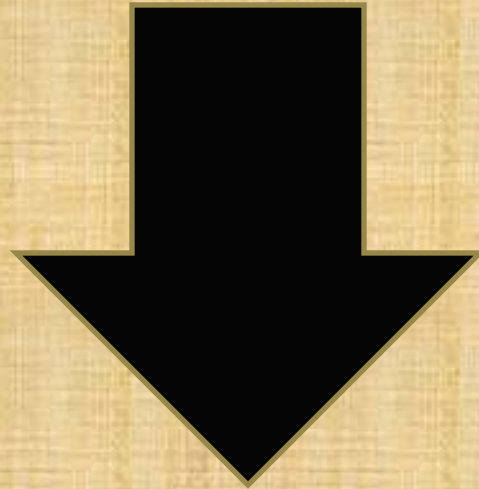
# Standard Model

$$SU(3)_c \otimes SU(2)_L \otimes U(1)$$




$$\left( SU(3)_c \otimes U(1) \right) \otimes SU(2)_L \otimes SU(2)_R$$

$$(SU(3)_c \otimes U(1)) \otimes SU(2)_L \otimes SU(2)_R$$



$$SU(4)_{c,l} \otimes SU(2)_L \otimes SU(2)_R$$

$$\begin{pmatrix} \nu & U_r & U_g & U_b \\ L & D_r & D_g & D_b \end{pmatrix}$$


$$SU(4)_{c,l} \simeq SU(3)_c \otimes U(1)$$

$$\begin{pmatrix} \nu & U_r & U_g & U_b \\ L & D_r & D_g & D_b \end{pmatrix}$$



4th color

**J. Pati – A. Salam**

$$SU(4)_{c,l} \otimes SU(2)_L \otimes SU(2)_R$$



$$\begin{pmatrix} \alpha \\ \beta \end{pmatrix}_L$$



$$\begin{pmatrix} \alpha \\ \beta \end{pmatrix}_R$$

gauge group  
of QHD

$$SU(n)_L \otimes SU(n)_R$$

mass scale

of

**QHD**



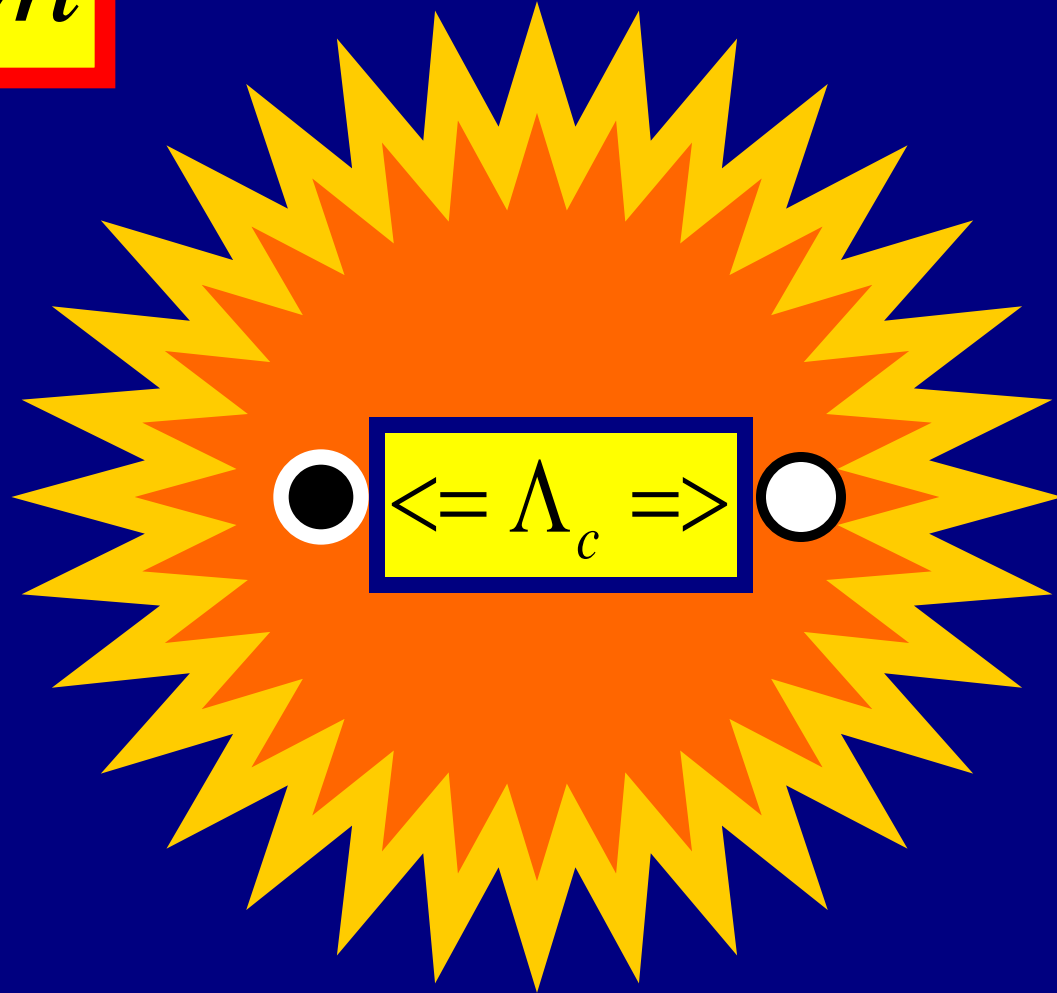
$$\left[ \Lambda_L * \Lambda_R \right]$$

$$\Lambda_L < \Lambda_R$$

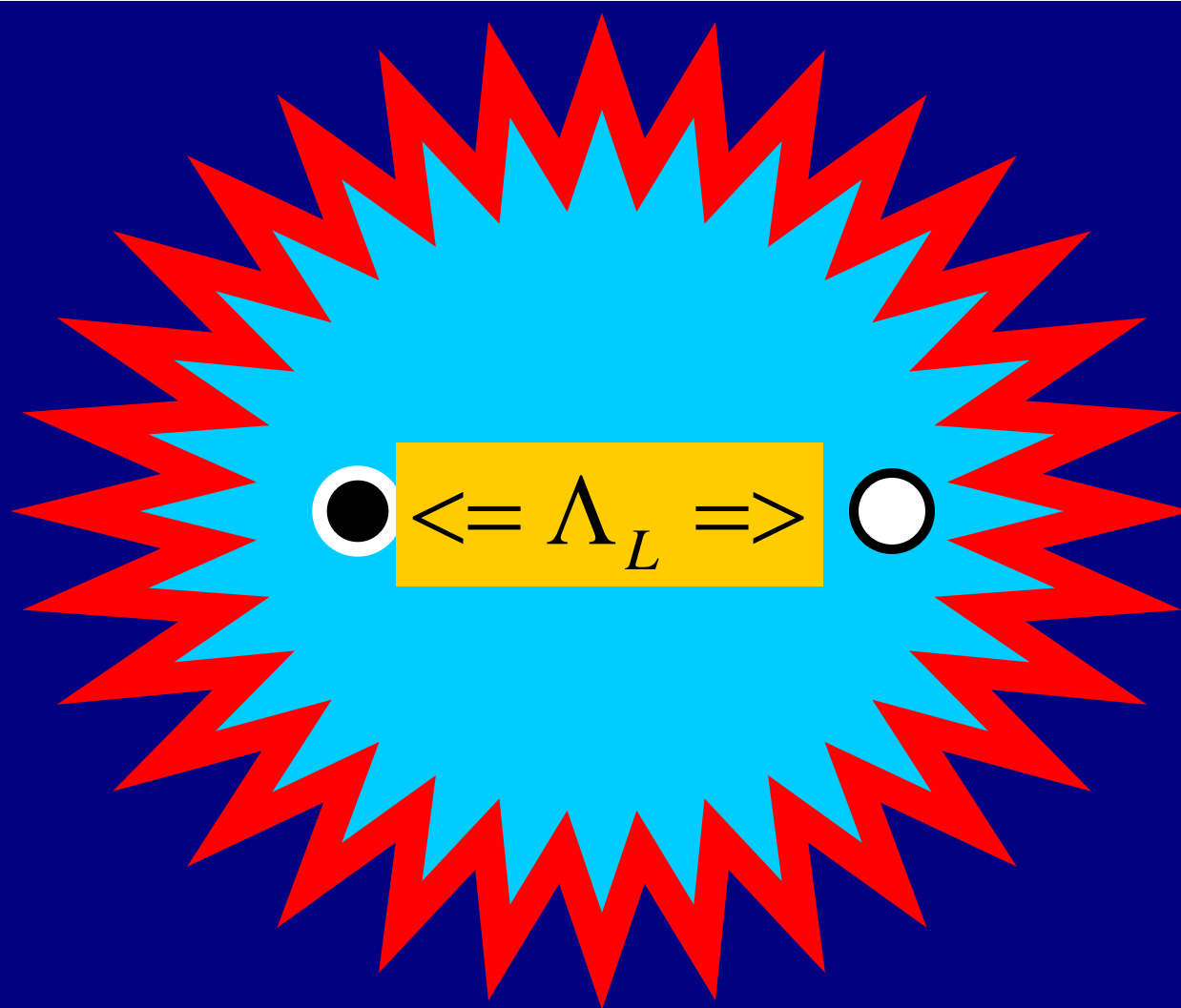
→ parity violation



$\rho$  – meson



$\Lambda_c : QCD - scale$

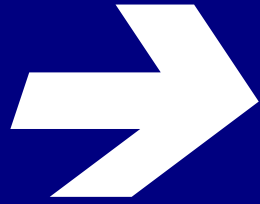


$W$  – *boson*

**Λ**

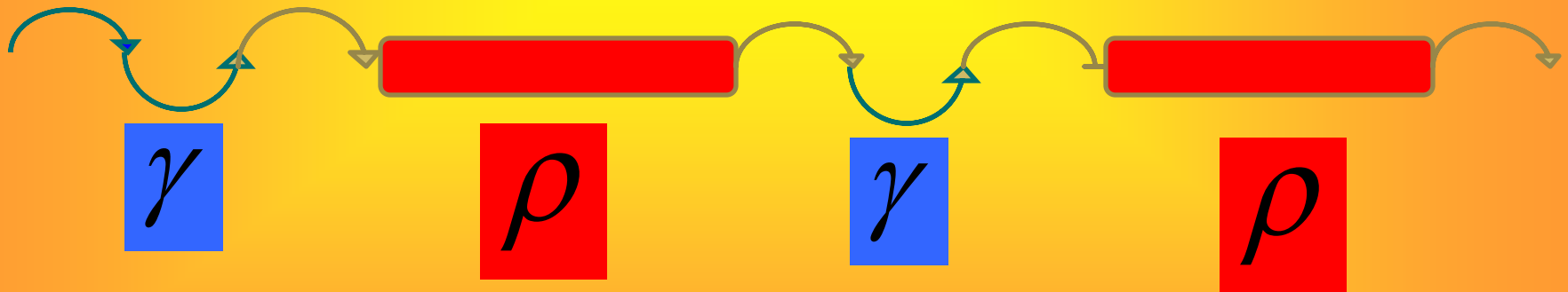
***L***

**?**

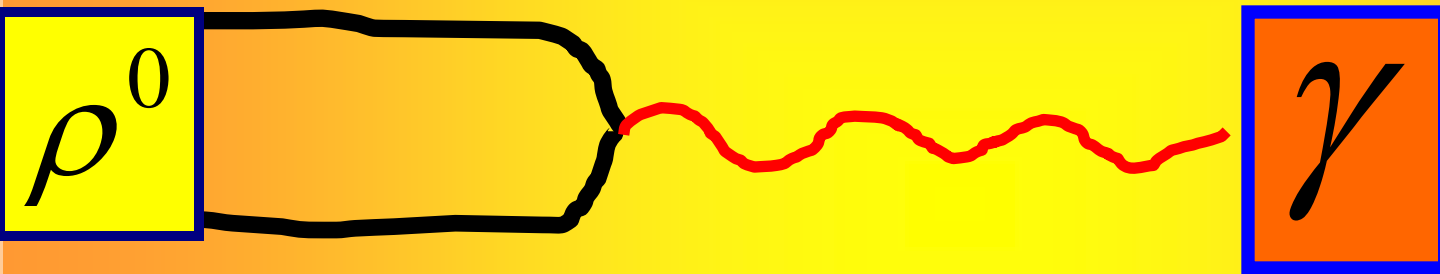


# *QCD*

Dynamical mixing of  
meson and photon



# mixing with photon

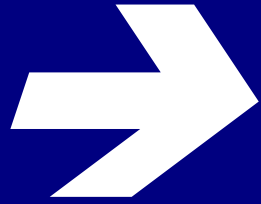


**m: mixing parameter**

$$M_{\rho^0}^2 = \frac{M_{\rho^+}^2}{1 - m^2}$$

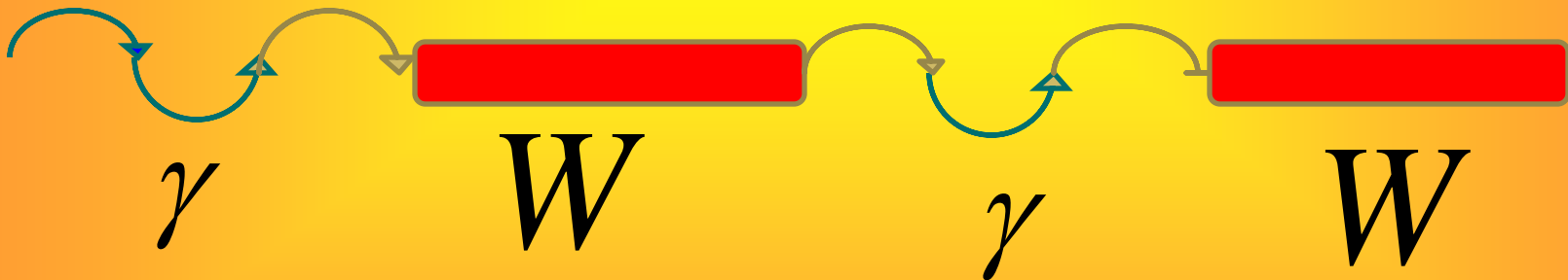
**$\sim 3.1$  MeV**

**$m = 0.09$**

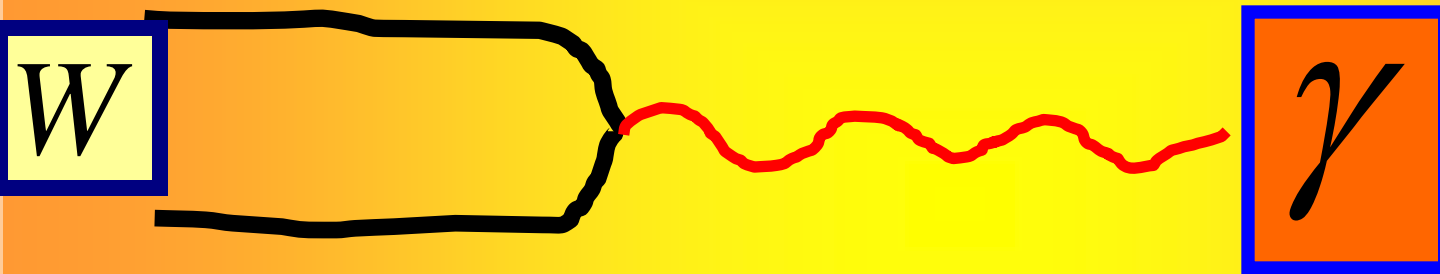


# *QHD*

Dynamical mixing of  
W-boson and photon



# mixing of W with photon



**m: mixing parameter**



$$M_Z^2 = \frac{M_W^2}{1 - m^2}$$

# Standard Model

$$M_Z^2 = \frac{M_W^2}{1 - \sin^2 \theta_w}$$



$$M_Z^2 = \frac{M_W^2}{1 - m^2}$$

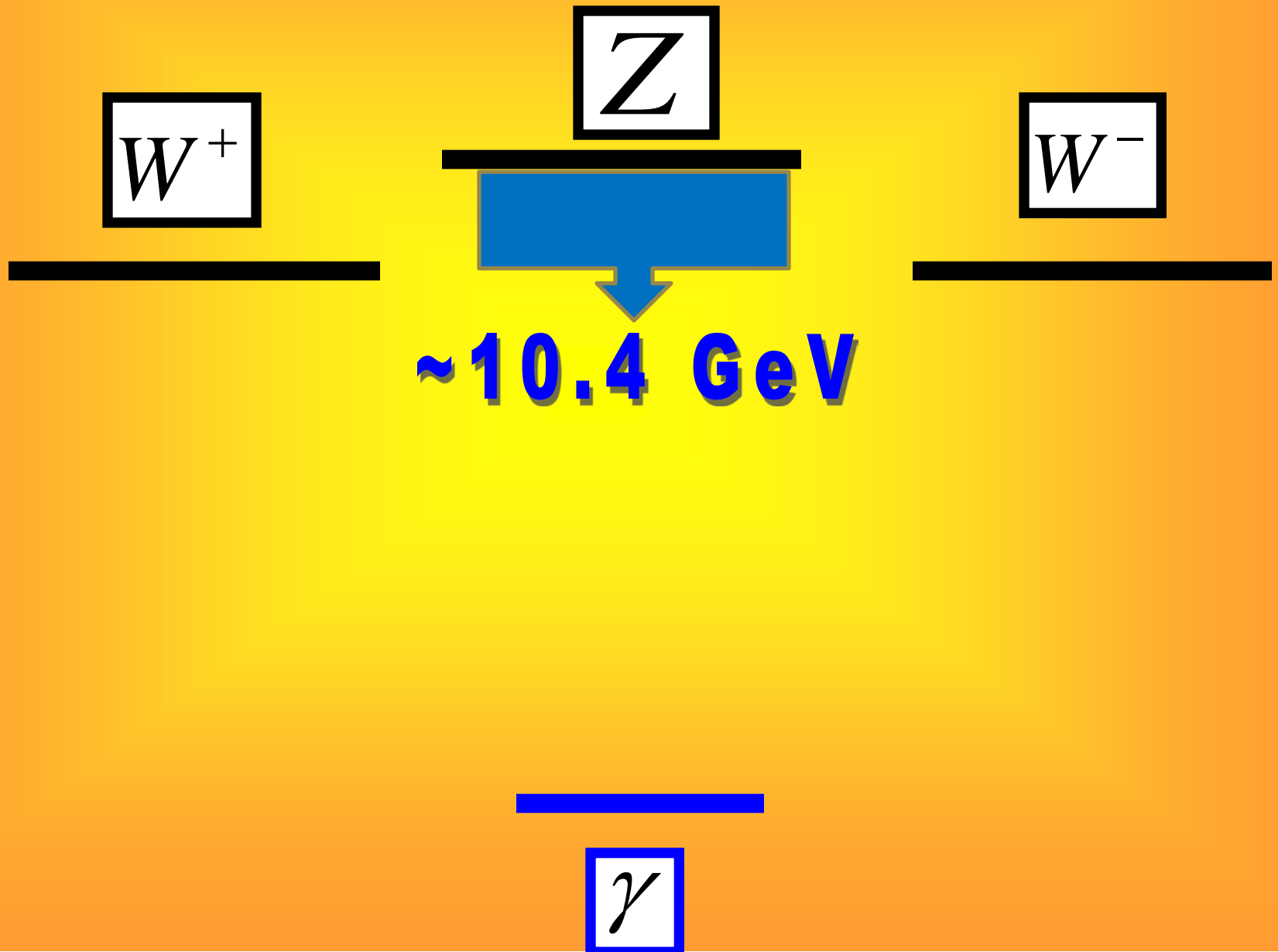
# Standard Model

$$M_Z^2 = \frac{M_W^2}{1 - \sin^2 \theta_w}$$

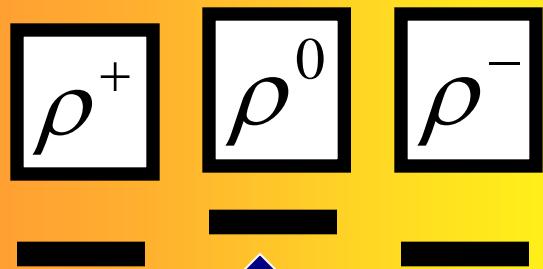


$$\sin \theta_w = m \approx 0.485$$

# Standard Model



# QCD + QED



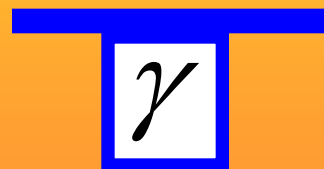
$\sim 3.1 \text{ MeV}$



# QHD + QED



$\sim 10.4 \text{ GeV}$



# W decay constant

$$\langle 0 | \frac{1}{2} (\bar{\alpha} \gamma_{\mu L} \alpha - \bar{\beta} \gamma_{\mu L} \beta) | Z \rangle = \varepsilon_{\mu} M_W F_W$$

$$m = e \frac{F_w}{M_w}$$

$$m \approx 0.485$$

$$\Rightarrow F_w \approx 125 \quad GeV$$

# experimental data:

$$M_W = 80.4...GeV$$

$$M_Z = 91.19...GeV$$

$$F_W = 124.6...GeV$$

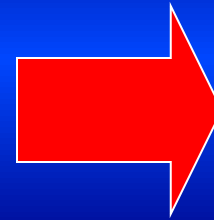
$$\sin^2 \theta_W = 0.2315$$

$$\alpha = \frac{e^2}{4\pi} \cong \frac{1}{128.9}$$

$$e \cong 0.3122$$

$$F_{\rho} \approx \Lambda_c \approx 220 \text{ MeV}$$

$$F_w \approx 0.125 \text{ TeV}$$



$$\Lambda_L$$



$$F_W \approx 0.130 \text{ TeV}$$

$$\Lambda_L \approx 0.13 \Leftrightarrow 1.0 \text{ TeV}$$

**uncertainty:**  
**gauge group of**  
**QHD**



$$F_W \approx 0.125 \text{ TeV}$$



$$0.12 \prec \Lambda_L \prec 1.0 \text{ TeV}$$

??? QHD gauge group ???

$$SU(n) \Rightarrow SU(3)$$



$$F_w \approx 0.13 \quad TeV$$

$$\Lambda_{h,L} \approx 0.13 \quad TeV$$

$$0.12 \lesssim \Lambda_{h,L} \lesssim 1.0 \text{ TeV}$$

$$\Lambda_{h,R} \gg \gg 1 \text{ TeV}$$

# **NEW BOSONS**

New:  
isoscalar

$$\frac{1}{\sqrt{2}}(\bar{\alpha}\alpha - \bar{\beta}\beta)$$

**Z**

$$\frac{1}{\sqrt{2}}(\bar{\alpha}\alpha + \bar{\beta}\beta)$$

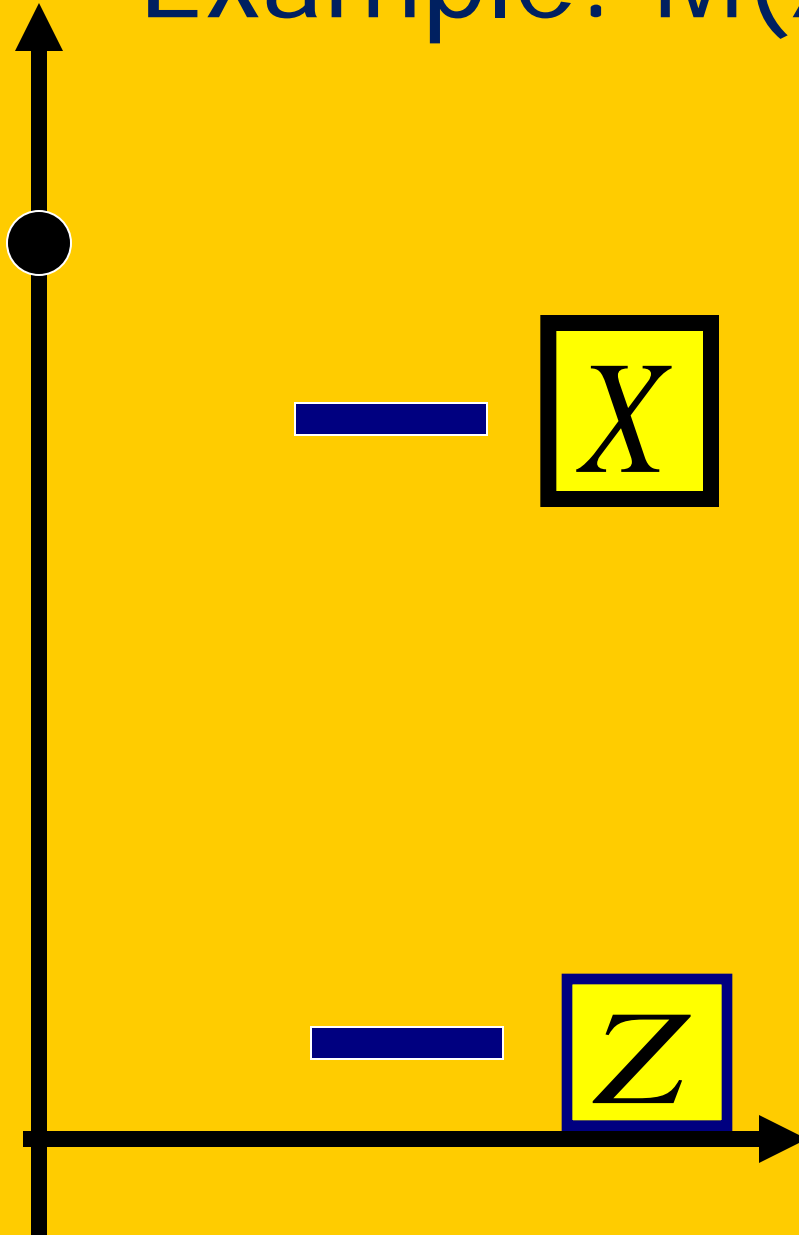
**X**

Present lower limit  
on X-mass:

$\sim 400 \text{ GeV}$

Example:  $M(X) = 0.8 \text{ TeV}$

1 TeV



Coupling of  $X$  to  
leptons and quarks:

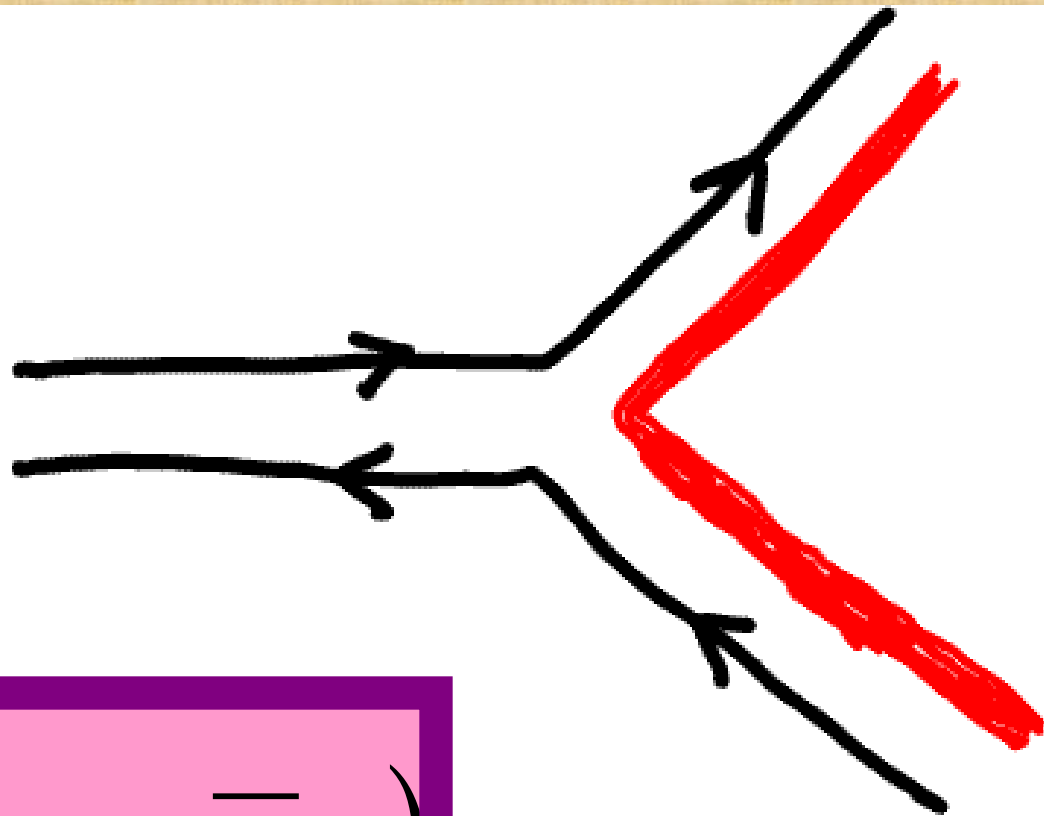
→ coupling of  $Z$  - boson



Z



X

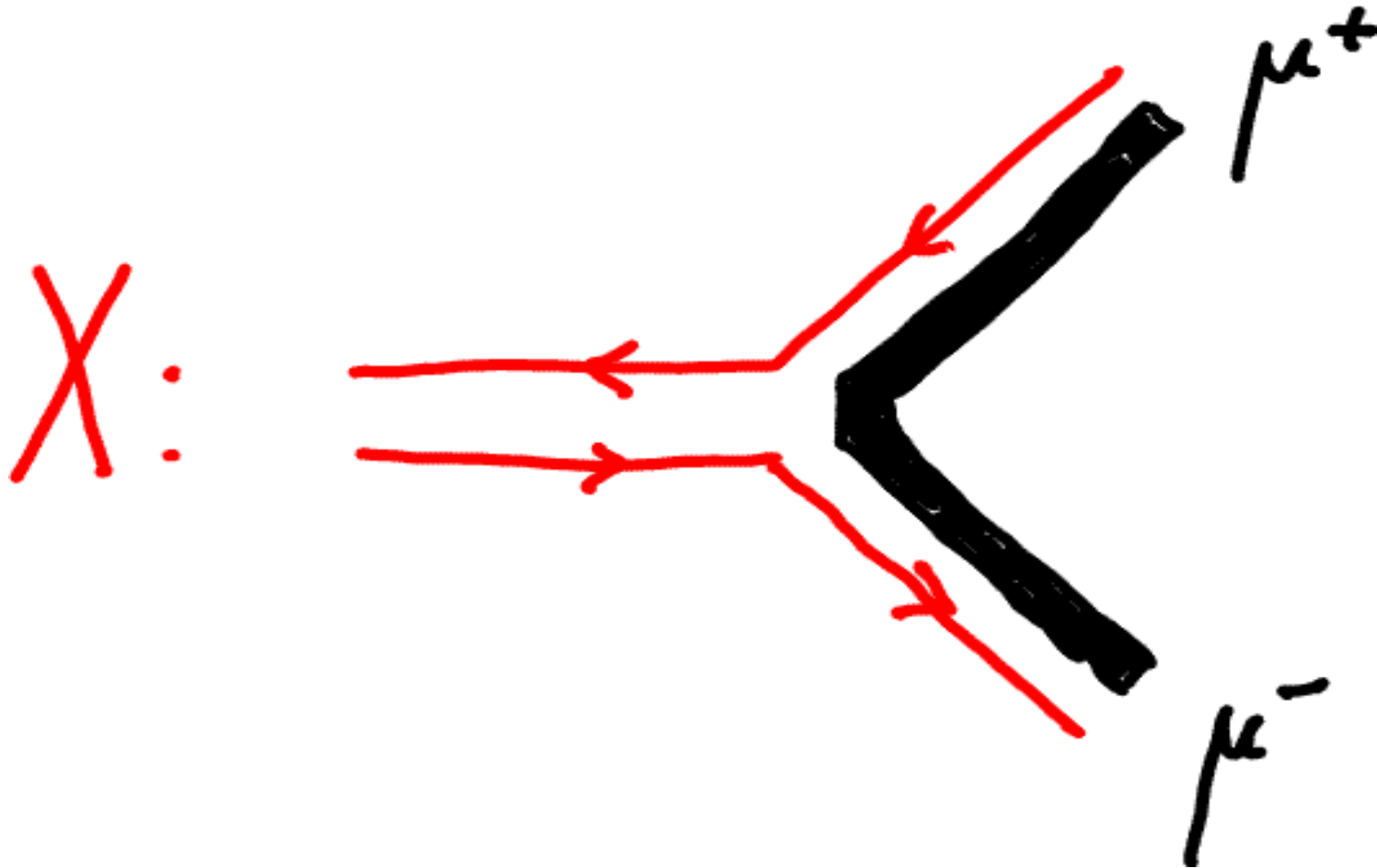


$$\frac{1}{\sqrt{2}} (\bar{\alpha} \alpha \pm \bar{\beta} \beta)$$

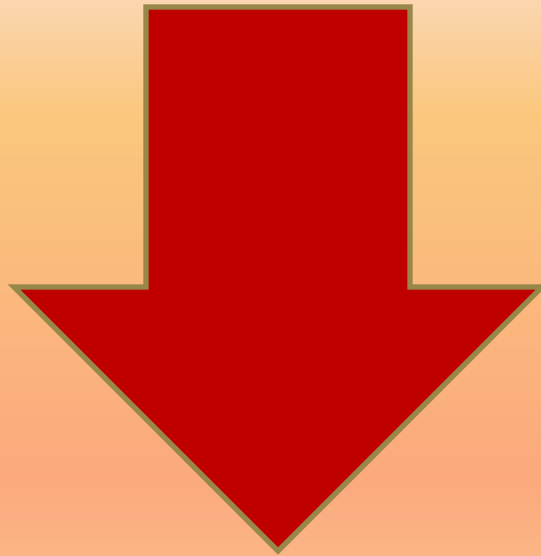
p, q

X – decay into muons

→ Z – decay into muons:



$$\Gamma(Z \Rightarrow \mu^+ \mu^-) \cong 84 \text{ MeV}$$

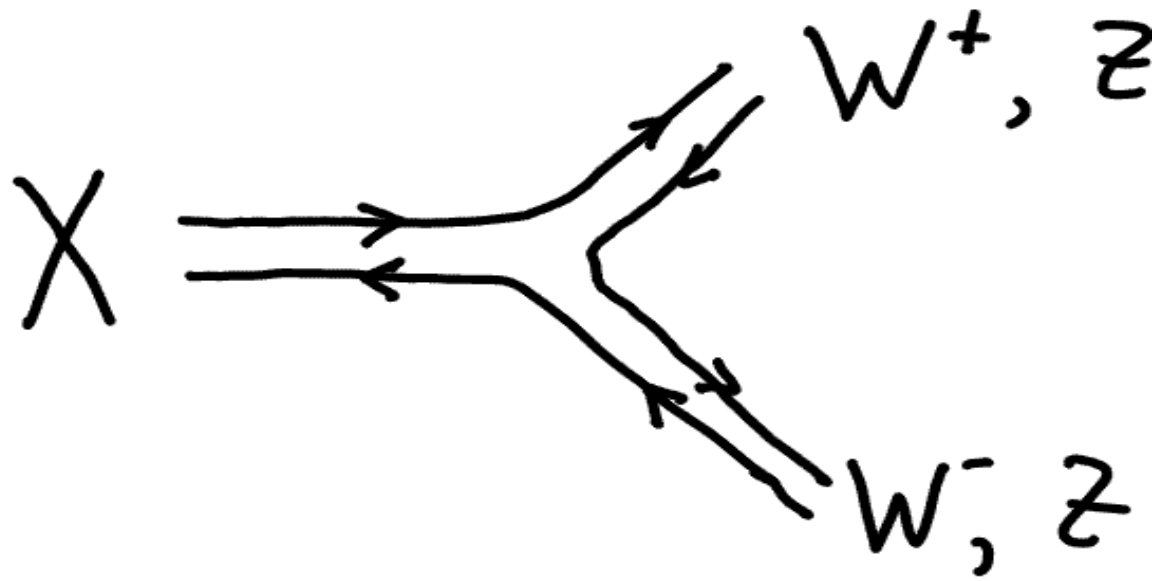


$$\Gamma(X \Rightarrow \mu^+ \mu^-) \cong 3.6 \text{ GeV}$$

$\chi$ -decays  $\rightarrow$  leptons  
quarks

$$\begin{aligned}\Gamma(\chi \rightarrow \mu^+ \mu^-) &\cong \Gamma(\chi \rightarrow e^+ e^-) \\ &\cong \Gamma(\chi \rightarrow \bar{\nu}_e \nu_e)\end{aligned}$$

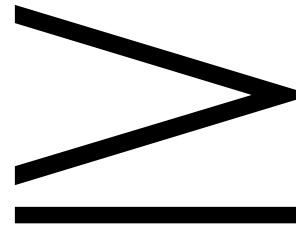
$$\begin{aligned}\Gamma(\chi \rightarrow \bar{u} u) &\cong \Gamma(\chi \rightarrow \bar{d} d) \\ &\cong 3 \times \Gamma(\chi \rightarrow \mu^+ \mu^-)\end{aligned}$$



Expected:

$$\Gamma(X \rightarrow W^+W^-)$$

$$\Gamma(X \rightarrow ZZ)$$



$$\Gamma(X \rightarrow \mu^+\mu^-)$$

# Summation

Total width of X:

 200 GeV

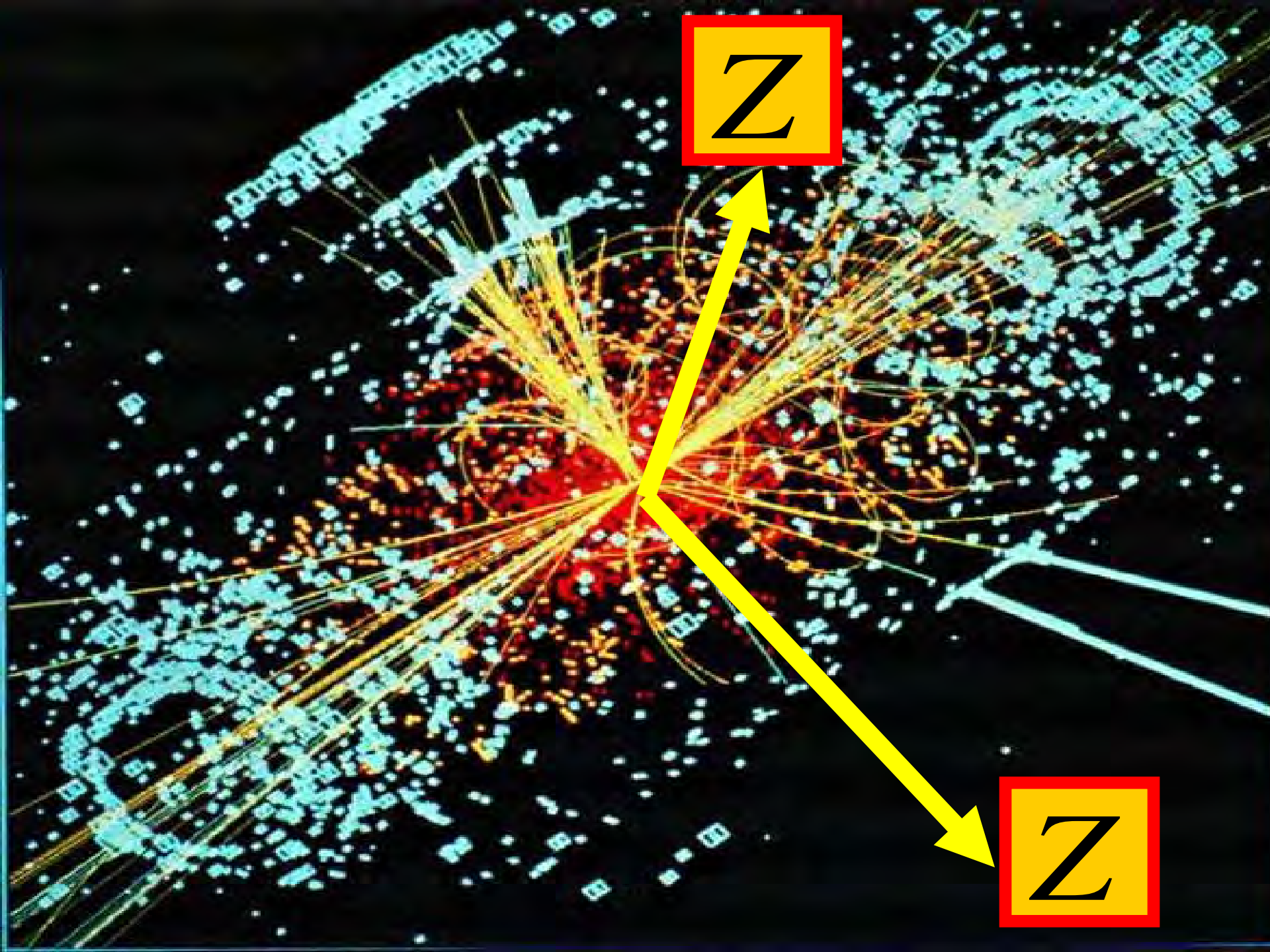
Total width of Z:

2.5 GeV

# Discovery of X- boson:

search for decay  
into weak bosons

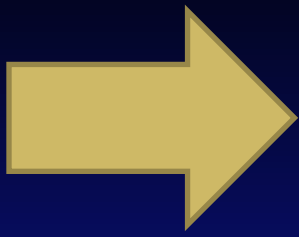
$$X \Rightarrow Z + Z$$





$$\Lambda_c \approx 0.3 \dots \text{GeV}$$

complexities  
of  
strong interactions  
 $\sim 1 \text{ GeV}$



$$\Lambda_h \propto 0.3 \text{ TeV}$$
$$= 1000 \cdot \Lambda_c$$

complexities  
of  
QHD interactions  
 $\sim 1 \text{ TeV}$

# EXCITED WEAK BOSONS

$I(J)$

$I : SU(2)$

$J : \textit{angular momentum}$

# p-wave bosons

three SU(2) singlets

$$S = \frac{1}{\sqrt{2}} (\bar{\alpha} \alpha + \bar{\beta} \beta)$$

$$S(0) = 0 \quad (0)$$

$$S(1) = 0 \quad (1)$$

$$S(2) = 0 \quad (2)$$

# p-wave bosons

three SU(2) triplets

$$T^+ = \bar{\beta}\alpha \quad T^- = \bar{\alpha}\beta \quad T^0 = \frac{1}{\sqrt{2}}(\bar{\alpha}\alpha - \bar{\beta}\beta)$$

$$T(0) = 1 \quad (0)$$

$$T(1) = 1 \quad (1)$$

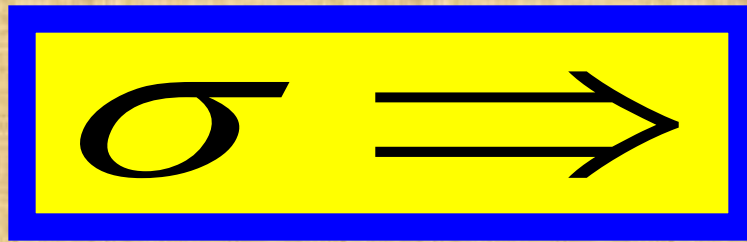
$$T(2) = 1 \quad (2)$$

# p-wave mesons ( QCD )

*scalar* :  $\sigma(\sim 700)$

*vector* :  $h_1(1170)$

*tensor* :  $f_2(1270)$

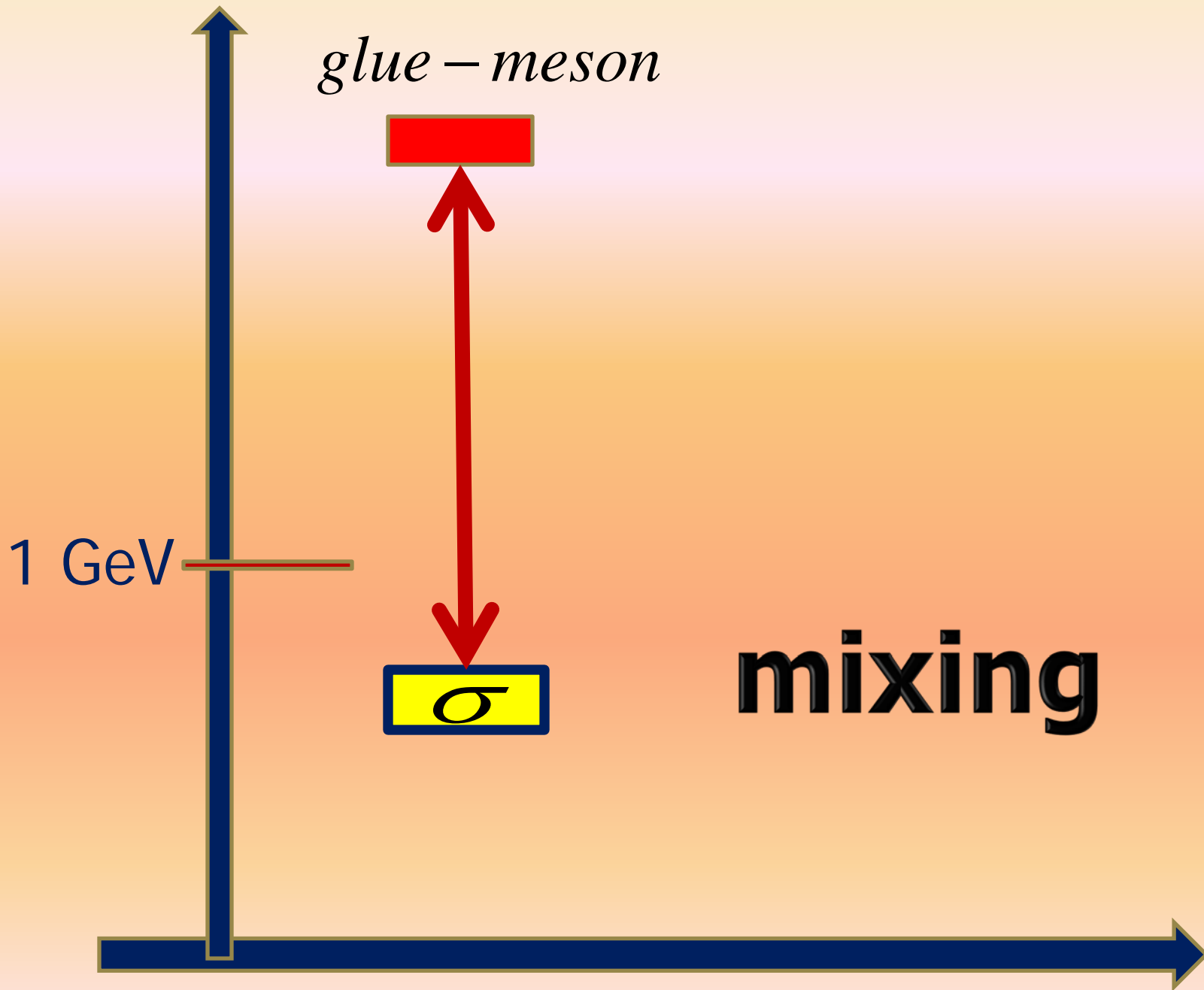


strong mixing

with

glue mesons

**$\Rightarrow$  low mass**





# analogy

$$\sigma(\sim 700) \quad \Rightarrow \quad S(0)$$

$$h_1(1170) \quad \Rightarrow \quad S(1)$$

$$f_2(1270) \quad \Rightarrow \quad S(2)$$

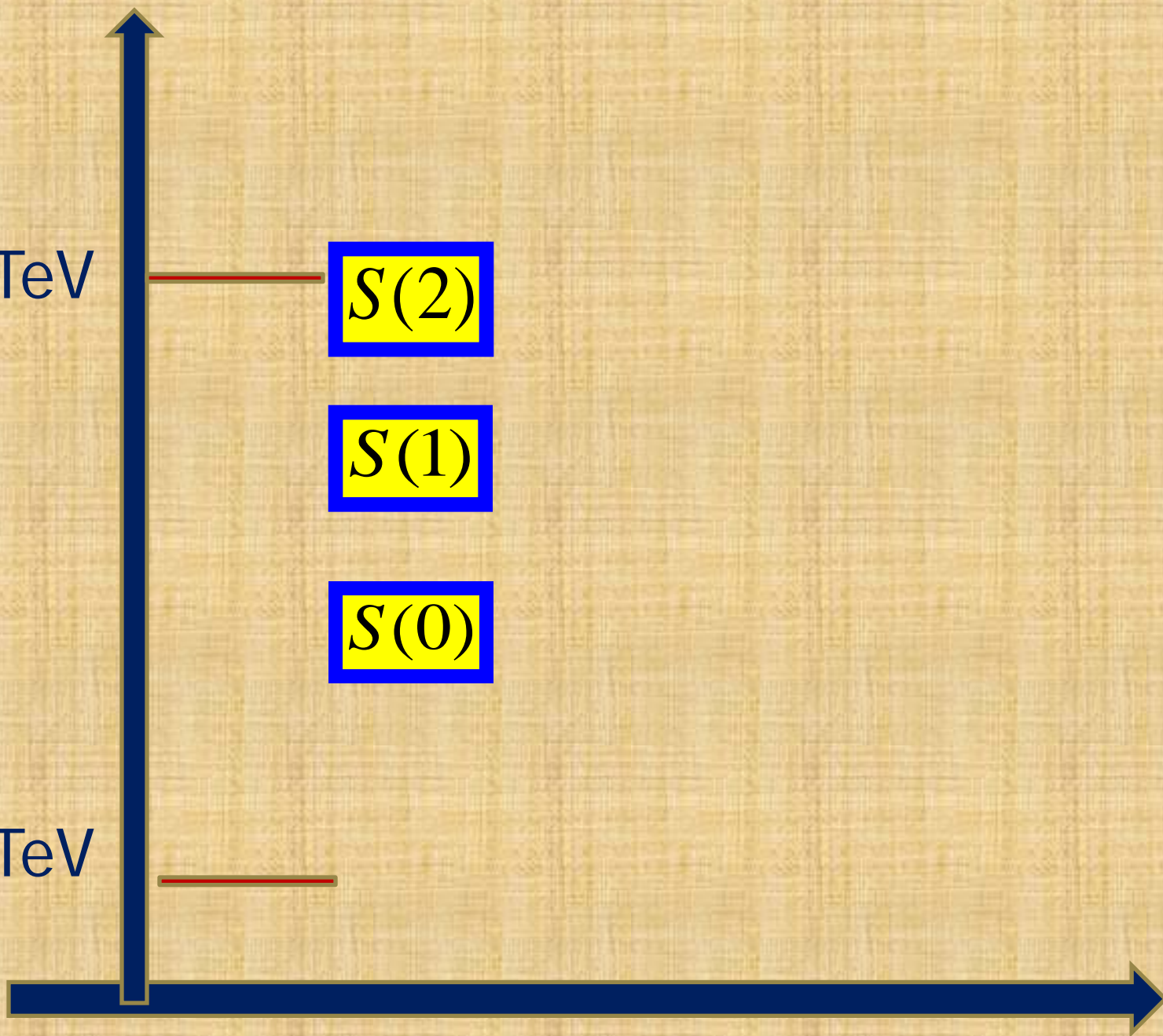
0.5 TeV

$S(2)$

$S(1)$

$S(0)$

0.1 TeV



$S(0)$

strong mixing

with

gluon bosons

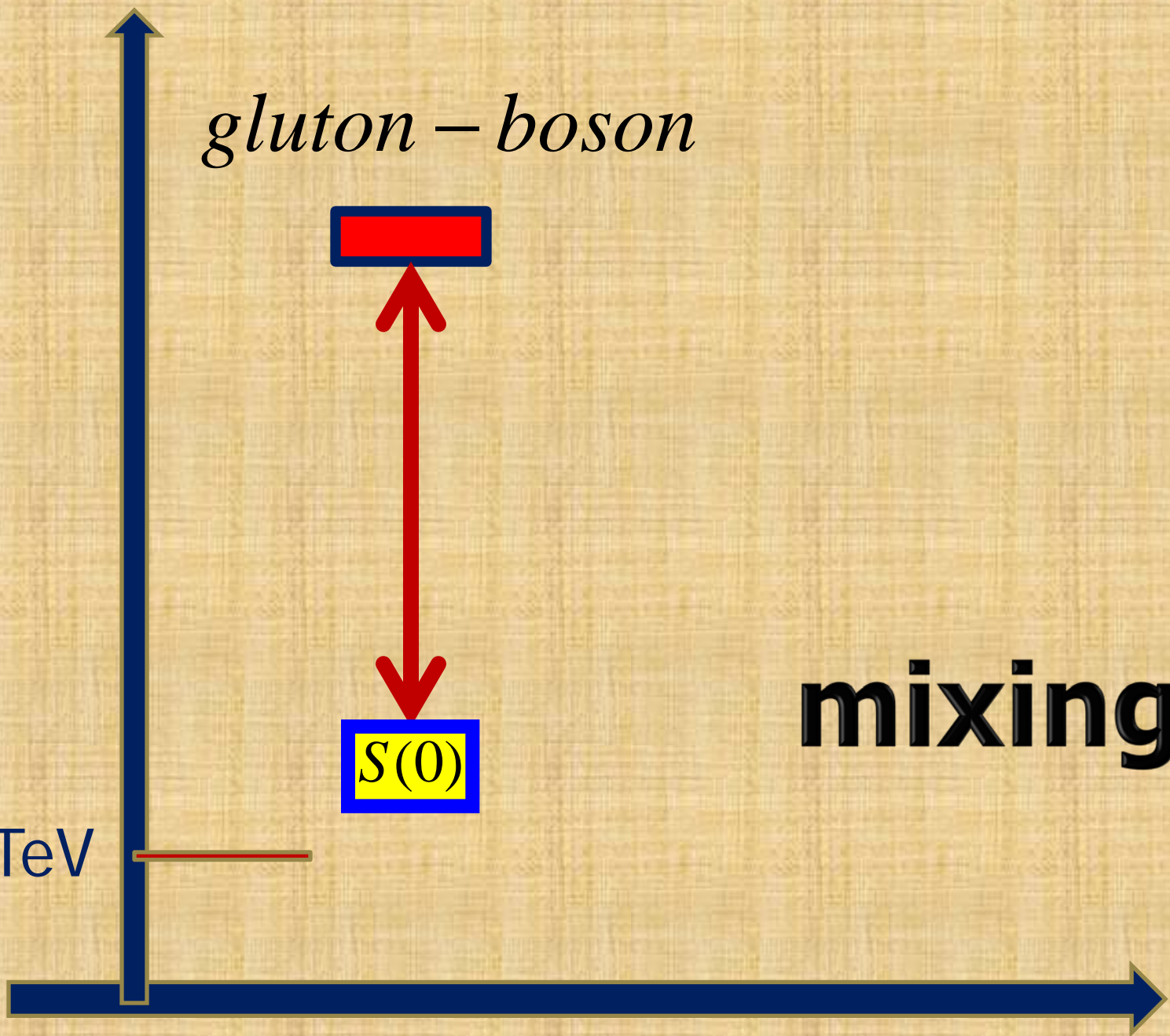
**=> low mass**

*gluton – boson*

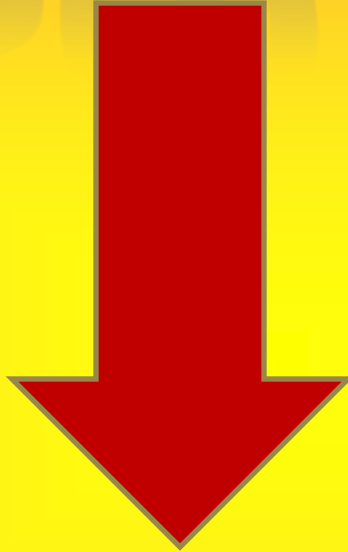


**mixing**

0.1 TeV

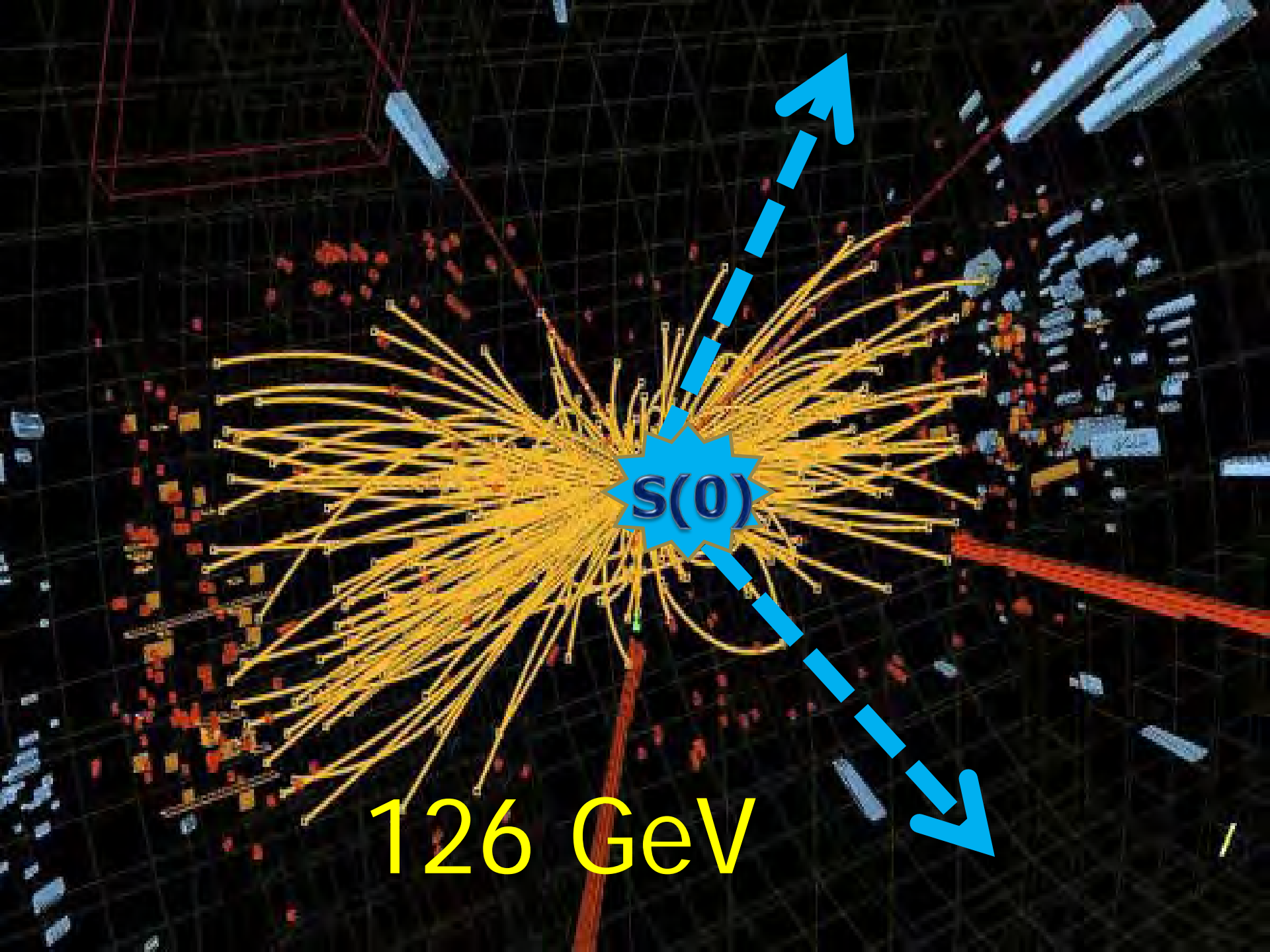


**S(0)**



**LHC**

**? 126 GeV ?**



$S(0)$

126 GeV

# isospin triplets in QCD

*scalar* :  $a_0(980)$

*vector* :  $b_1(1235)$

*tensor* :  $f_2(1270)$

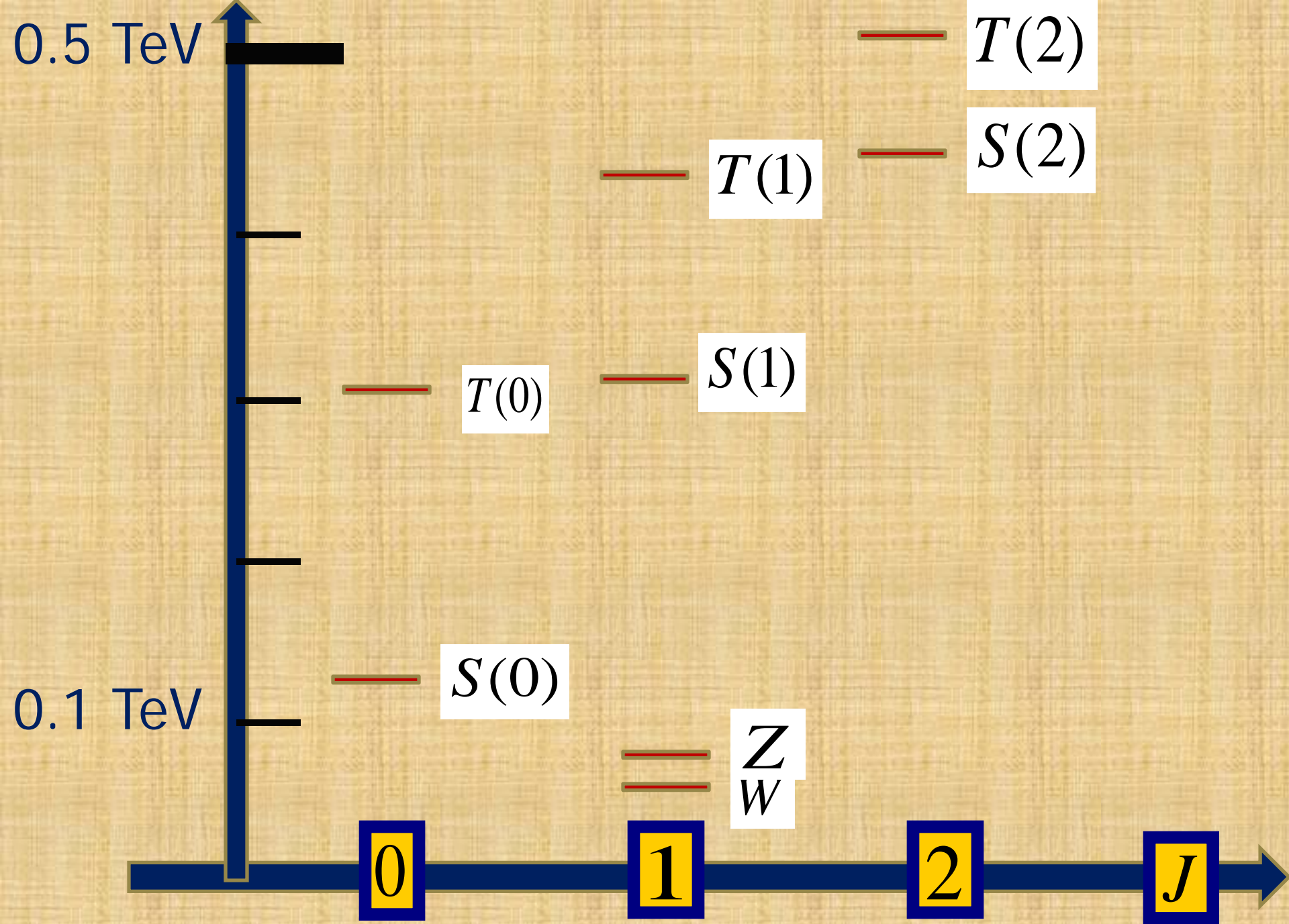
# analogy

$a_0(980) \Rightarrow T(0)$

$b_1(1235) \Rightarrow T(1)$

$f_2(1270) \Rightarrow T(2)$





$$W^3 \Rightarrow 0.77..Z + 0.23..\gamma$$

$$S(0) \Rightarrow W^+ + W^- \quad 100\%$$

$$S(0) \Rightarrow Z + Z \quad 59\%$$

$$S(0) \Rightarrow Z + \gamma \quad 36\%$$

$$S(0) \Rightarrow \gamma + \gamma \quad 5\%$$

$S(0) =$

# decays

$$S(0) \Rightarrow "W^+" + W^-$$

$$S(0) \Rightarrow W^+ + "W^-"$$

$$S(0) \Rightarrow "Z" + Z$$

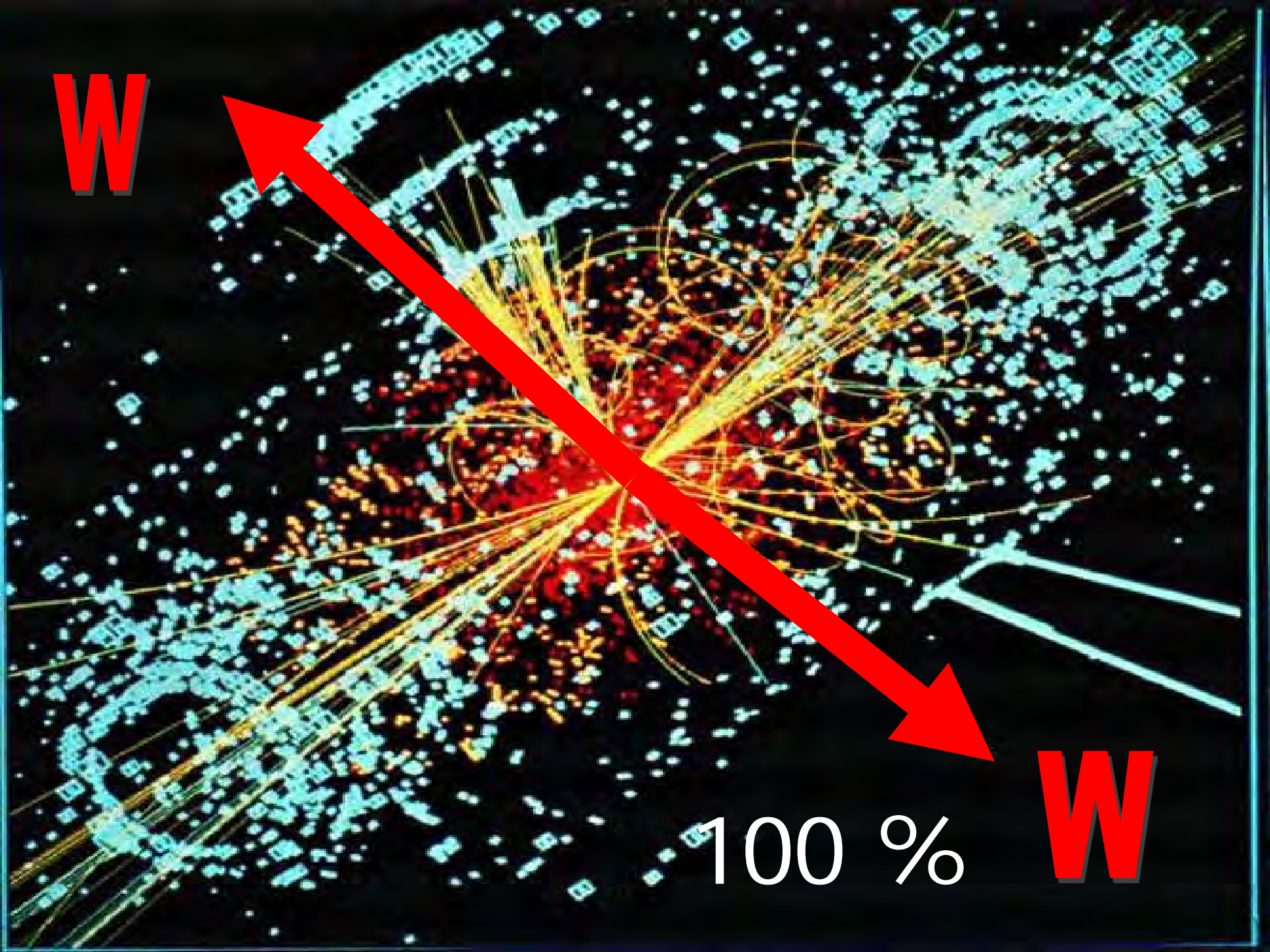
"Z"  $\Rightarrow$  *virtual* Z

$$S(0) \Rightarrow W^+ + W^-$$

$$S(0) \Rightarrow W^- + W^+$$

$$S(0) \Rightarrow W^3 + W^3$$

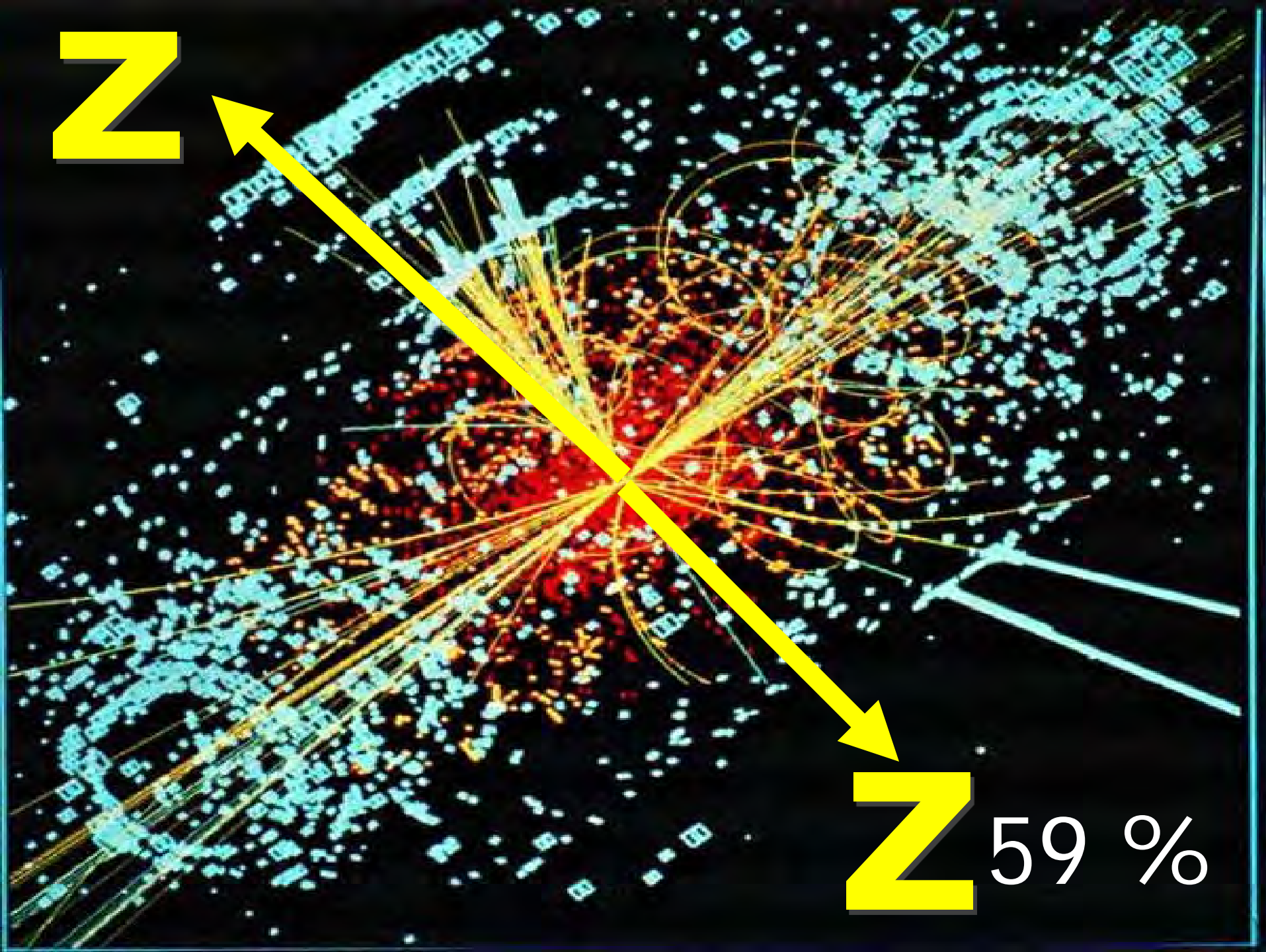
$$W^3 = \cos \theta_w Z + \sin \theta_w \gamma$$

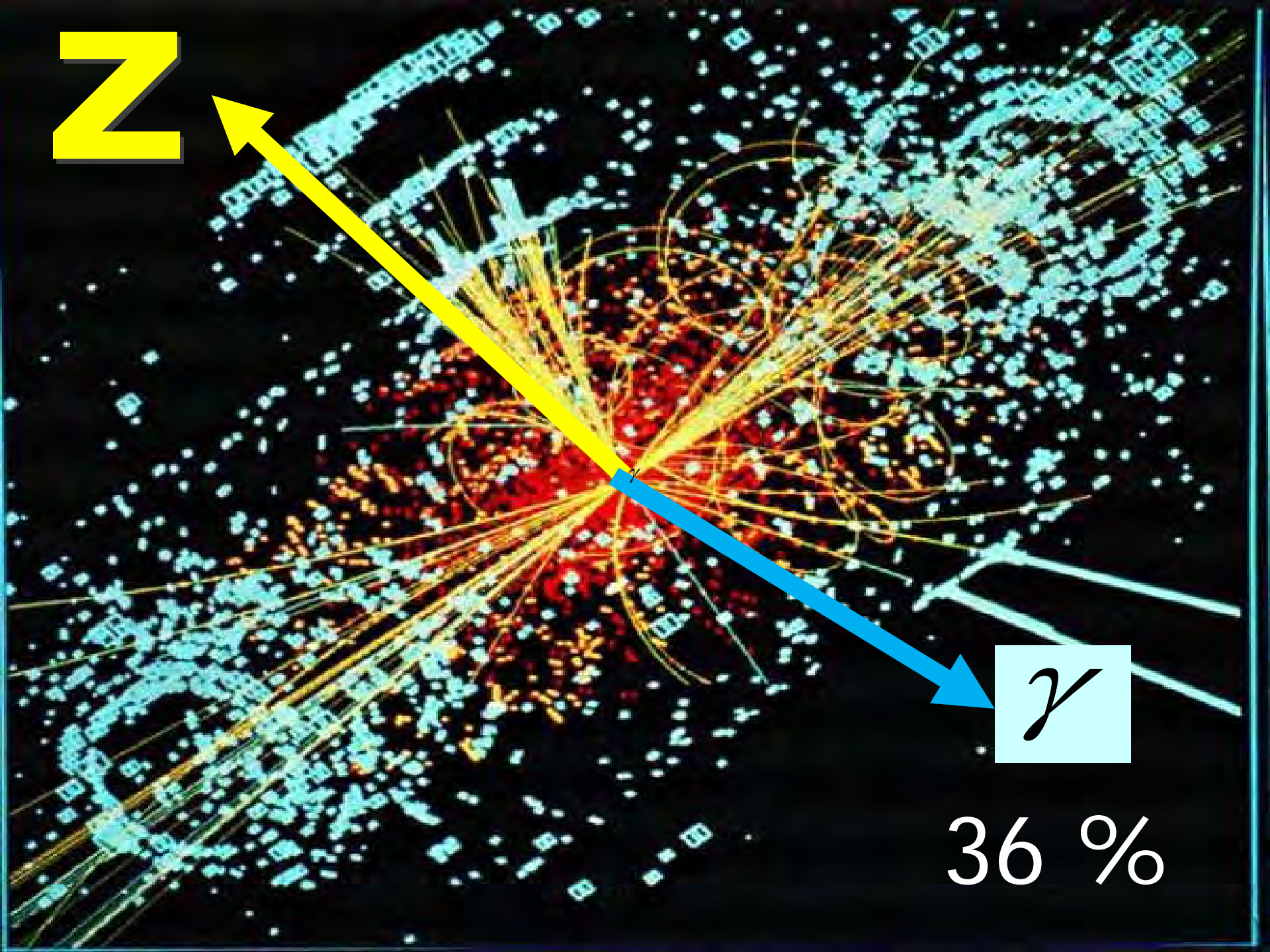


W

100 %

W



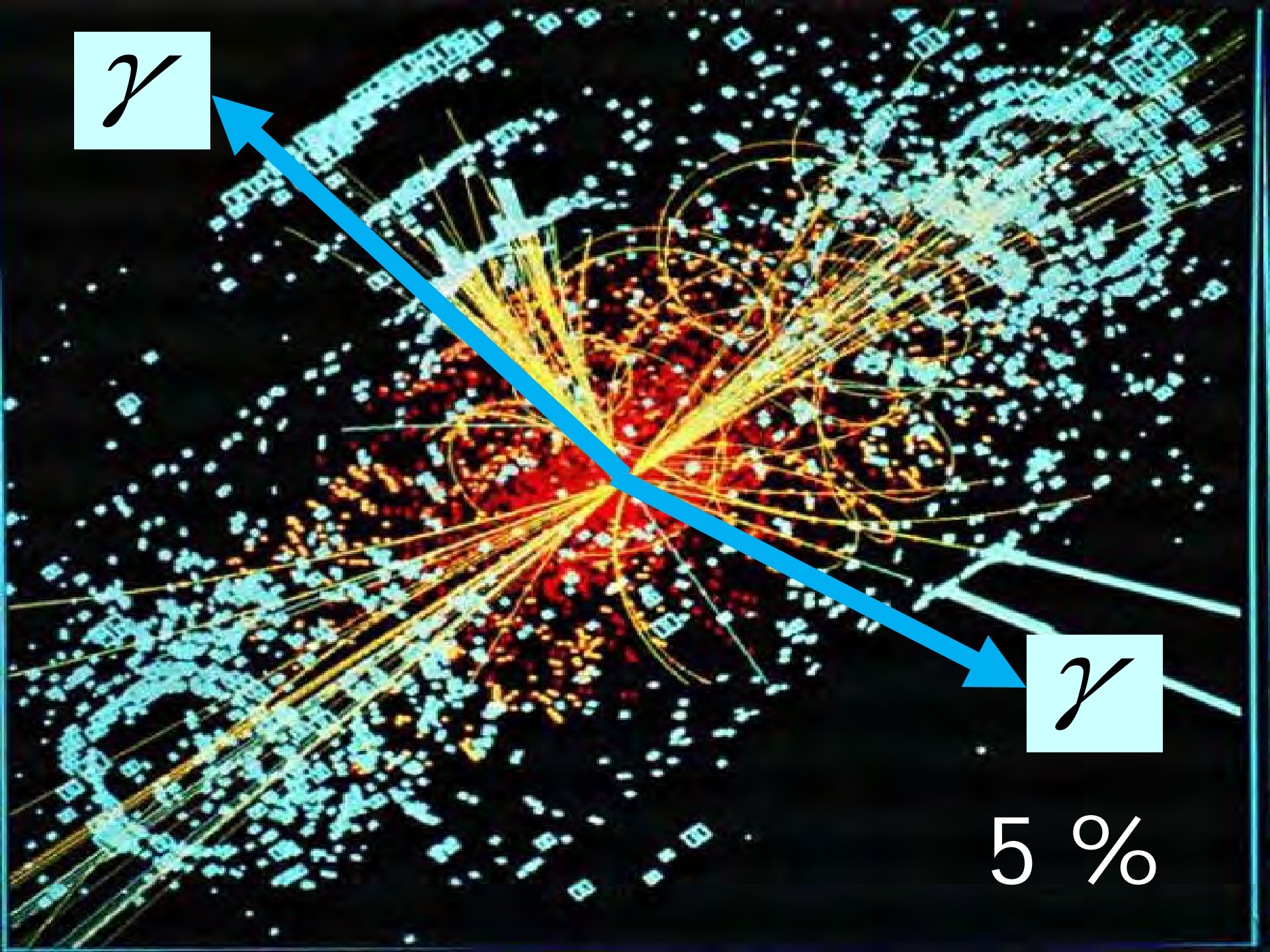


$z$

$\gamma$

36 %

$\gamma$



$\gamma$

5 %



# Experiment

$$\frac{S(0) \Rightarrow \gamma + \gamma}{S(0) \Rightarrow W^+ + W^-} \approx 0.04 \pm 0.015$$

Expected <

**$S(0) : 0.05$**

# „Higgs“ – boson

$$\frac{H \Rightarrow \gamma + \gamma}{H \Rightarrow W^+ + W^-} \approx 0.015$$

**126 GeV**

**„Higgs“ boson**

**decay into leptons**

**electrons : muon : tauons**

**0.000002 : 1 : 286**

**126 GeV**

**S(0)**

**electrons : muon : tauons**

**1 : 1 : 1**

# decays of $S(1)$

$M = 320 \text{ GeV}$

$$S(1) \Rightarrow W^+ + W^-$$

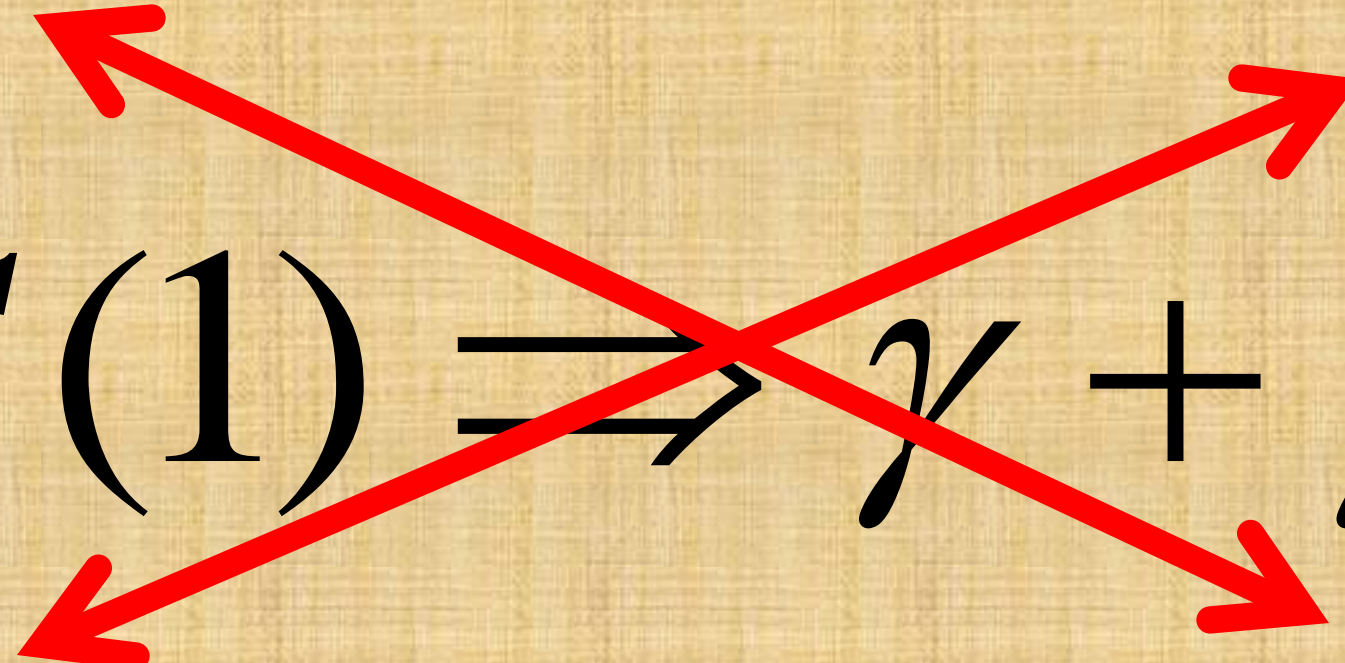
$$S(1) \Rightarrow Z + Z$$

$$S(1) \Rightarrow Z + Z + \gamma$$

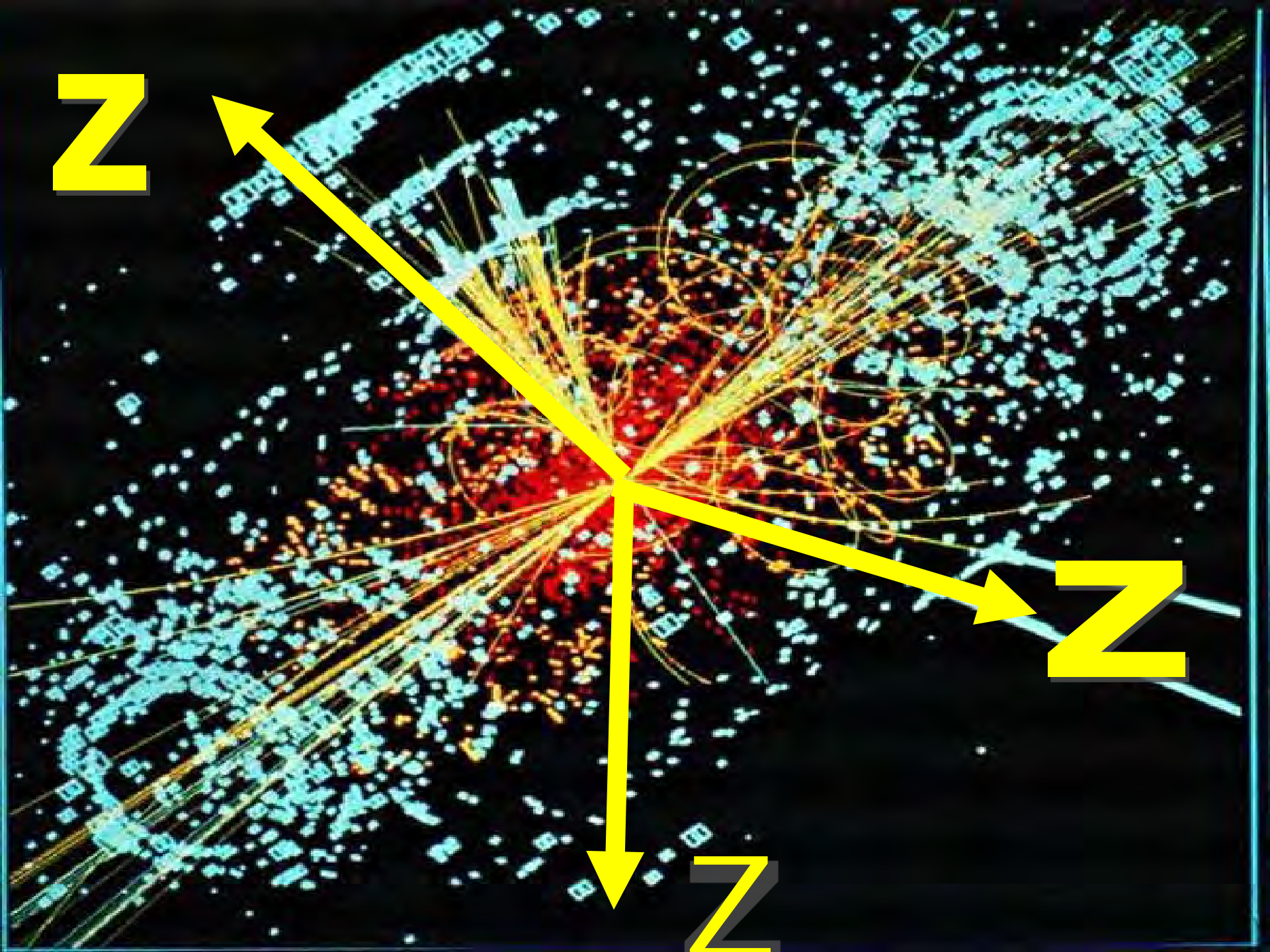
$$S(1) \Rightarrow Z + Z + Z$$

$$S(1) \Rightarrow Z + \gamma + \gamma$$

$$S(1) \Rightarrow \gamma + \gamma + \gamma$$


$$S(1) \Rightarrow \gamma + \gamma$$

**Landau-Yang-Theorem**



three

lepton-quark

families

$$\begin{pmatrix} \nu_e & u & u & u \\ e^- & d & d & d \\ \nu_\mu & c & c & c \\ \mu^- & s & s & s \\ \nu_\tau & t & t & t \\ \tau^- & b & b & b \end{pmatrix}$$

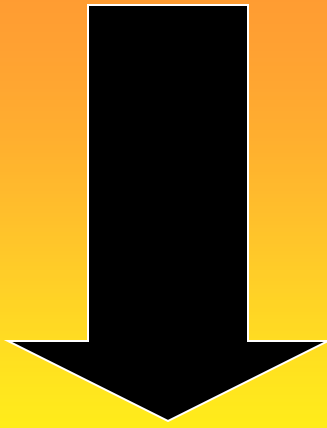


24

? fundamental ?  
fermions

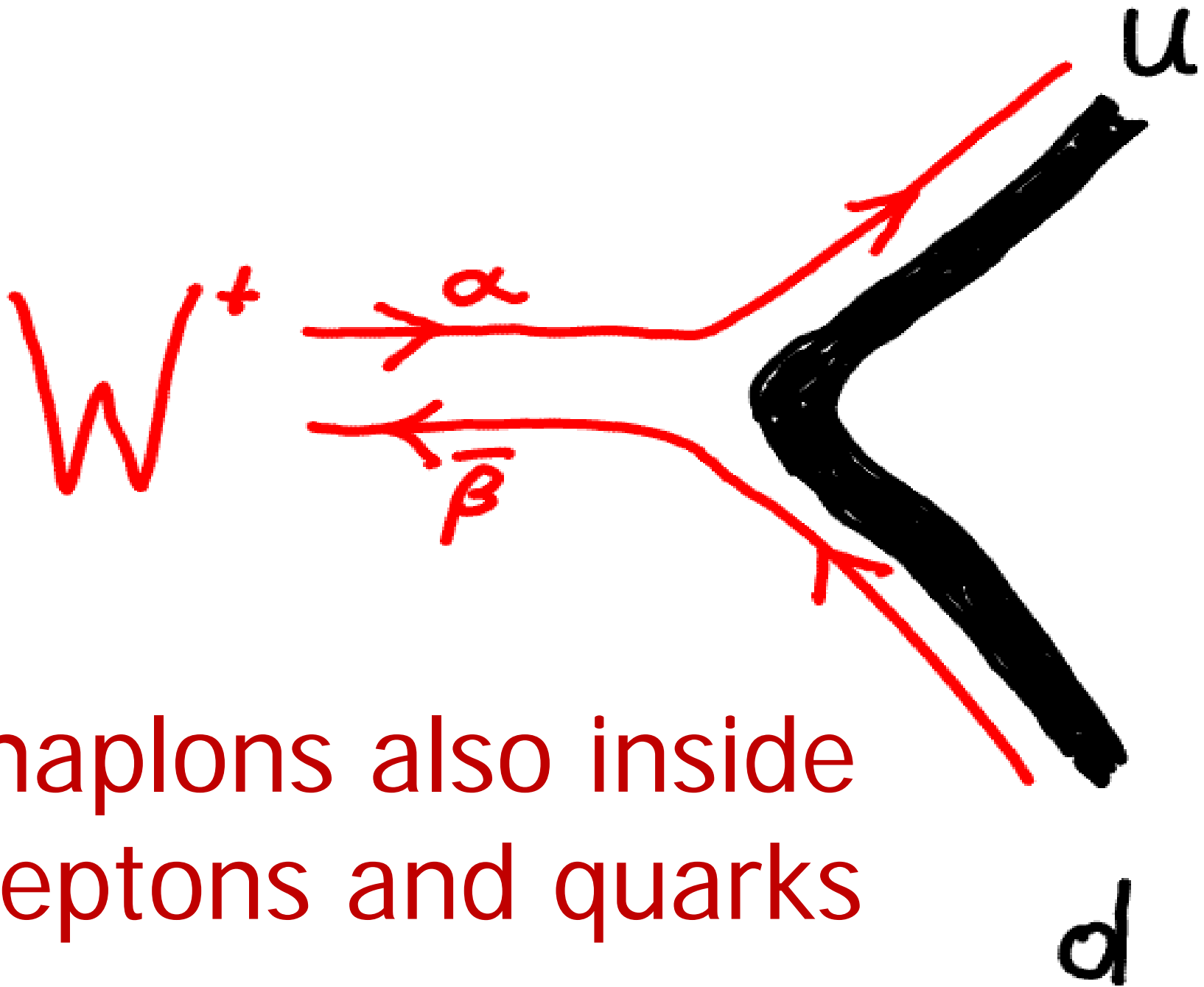
? 12 masses ?

? 10 mixing parameter ?



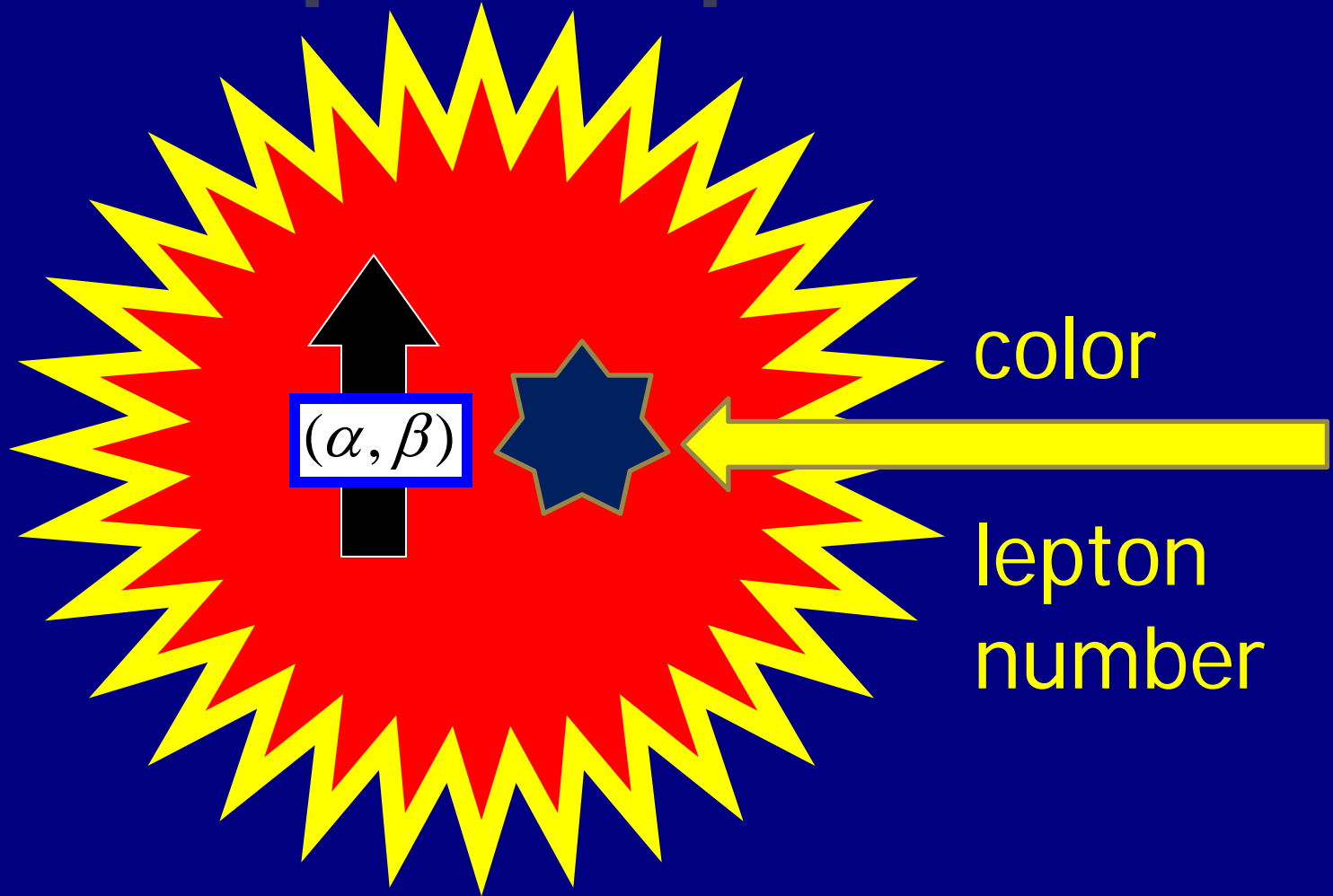
*leptons and quarks*

*→ composite*



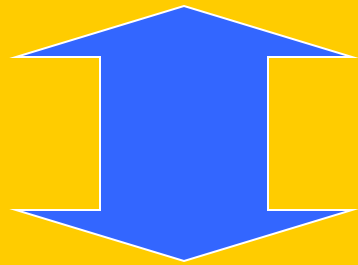
haplons also inside  
leptons and quarks

# leptons - quarks



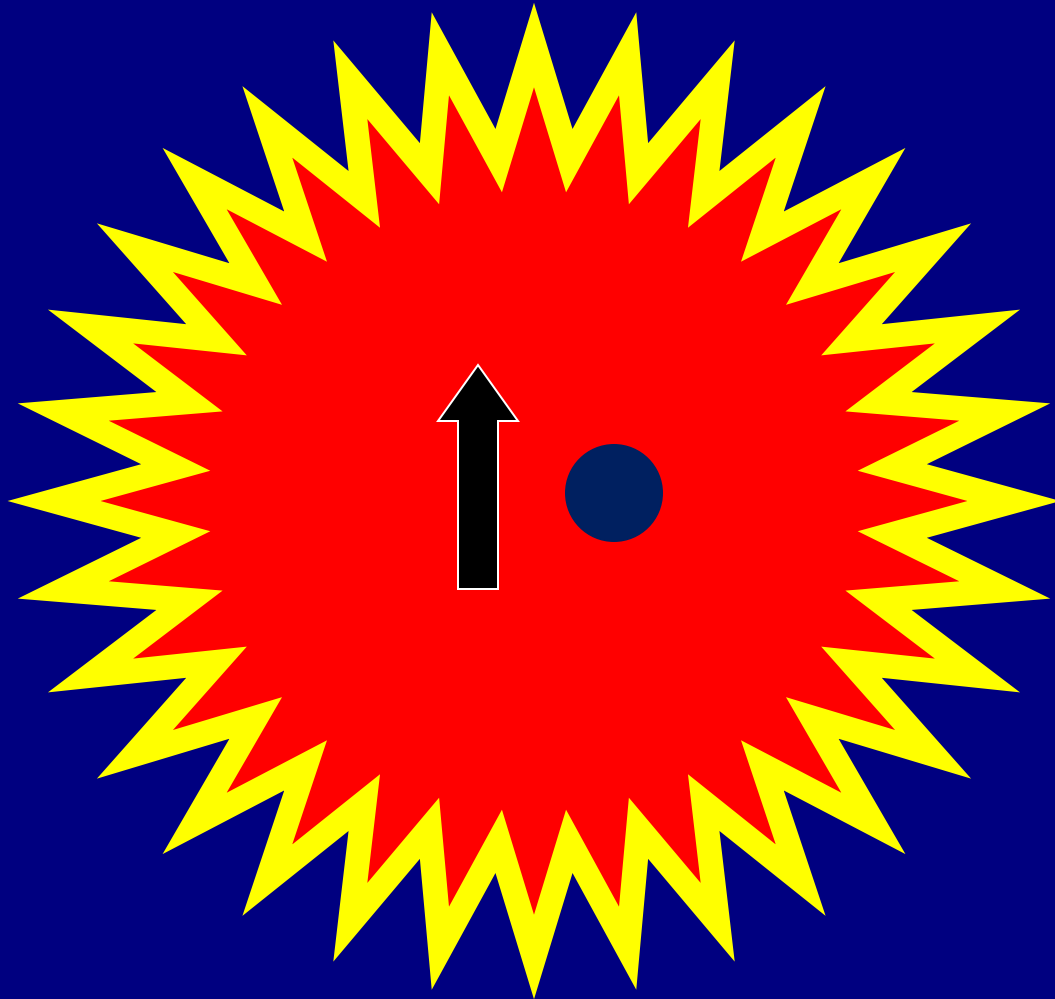
**simplest theory:**

**leptons - quarks**



**(fermion + scalar)**

leptons - quarks



# lepton-quark-family

$$\left( \begin{array}{cccc} \nu & U_r & U_g & U_b \\ L & D_r & D_g & D_b \end{array} \right) \{SU(2)$$

$$\begin{pmatrix} \nu & U_r & U_g & U_b \\ L & D_r & D_g & D_b \end{pmatrix}$$

$$\{SU(2)\}$$



$$SU(4) \Rightarrow U(1) \otimes SU(3)_c$$





$$\begin{bmatrix} \alpha \\ \beta \end{bmatrix}$$

2 fermions



$\{ SU(4) \}$



$$\begin{bmatrix} \alpha \\ \beta \end{bmatrix}$$

2 fermions



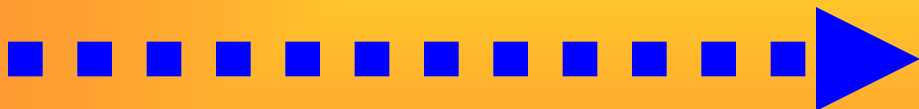
$$\begin{bmatrix} l \\ r \\ g \\ b \end{bmatrix}$$

4 scalars

# 4 scalars



**inside leptons**



**inside quarks**

# electric charges

$$\begin{array}{c} \alpha \\ \beta \end{array} \Rightarrow \begin{pmatrix} 1/2 \\ -1/2 \end{pmatrix} \bullet e$$

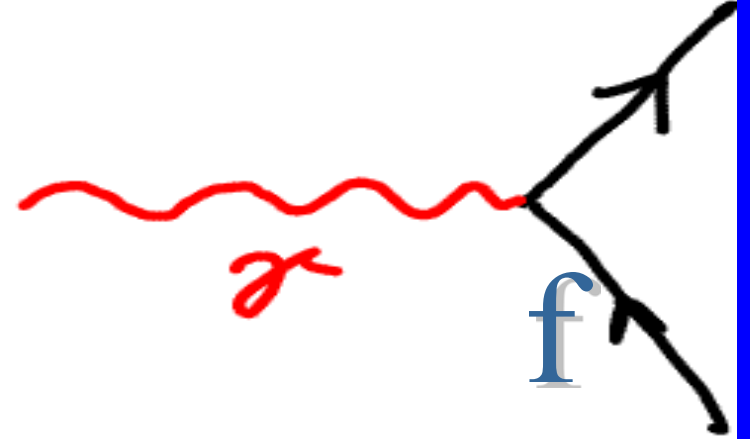
$$r : + \frac{1}{6}$$

$$l : - \frac{1}{2}$$

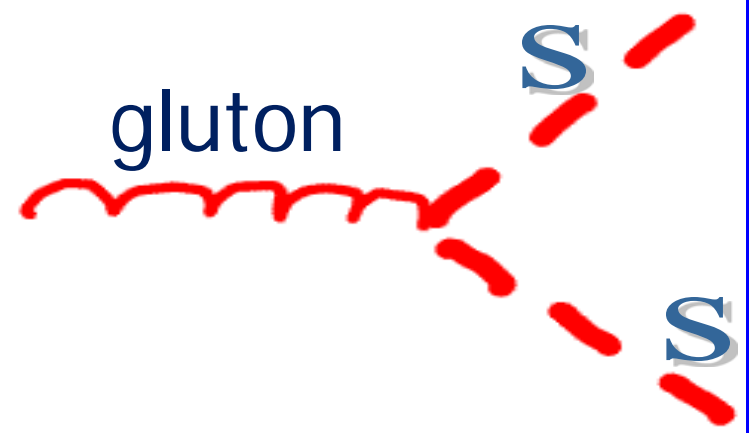
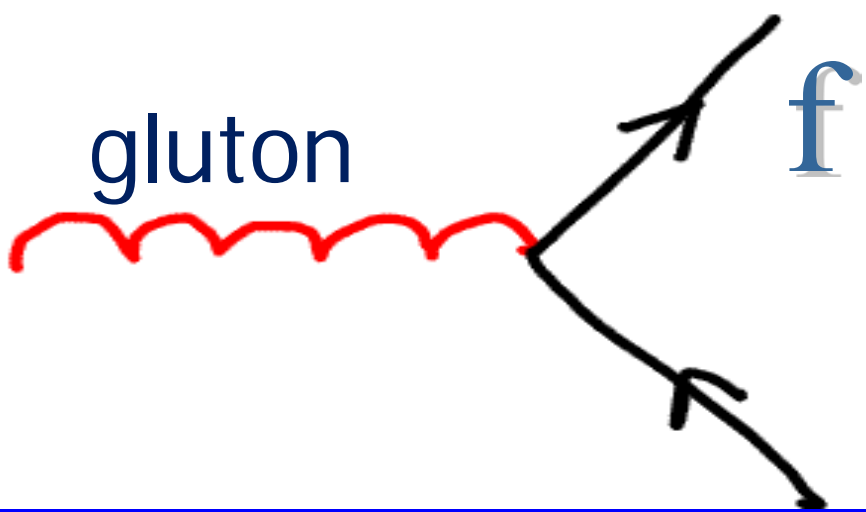
$$g : + \frac{1}{6}$$

$$b : + \frac{1}{6}$$

**charges  
quantized !**



# interactions



# leptons

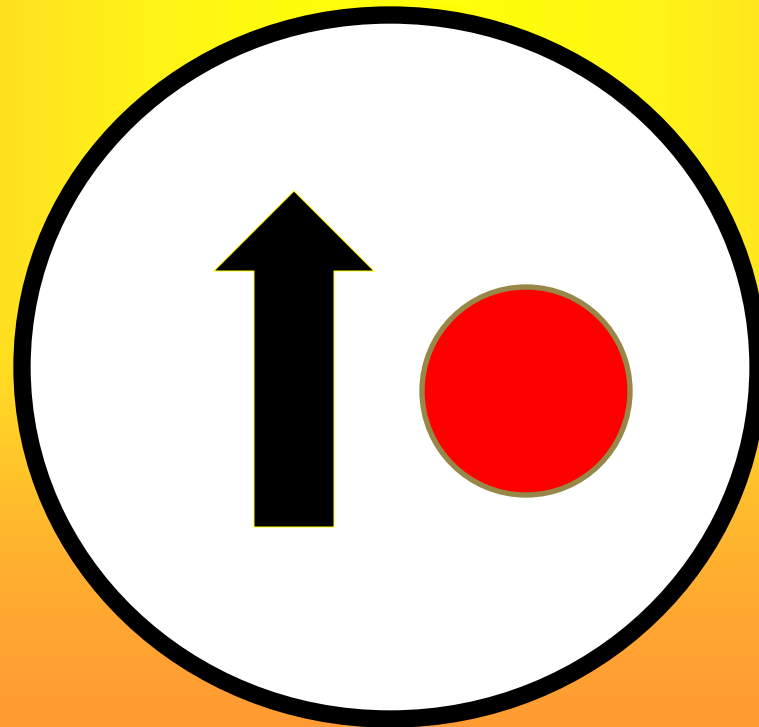
$$(\alpha l) : \nu_e - \nu_\mu - \nu_\tau$$

$$(\beta l) : e - \mu - \tau$$



$(\alpha r) : u_r, c_r, t_r$

$(\beta r) : d_r, s_r, b_r$

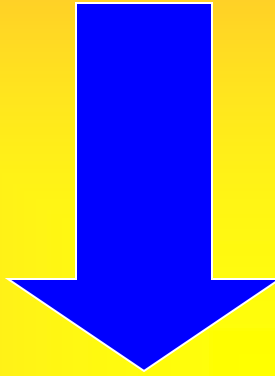


red  
quarks



scalar

fermion



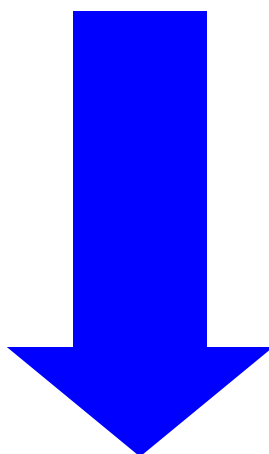
**electron**





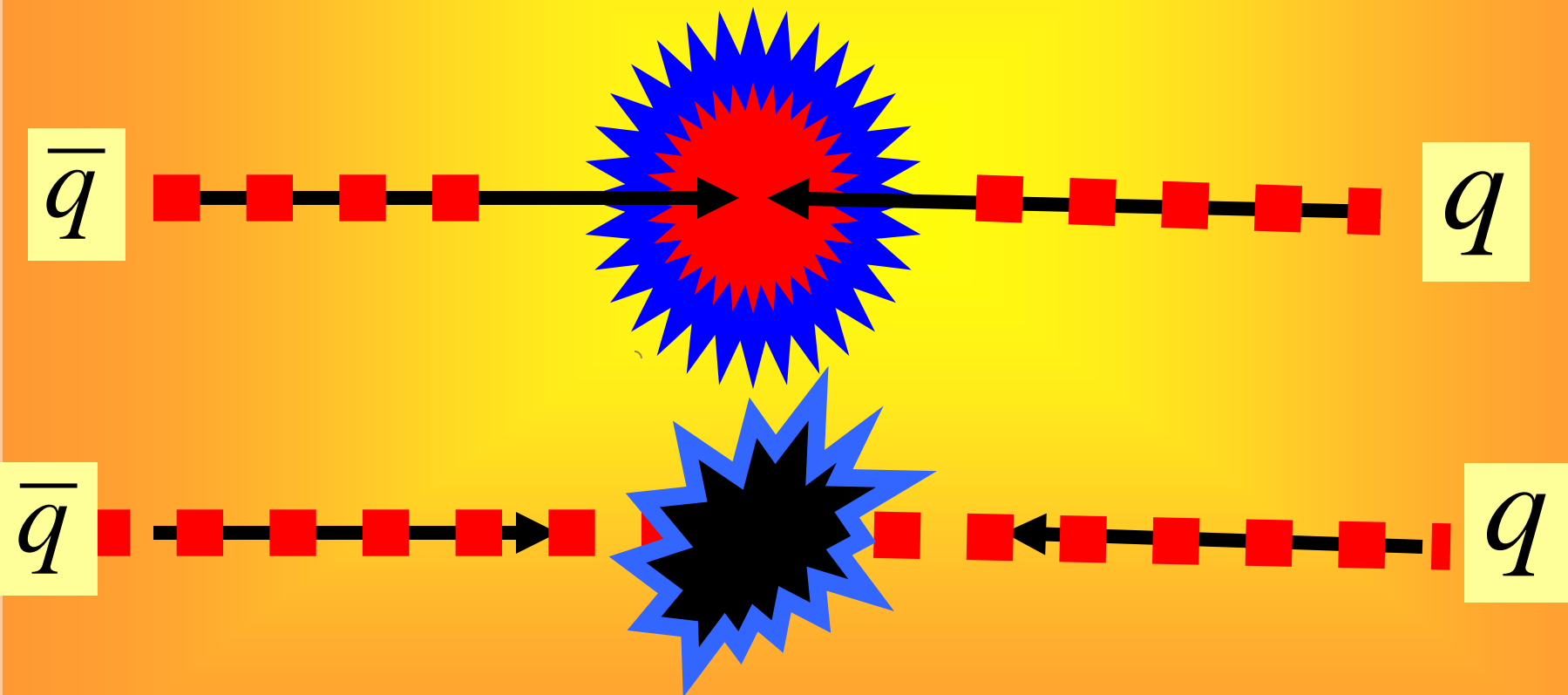
scalar

fermion



**red quark**

# quark – antiquark scattering:



$q$



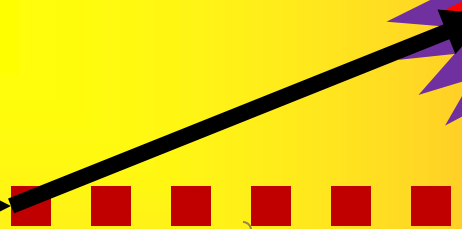
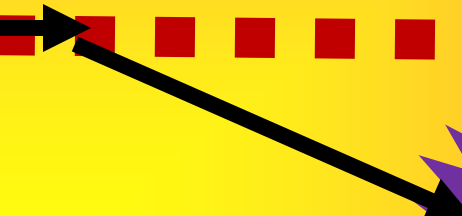
$\bar{q}$

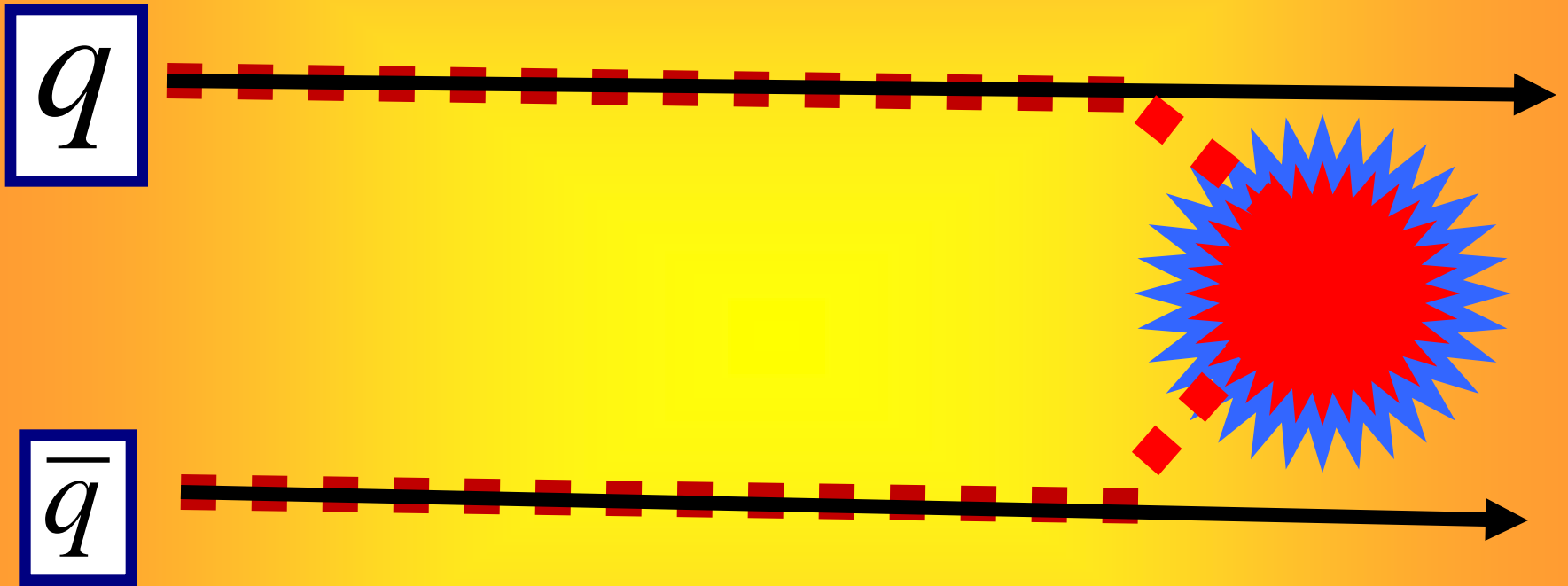


$q$

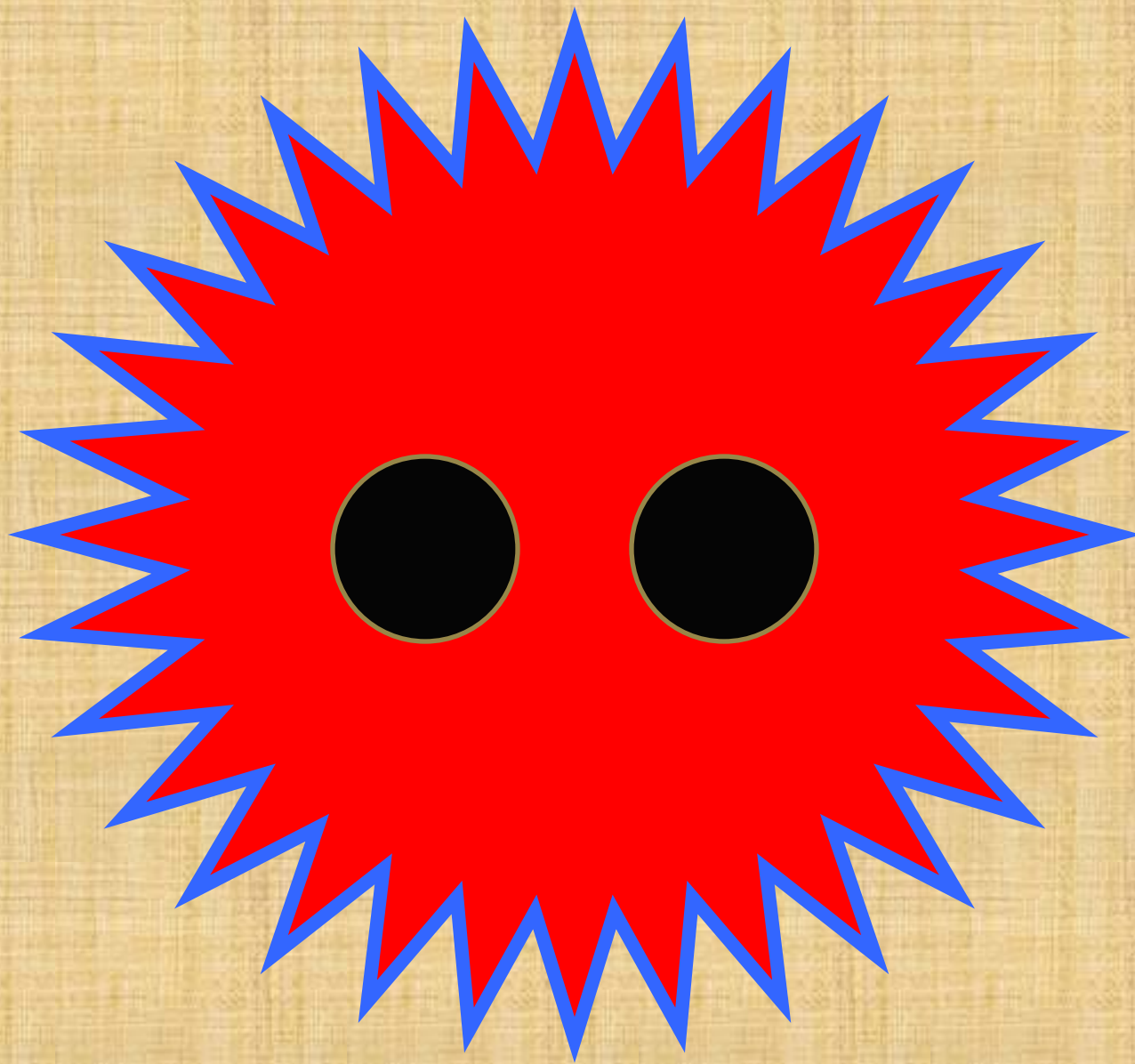


$\bar{q}$



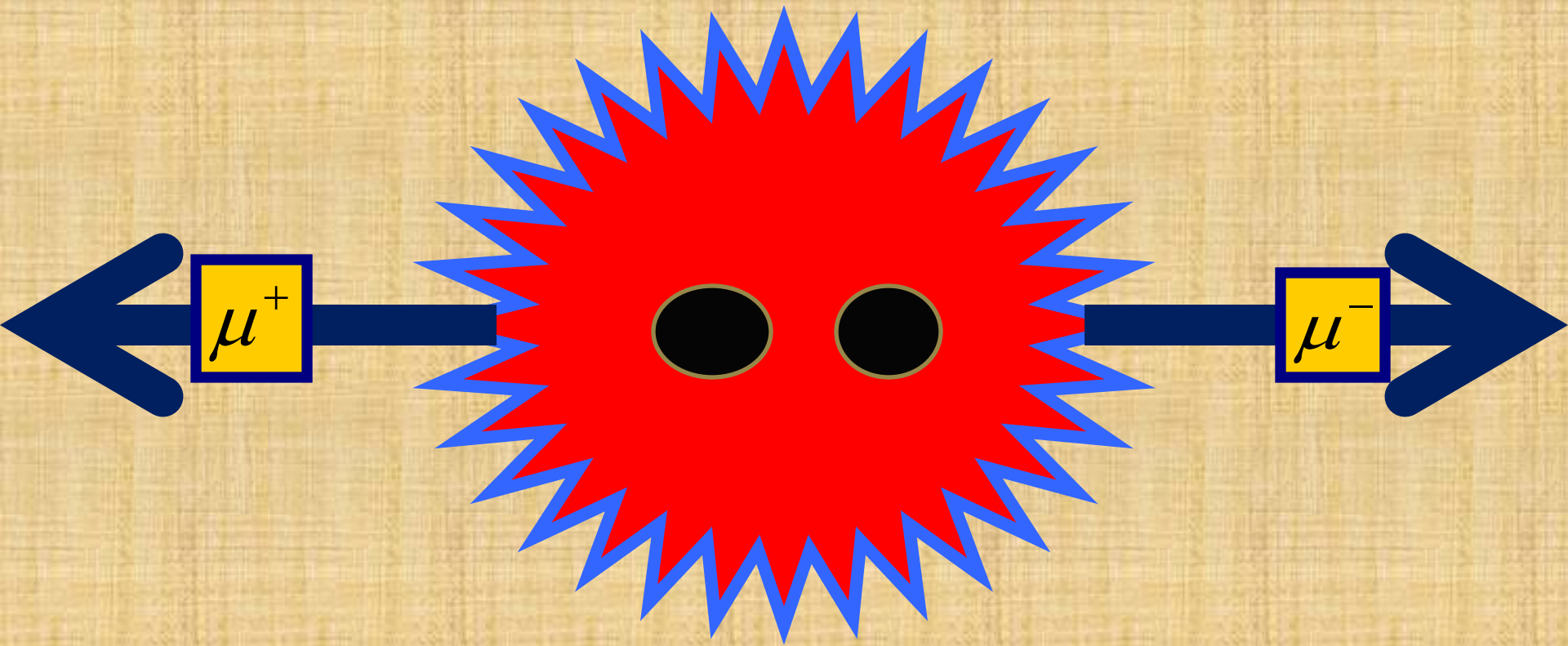


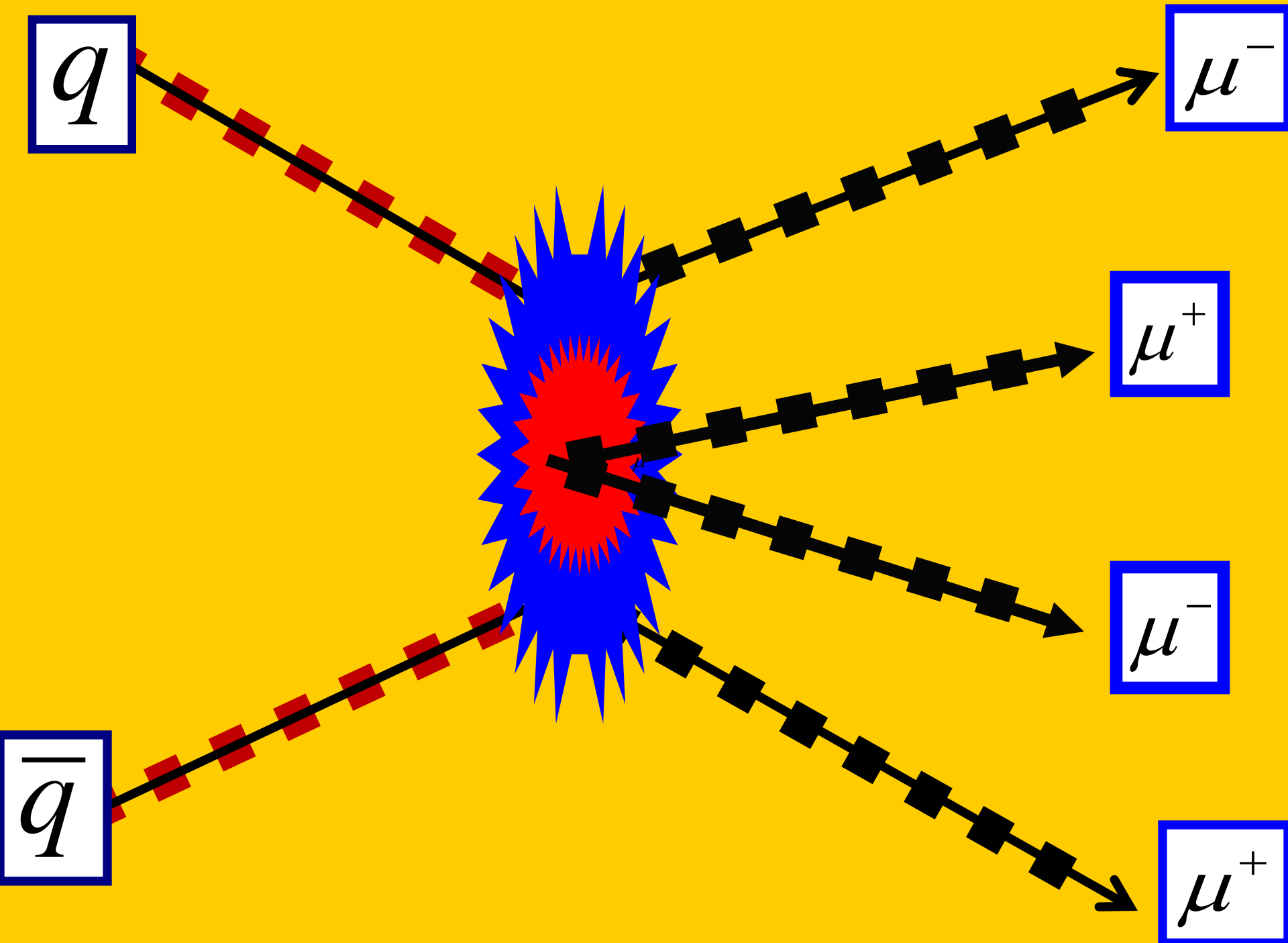
bound states of two scalars



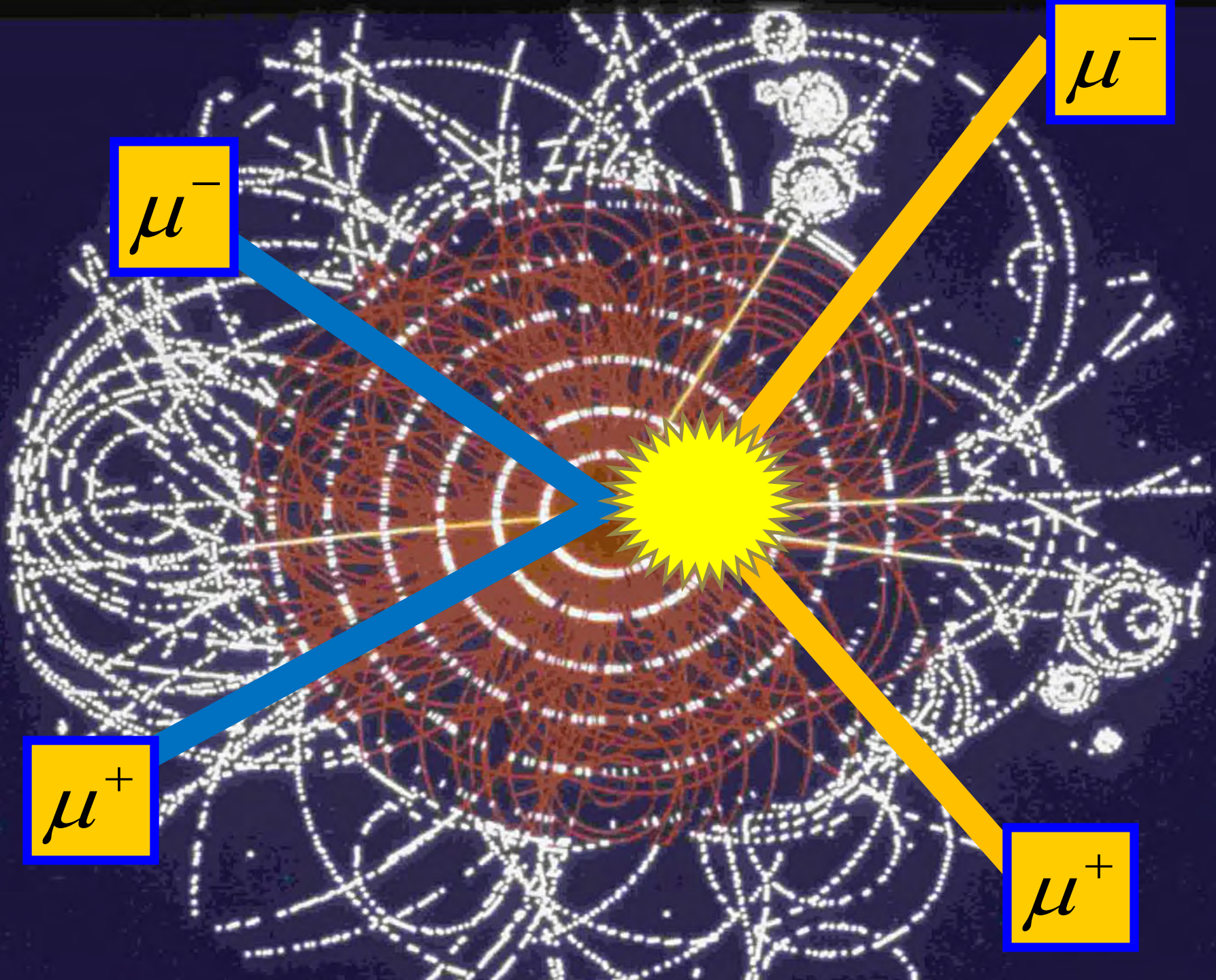
**$M > 0.5 \text{ TeV} ?$**

decay into leptons and quarks









$\mu^-$

$\mu^-$

$\mu^+$

$\mu^+$

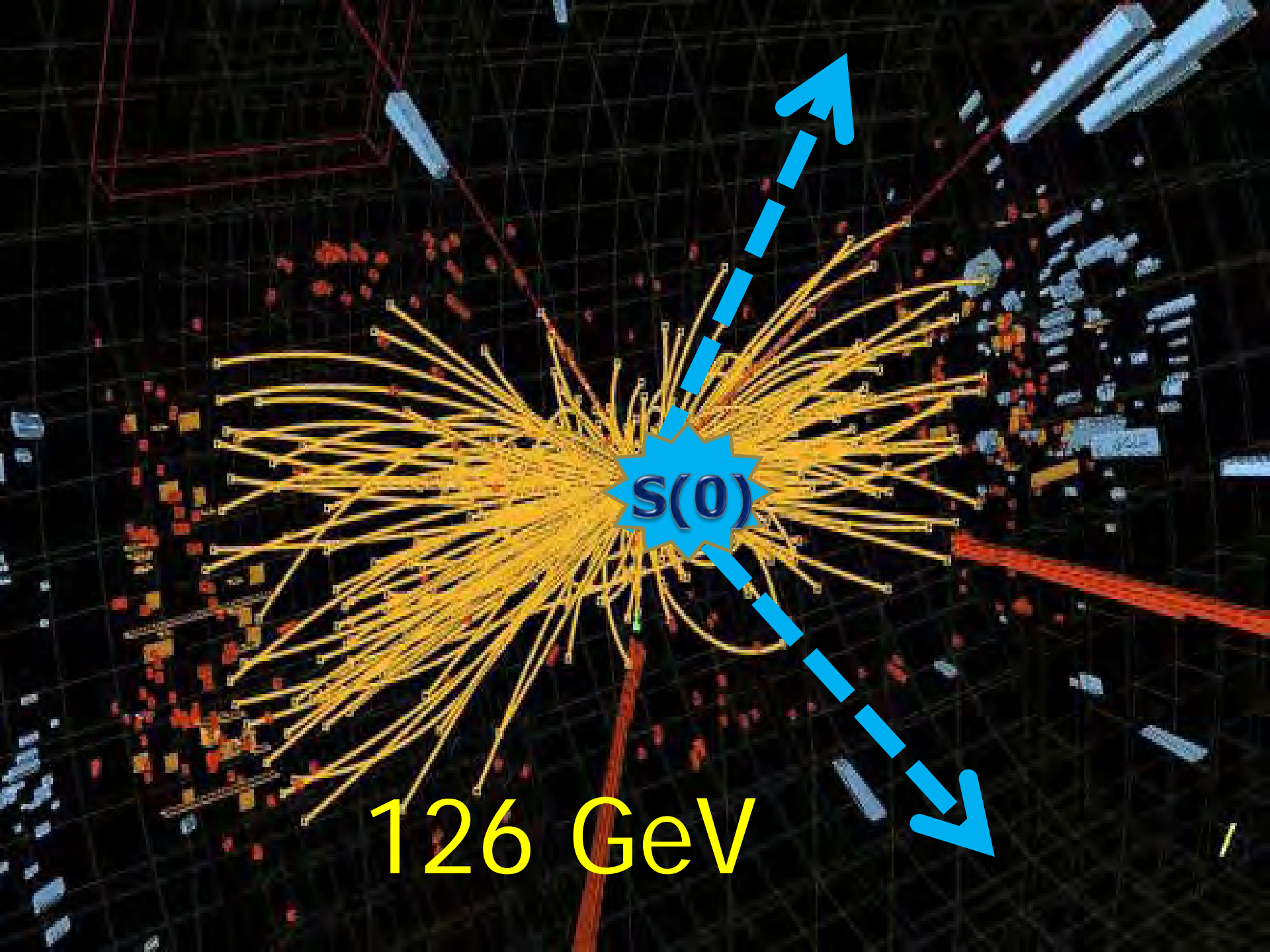
# conclusions

weak bosons

leptons

quarks

⇒ composite



$S(0)$

126 GeV

$S(0)$

excited

weak boson

Spin 0

many QHD resonances

above  
1 TeV

LHC